CS 677: Parallel Programming for Many-core Processors Lecture 7

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Logistics

- Midterm: March 27 (after spring break)
 - Closed book
 - All notes from weeks 2 to 7, except for:
 - MRI case study
 - prefix sum
 - No version-specific details and parameters
 - Device parameters will be provided if necessary

Overview

- Homework 4
- Parallel Patterns: Parallel Prefix Sum (Scan)
 Part II
- Case Study Electrostatic Potential Calculation

 A class project at UIUC also resulting in publications
 Chapter 12 in K&H
- Input Binning
 - From NVIDIA and University of Houston

Homework Assignment 4

• Apply Sobel filter on (grayscale) images

$$G_x = \begin{bmatrix} -1 & 0 & 1 \\ -2 & 0 & 2 \\ -1 & 0 & 1 \end{bmatrix} \qquad G_y = \begin{bmatrix} -1 & -2 & -1 \\ 0 & 0 & 0 \\ 1 & 2 & 1 \end{bmatrix}$$

Homework Assignment 4: CPU Version

```
for (i = 1; i < ImageNRows - 1; i++)
  for (j = 1; j < ImageNCols -1; j++)
  {
      sum1 = u[i-1][j+1] - u[i-1][j-1]
            + 2 * u[i][j+1] - 2 * u[i][j-1]
            + u[i+1][j+1] - u[i+1][j-1];
      sum2 = u[i-1][j-1] + 2 * u[i-1][j]
            + u[i-1][j+1] - u[i+1][j-1]
            - 2 * u[i+1][j] - u[i+1][j+1];
      magnitude = sum1*sum1 + sum2*sum2;
      if (magnitude > THRESHOLD)
            e[i][j] = 255;
      else
            e[i][j] = 0;
```

}

Homework Assignment 4



- Compute magnitude of filter response $G_x^2 + G_y^2$ and output:
 - 0 if magnitude below threshold
 - 255 if magnitude above threshold
 - 0 pixel is within 1 pixel of image border

Example Output





Open Questions

- Memory bandwidth
- 1D vs. 2D block structure
 Fetching of pixels at block boundaries
- I prefer solutions without padding, but you can pad for a 10% penalty
- Solutions using global memory only will receive little credit

The PPM Image Format

- PPM is a very simple format
- Each image file consists of a header followed by all the pixel data
- Header

P6 # comment 1 # comment 2 P3 means ASCII file P6 means binary (most practical)

#comment n rows columns maxvalue pixels See filereading code in homework zip file

Use Gimp or IrfanView to manipulate images and convert between formats

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Reading the Header

```
fp = fopen(filename, "rb");
...
int num = fread(chars, sizeof(char), 1000, fp);
if (chars[0] != 'P' || chars[1] != '6')
{
   fprintf(stderr, "ERROR file '%s' does not
      start with \"P6\"
                           I am expecting a binary
      PPM file\n", filename);
   return NULL;
}
                                       check for "P6"
                                       in first line
```

Reading the Header (cont)

```
unsigned int width, height, maxvalue;
char *ptr = chars+3; // P 6 newline
if (*ptr == '#') // comment line!
                                     skip over comments by
                                     looking for # in first
{
     ptr = 1 + strstr(ptr, "\n");
                                     column
}
&width, &height, &maxvalue);
fprintf(stderr, "read %d things width %d height %d
     maxval %d\n", num, width, height, maxvalue);
*xsize = width;
*ysize = height;
*maxval = maxvalue;
```

Reading the Data

```
// allocate buffer to read the rest of the file into
int bufsize = 3 * width * height * sizeof(unsigned char);
if ((*maxval) > 255) bufsize *= 2;
unsigned char *buf = (unsigned char *)malloc( bufsize );
```

A Kogge-Stone Parallel Scan Algorithm



Improving Efficiency

• A common parallel algorithm pattern:

Balanced Trees

- Build a balanced binary tree on the input data and sweep it to and from the root
- Tree is not an actual data structure, but a concept to determine what each thread does at each step
- For scan:
 - Traverse down from leaves to root building partial sums at internal nodes in the tree
 - Root holds sum of all leaves
 - Traverse back up the tree building the scan from the partial sums

Brent-Kung Parallel Scan - Reduction Step



Inclusive Post Scan Step



Inclusive Post Scan Step





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Reduction Step Kernel Code

```
_global__ void Brent_Kung_scan_kernel(float *X, float *Y,
int InputSize) {
   __shared__ float XY[SECTION_SIZE];
int i = 2*blockIdx.x*blockDim.x + threadIdx.x;
if (i < InputSize) XY[threadIdx.x] = X[i];
if (i+blockDim.x < InputSize) XY[threadIdx.x+blockDim.x] = X[i+blockDim.x];
for (unsigned int stride = 1; stride <= blockDim.x; stride *= 2) {
   __syncthreads();
   int index = (threadIdx.x+1) * 2* stride -1;
   if (index < SECTION_SIZE) {
      XY[index] += XY[index - stride];
   }
}
```

```
// threadIdx.x+1 = 1, 2, 3, 4....
// stride = 1, index =
```


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Kernel Function

```
_global__ void Brent_Kung_scan_kernel(float *X, float *Y,
int InputSize) {
```

```
shared float XY[SECTION SIZE];
int i = 2*blockIdx.x*blockDim.x + threadIdx.x;
if (i < InputSize) XY[threadIdx.x] = X[i];
if (i+blockDim.x < InputSize) XY[threadIdx.x+blockDim.x] = X[i+blockDim.x];
for (unsigned int stride = 1; stride <= blockDim.x; stride *= 2) {
  syncthreads();
 int index = (threadIdx.x+1) * 2* stride -1;
 if (index < SECTION SIZE) {
   XY[index] += XY[index - stride];
}
for (int stride = SECTION SIZE/4; stride > 0; stride /= 2) {
 syncthreads();
 int index = (threadIdx.x+1)*stride*2 - 1;
 if(index + stride < SECTION_SIZE) {
   XY[index + stride] += XY[index];
}
____syncthreads();
if (i < InputSize) Y[i] = XY[threadIdx.x];
if (i+blockDim.x < InputSize) Y[i+blockDim.x] = XY[threadIdx.x+blockDim.x];
```

Work Analysis

- The parallel Inclusive Scan executes 2 log(n) parallel iterations
 - log(n) in reduction and log(n) in post scan
 - The iterations do n/2, n/4,..1, 1, ..., n/4. n/2 adds
 - − Total adds: $2(n-1) \rightarrow O(n)$ work
 - The total number of adds is no more than twice of that done in the efficient sequential algorithm
 - The benefit of parallelism can easily overcome the 2x work when there is sufficient hardware

A Couple of Details

- Brent-Kung uses half the number of threads compared to Kogge-Stone
 - Each thread should load two elements into the shared memory
- Brent-Kung takes twice the number of steps compared to Kogge-Stone
 - Kogge-Stone is more popular for parallel scan with blocks in GPUs

Flow of a Complete Scan - Hierarchical Approach

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Using Global Memory Contents in CUDA

- Data in registers and shared memory of one thread block are not visible to other blocks
- To make data visible, the data has to be written into global memory
- However, any data written to the global memory are not visible until a memory fence. This is typically done by terminating the kernel execution
- Launch another kernel to continue the execution. The global memory writes done by the terminated kernels are visible to all blocks.

Flow of a Complete Scan - Hierarchical Approach

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Working on Arbitrary-Length Input

- Build on the scan kernel that handles up to 2*blockDim.x elements
- For Kogge-Stone, have each section of blockDim.x elements assigned to a block
- Have each block write the sum of its section into a Sum array indexed by blockldx.x
- Run parallel scan on the Sum array
 - May need to break down Sum into multiple sections if it is too big for a block
- Add the scanned Sum array values to the elements of corresponding sections

Electrostatic Potential Calculation

Electrostatic potential map is used in building stable structures for molecular dynamics simulation

Core Computation

• The contribution of atom[i] to the electrostatic potential at lattice point j is atom[i].charge / r_{ii}

• The total potential at lattice point j is the sum of contributions from all atoms in the system

Sequential CPU Code

void cenergy(float *energygrid, dim3 grid, float gridspacing, float z, const float *atoms, int numatoms) { int i,j,n; int atomarrdim = numatoms * 4; Computes a single slice (const z) for (j=0; j < grid.y; j++) { float y = gridspacing * (float); for (i=0; i < grid.x; i++) $\{$ float x = gridspacing * (float) i; float energy = 0.0f; for (n=0; n<atomarrdim; n+=4) { // calculate potential contribution of each atom float dx = x - atoms[n];float dy = y - atoms[n+1];float dz = z - atoms[n+2];energy += atoms[n+3] / sqrtf(dx*dx + dy*dy + dz*dz); } energygrid[grid.x*grid.y*k + grid.x*j + i] = energy;

GPU Implementation

- Option 1: each thread calculates the contribution of one atom to all grid points

 "Scatter"
- Option 2: each thread calculates the accumulated contributions of all atoms to one grid point
 - "Gather"
- Pros/cons?

Loop Transformation

- Need perfectly nested loops
 - as in MRI
 example
 - Move calculation of y into inner loop

```
– Pros/cons?
```

}

for (j=0; j < grid.y; j++) { float y = gridspacing * (float); for (i=0; i<grid.x; i++) { float x = gridspacing * (float) i; float energy = 0.0f; for (n=0; n < atomarrdim; n+=4) { float dx = x - atoms[n]1: float dy = y - atoms[n+1];float dz = z - atoms[n+2];energy += atoms[n+3] / sqrtf(dx*dx + dy*dy + dz*dz); } energygrid[grid.x*grid.y*k + grid.x*j + i] = energy; }

DCS Kernel Design Overview

DCS Kernel Version 1

```
Start global memory reads
float curenergy = energygrid[outaddr];
                                                   early. Kernel hides some of
float coorx = gridspacing * xindex;
                                                        its own latency.
float coory = gridspacing * yindex;
int atomid;
float energyval=0.0f;
for (atomid=0; atomid<numatoms; atomid++) {
 float dx = coorx - atominfo[atomid].x;
 float dy = coory - atominfo[atomid].y;
 energyval += atominfo[atomid].w *
                    rsqrtf(dx*dx + dy*dy + atominfo[atomid].z);
                                                   Only dependency on global
                                                   memory read is at the end of
energygrid[outaddr] = curenergy + energyval;
                                                          the kernel...
                                                                           34
```

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qsqrtf(): reciprocal square root

DCS Kernel Version 1

float curenergy = energygrid[outaddr];	Start global memory reads
float coorx = gridspacing * xindex;	its own latency.
float coory = gridspacing * yindex;	
int atomid;	ILF VS. ILF
float energyval=0.0f;	
<pre>for (atomid=0; atomid<numatoms; atomid++)="" pre="" {<=""></numatoms;></pre>	
float dx = coorx - atominfo[atomid].x;	atominfo[].z is already squared
float dy = coory - atominfo[atomid].y;	П
energyval += atominfo[atomid].w *	ŢŢ
rsqrtf(dx*dx + dy*dy + atominfo[atomid].z);	
}	Only dependency on global
energygrid[outaddr] = curenergy + energyval;	memory read is at the end of the kernel

. . .

Information Reuse

DCS kernel Version 2

...for (atomid=0; atomid<numatoms; atomid++) { float dy = coory - atominfo[atomid].y;float dysqpdzsq = (dy * dy) xatominfo[atomid].z; float x = atominfo[atomid].x;Compared to non-unrolled float $dx_1 = coorx_1 - x;$ kernel: memory loads are float $dx^2 = coorx^2 - x$; decreased by 4x, and FLOPS float dx3 = coorx3 - x;per evaluation are reduced, but float dx4 = coorx4 - x;register use is increased... float charge = atominfo[atomid].w; energyvalx1 += charge * rsqrtf(dx1*dx1 + dysqpdzsq); energyvalx2 += charge * rsqrtf(dx2*dx2 + dysqpdzsq); energyvalx3 += charge * rsqrtf(dx3*dx3 + dysqpdzsq); energyvalx4 += charge * rsqrtf(dx4*dx4 + dysqpdzsq);

Memory Coalescing

- Two issues:
 - Each thread calculates potentials of four adjacent grid points
 - If grid width is not multiple of tile width, boundary management becomes complicated

Memory Layout for Coalescing

DCS Kernel Version 3

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Performance Comparison

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CPU vs. CPU-GPU Comparison

UIUC ECE 598HK

Computational Thinking for Many-core Computing

Input Binning

Objective

- To understand how data scalability problems in gather parallel execution motivate input binning
- To learn basic input binning techniques
- To understand common tradeoffs in input binning

Scatter to Gather Transformation

However

- Input tends to be much less regular than output
 - It may be difficult for each thread to efficiently locate all inputs relevant to its output
 - Or, to efficiently exclude all inputs irrelevant to its output
- In a naïve arrangement, all threads may have to process all inputs to decide if each input is relevant to its output
 - This makes execution time scale poorly with data set size
 - Important problem when processing large data sets

DCS Algorithm for Electrostatic Potentials Revisited

- At each grid point, sum the electrostatic potential from all atoms
 - All threads read all inputs
- Highly data-parallel
- But has quadratic complexity
 - Number of grid points × number of atoms
 - Both proportional to volume
 - Poor data scalability

Algorithm for Electrostatic Potentials With a Cutoff

- Ignore atoms beyond a cutoff distance, r_c
 - Typically 8Å-12Å
 - Long-range potential may be computed separately
 - Number of atoms within cutoff distance is roughly constant (uniform atom density)
 - 200 to 700 atoms within 8Å-12Å cutoff sphere for typical biomolecular structures

Implementation Challenge

- For each tile of grid points, we need to identify the set of atoms that need to be examined
 - One could naively examine all atoms and only use the ones whose distance is within the given range
 - But this examination still takes time, and brings the time complexity right back to
 - number of atoms × number of grid points
 - Each thread needs to avoid examining the atoms outside the range of its grid point(s)

Binning

- A process that groups data to form a chunk called *bin*
- Helps problem solving due to data coarsening
- Uniform bin arrays, Variable bins, KD Trees, ...

Binning for Cut-Off Potential

- Divide the simulation volume with nonoverlapping uniform cubes
- Every atom in the simulation volume falls into a cube based on its spatial location

Bins represent location property of atoms

 After binning, each cube has a unique index in the simulation space for easy parallel access

Spatial Sorting Using Binning

- Presort atoms into *bins* by location in space
- Each bin holds several atoms
- Cutoff potential only uses bins within r_c
 - Yields a linear complexity cutoff potential algorithm

Bin Size Considerations

- Capacity of atom bins needs to be balanced
 - Too large many dummy atoms in bins
 - Too small some atoms will not fit into bins
 - Target bin capacity to cover more than 95% or atoms
- CPU places all atoms that do not fit into bins into an overflow bin
 - Use a CPU sequential algorithm to calculate their contributions to the energy grid lattice points.
 - CPU and GPU can do potential calculations in parallel

Bin Design

- Uniform sized/capacity bins allow array implementation
 - And the relative offset list approach
- Bin capacity should be big enough to contain all the atoms that fall into a bin
 - Cut-off will screen away atoms that weren't processed
 - Performance penalty if too many are screened away

Going from DCS Kernel to Large Bin Cut-off Kernel

- Adaptation of techniques from the direct Coulomb summation kernel for a cutoff kernel
- Atoms are stored in constant memory as with DCS kernel
- CPU loops over potential map regions that are (24Å)³ in volume (cube containing cutoff sphere)
- Large bins of atoms are appended to the constant memory atom buffer until it is full, then GPU kernel is launched
- Host loops over map regions reloading constant memory and launching GPU kernels until completion

Large Bin Design Concept

- Map regions are (24Å)³ in volume
- Regions are sized large enough to provide the GPU enough work in a single kernel launch
 - (48 lattice points)³ for lattice with 0.5Å spacing
 - Small bins don't provide the GPU enough work to utilize all SMs, to amortize constant memory update time, or kernel launch overhead

Large-bin Cutoff Kernel Evaluation

- 6× speedup relative to fast CPU version
- Work-inefficient
 - Coarse spatial hashing into (24Å)³ bins
 - Only 6.5% of the atoms a thread tests are within the cutoff distance
- Better adaptation of the algorithm to the GPU will gain another 2.5×

Improving Work Efficiency

- Thread block examines atom bins up to the cutoff distance
 - Use a sphere of bins
 - All threads in a block scan the same bins and atoms
 - No hardware penalty for multiple simultaneous reads of the same address
 - Simplifies fetching of data
 - The sphere has to be big enough to cover all grid point at corners
 - There will be a small level of divergence
 - Not all grid points processed by a thread block relate to all atoms in a bin the same way
 - (A within cut-off distance of N but outside cut-off of M)

The Neighborhood is a volume

- Calculating and specifying all bin indexes of the sphere can be quite complex
 - Rough approximations reduce efficiency

Neighborhood Offset List (Pre-calculated)

- A list of relative offsets enumerating the bins that are located within the cutoff distance for a given location in the simulation volume
- Detection of surrounding atoms becomes realistic for output grid points
 - By visiting bins in the neighborhood offset list and iterating over the atoms they contain

Performance

- O(MN') where M and N' are the number of output grid points and atoms in the neighborhood offset list, respectively
 - In general, N' is small compared to the number of all atoms
- Works well if the distribution of atoms is uniform

Details on Small Bin Design

- For 0.5Å lattice spacing, a (4Å)³ cube of the potential map is computed by each thread block
 - 8×8×8 potential map points
 - 128 threads per block (4 points/thread)
 - 34% of examined atoms are within cutoff distance

More Design Considerations for the Cutoff Kernel

- High memory throughput to atom data essential
 - Group threads together for locality
 - Fetch bins of data into shared memory
 - Structure atom data to allow fetching
- After taking care of memory demand, optimize to reduce instruction count

Loop and instruction-level optimization

Tiling Atom Data

- Shared memory used to reduce Global Memory bandwidth consumption
 - Threads in a thread block collectively load one bin at a time into shared memory
 - Once loaded, threads scan atoms in shared memory
 - Reuse: Loaded bins used 128 times

Execution cycle of a thread block

Handling Overfull Bins

- In typical use, 2.6% of atoms exceed bin capacity
- Spatial sorting puts these into a list of extra atoms
- Extra atoms processed by the CPU
 - Computed with CPU-optimized algorithm
 - Takes about 66% as long as GPU computation
 - Overlapping GPU and CPU computation yields additional speedup
 - CPU performs final integration of grid data

CPU Grid Data Integration

- Effect of overflow atoms are added to the CPU master energygrid array
- Slice of grid point values calculated by GPU are added into the master energygrid array while removing the padded elements

GPU Thread Coarsening

- Each thread computes potentials at four potential map points
 - Reuse x and z components of distance calculation
 - Check x and z components against cutoff distance (cylinder test)
- Exit inner loop early upon encountering the first empty slot in a bin

GPU Thread Inner Loop

Exit when an empty atom bin entry is encountered

```
for (i = 0; i < BIN_DEPTH; i++) {
  aq = AtomBinCache[i].w;
  if (aq == 0) break;
  dx = AtomBinCache[i].x - x;
  dz = AtomBinCache[i].z - z;</pre>
```

Cylinder test

```
dxdz2 = dx*dx + dz*dz;
if (dxdz2 > cutoff2) continue;
```

Cutoff test and potential value calculation

```
dy = AtomBinCache[i].y - y;
r2 = dy*dy + dxdz2;
if (r2 < cutoff2)
    poten0 += aq * rsqrtf(r2);
    // Simplified example
dy = dy - 2 * grid_spacing;
/* Repeat three more times */
}
```

Cutoff Summation Runtime

Summary

- Large bins allow re-use of all-input kernels with little code change
 - But work efficiency can be very low
- Use of small-sized bins require more sophisticated kernel code to traverse list of small bins
 - Much higher work efficiency
 - Small bins also serve as tiles for locality
- CPU processes overflow atoms from fixed capacity bins