

# CS 558: Computer Vision

## 11<sup>th</sup> Set of Notes

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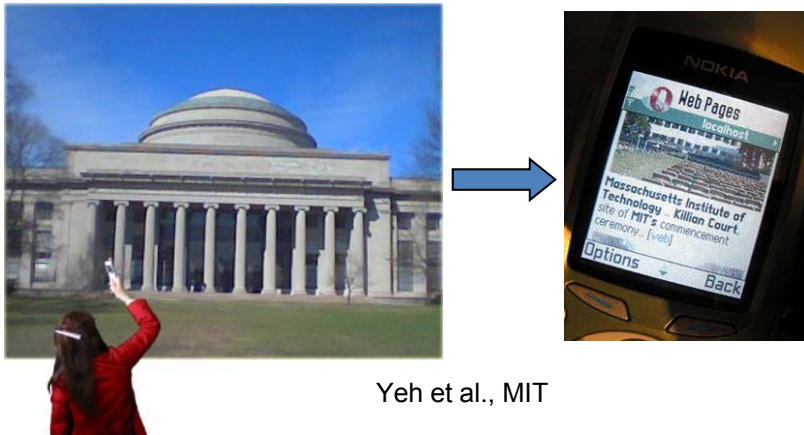
# Overview

- Object detection and recognition
  - Supervised Classification
  - Boosting and face detection
  - Pedestrian detection (HOG)
  - Part-based models
- Based on slides by K. Grauman, D. Hoiem and S. Lazebnik

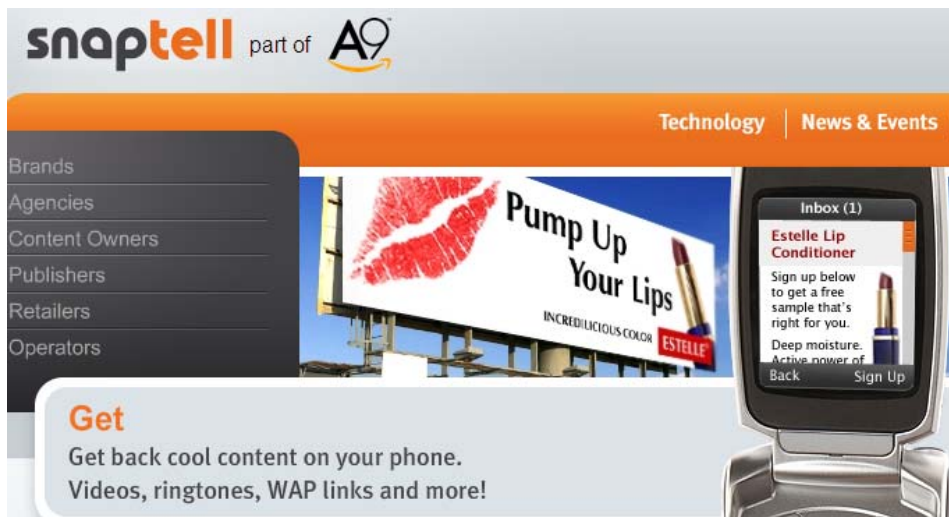
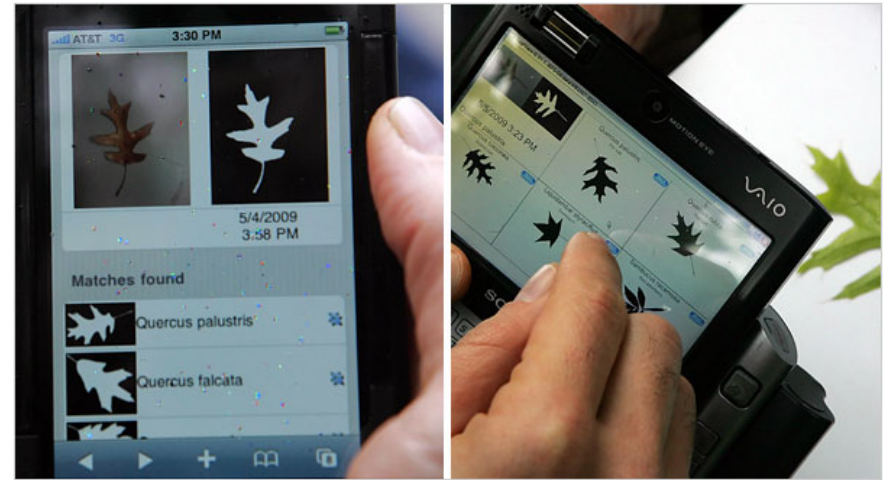
# Why recognition?

- Recognition a fundamental part of perception
  - e.g., robots, autonomous agents
- Organize and give access to visual content
  - Connect to information
  - Detect trends and themes

# Posing visual queries



## Digital Field Guides Eliminate the Guesswork




# Autonomous agents able to detect objects



<http://www.darpa.mil/grandchallenge/gallery.asp>







# Finding visually similar objects





 **like** visual shopping *alpha*



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**Natural Comfort - LV58**  
a sexy classic pump with a pillow-like footbed to keep your feet happy. leather or patent leather upper. wrapped memory-foam footbed. covered heel. leather sole.  
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**rsvp - Caitlyn**  
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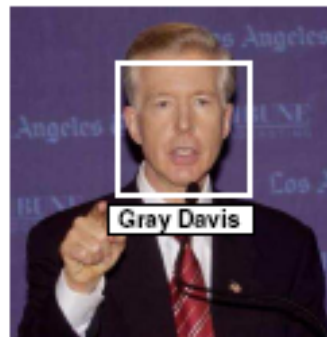
# Auto-annotation



President George W. Bush makes a statement in the Rose Garden while Secretary of Defense Donald Rumsfeld looks on, July 23, 2003. Rumsfeld said the United States would release graphic photographs of the dead sons of Saddam Hussein to prove they were killed by American troops. Photo by Larry Downing/Reuters



British director Sam Mendes and his partner actress Kate Winslet arrive at the London premiere of 'The Road to Perdition', September 18, 2002. The film stars Tom Hanks as a Chicago hit man who has a separate family life and co-stars Paul Newman and Jude Law. REUTERS/Dan Chung



Incumbent California Gov. Gray Davis (news - web sites) leads Republican challenger Bill Simon by 10 percentage points - although 17 percent of voters are still undecided, according to a poll released October 22, 2002 by the Public Policy Institute of California. Davis is shown speaking to reporters after his debate with Simon in Los Angeles, on Oct. 7. (Jim Ruymen/Reuters)

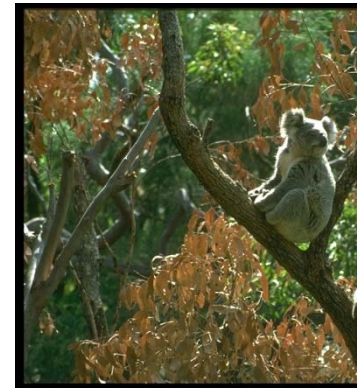
# Challenges: robustness



Illumination



Object pose



Clutter



Occlusions



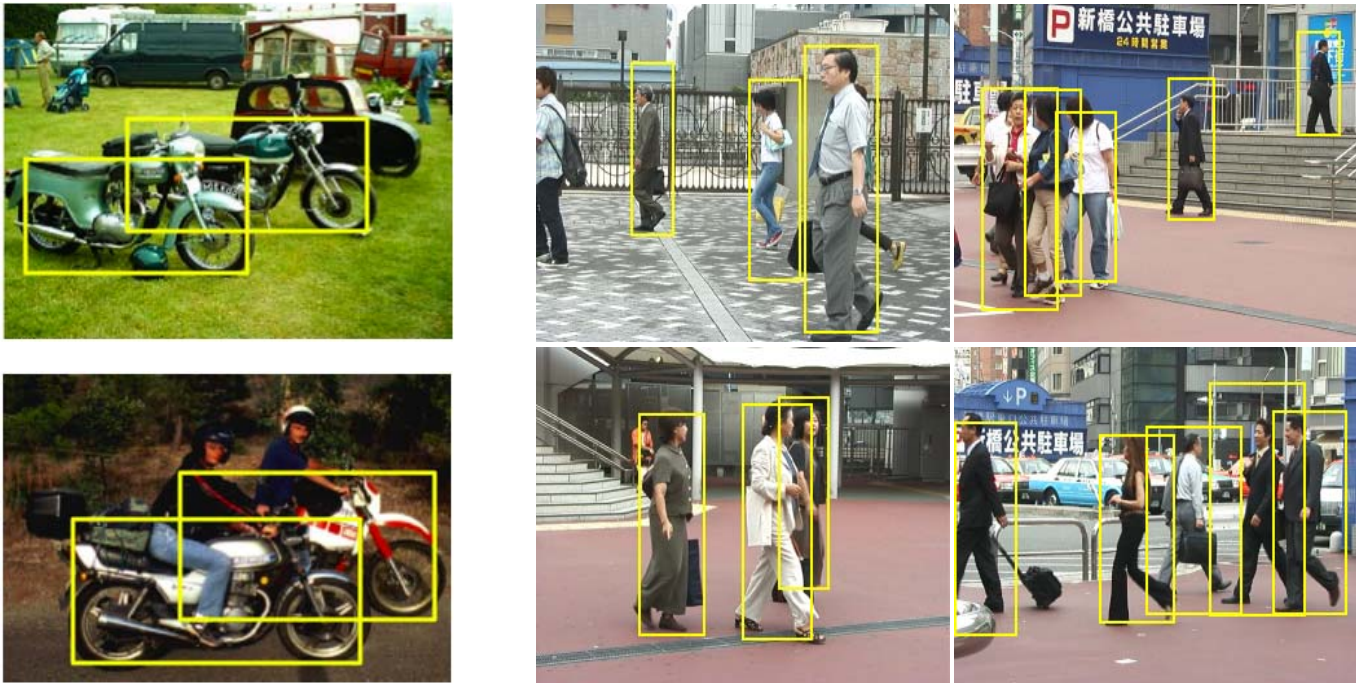
Intra-class  
appearance



Viewpoint

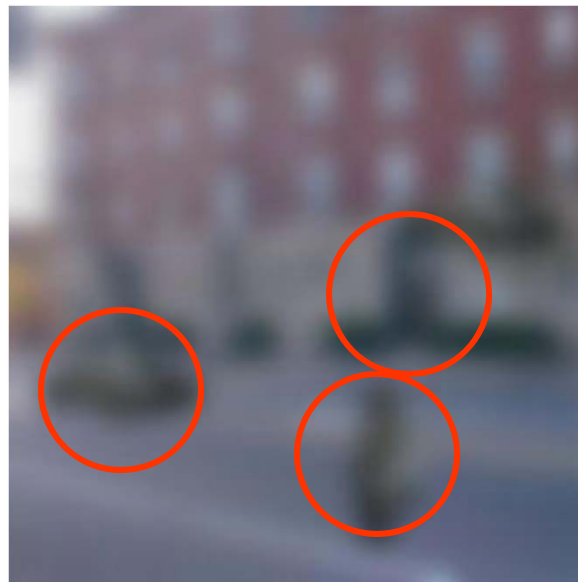
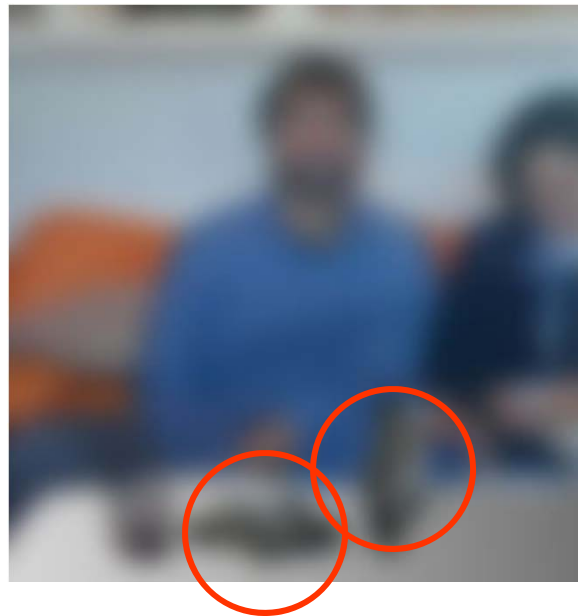


# Challenges: robustness



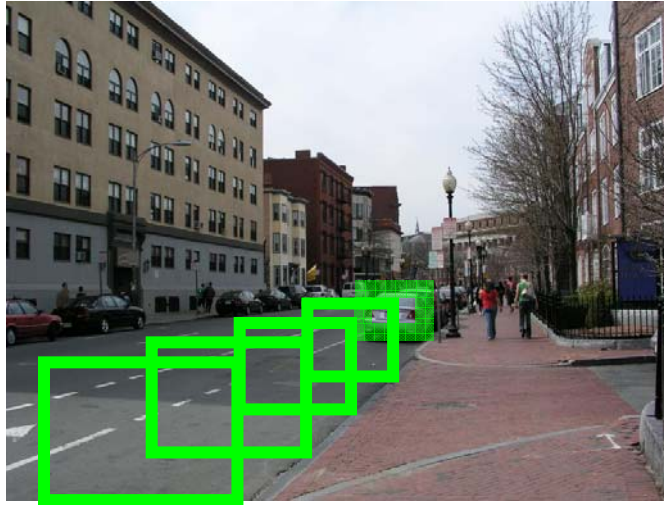
Realistic scenes are crowded, cluttered,  
have overlapping objects

# Challenges: importance of context



slide credit: Fei-Fei, Fergus & Torralba

# Challenges: importance of context

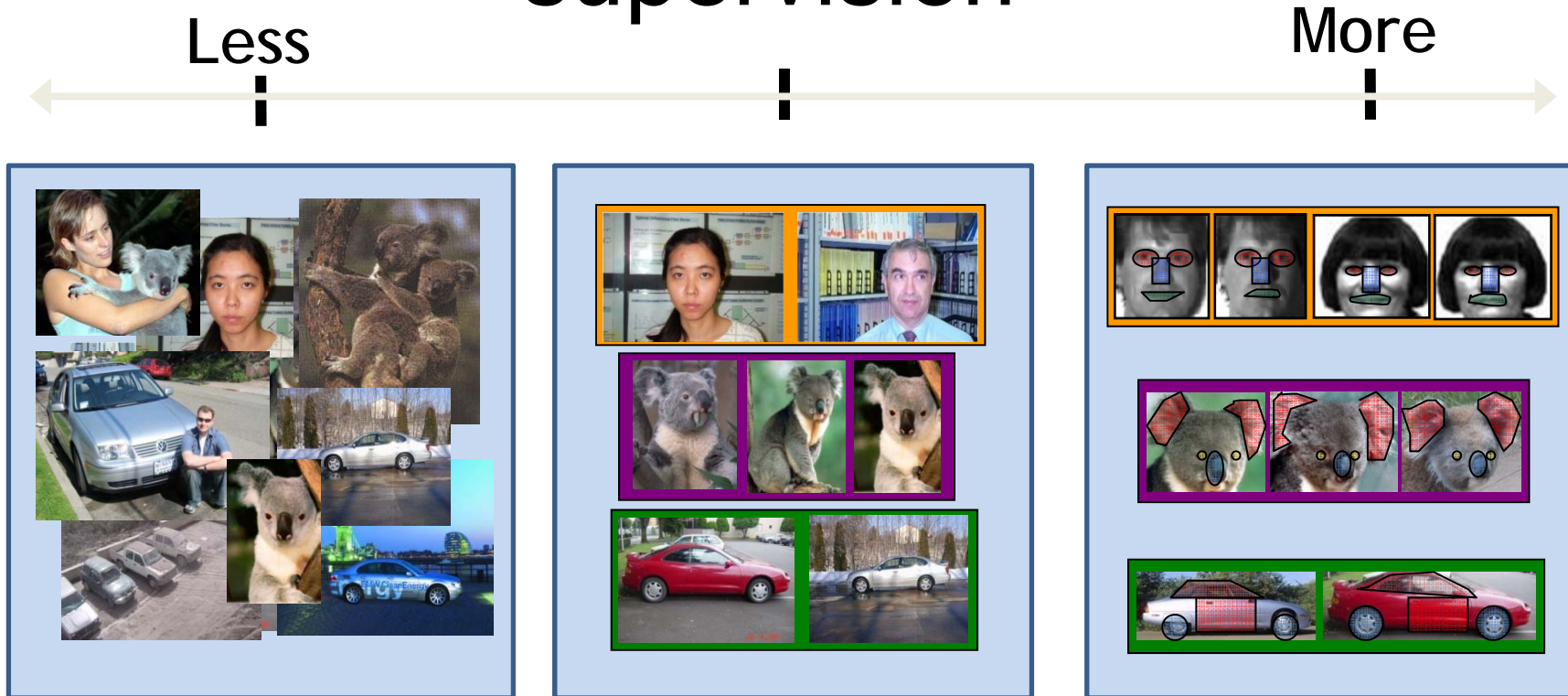


# Challenges: complexity

- Thousands to millions of pixels in an image
- 3,000-30,000 human recognizable object categories
- 30+ degrees of freedom in the pose of articulated objects (humans)
- Billions of images indexed by Google Image Search
- About half of the cerebral cortex in primates is devoted to processing visual information [Felleman and van Essen 1991]



# Challenges: learning with minimal supervision



Unlabeled,  
multiple objects

Classes labeled, some  
clutter

Cropped to object,  
parts and classes  
labeled

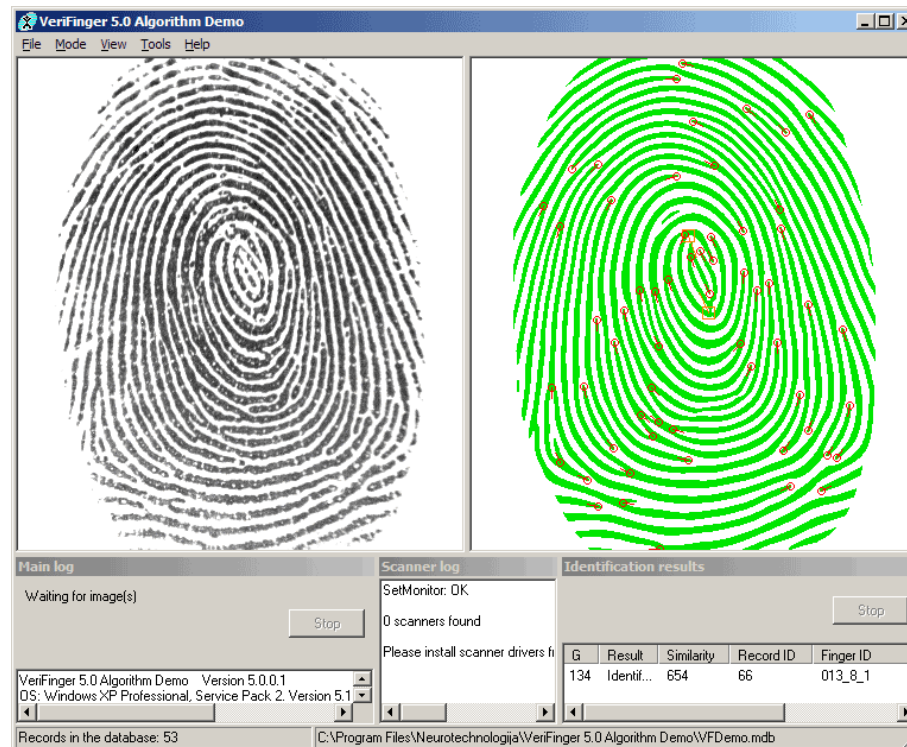
# What works most reliably today

- Reading license plates, zip codes, checks

3 6 8 1 7 9 6 6 9 1  
6 7 5 7 8 6 3 4 8 5  
2 1 7 9 7 1 2 8 4 5  
4 8 1 9 0 1 8 8 9 4  
7 6 1 8 6 4 1 5 6 0  
7 5 9 2 6 5 8 1 9 7  
2 2 2 2 2 3 4 4 8 0  
0 2 3 8 0 7 3 8 5 7  
0 1 4 6 4 6 0 2 4 3  
7 1 2 8 7 6 9 8 6 1

# What works most reliably today

- Reading license plates, zip codes, checks
- Fingerprint recognition



Source: Lana Lazebnik

# What works most reliably today

- Reading license plates, zip codes, checks
- Fingerprint recognition
- Face detection



[Face priority AE] When a bright part of the face is too bright



# What works most reliably today

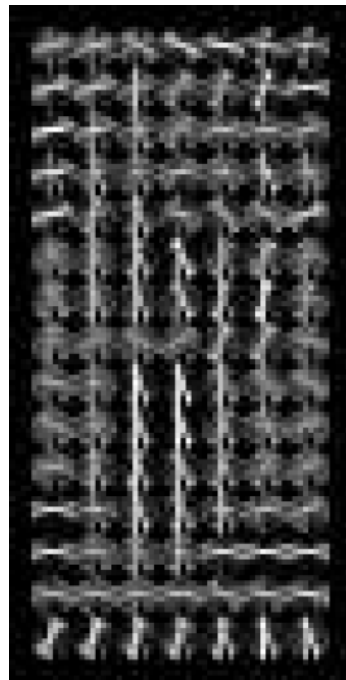
- Reading license plates, zip codes, checks
- Fingerprint recognition
- Face detection
- Recognition of flat textured objects (CD covers, book covers, etc.)



# Generic category recognition: basic framework

- Build/train object model
  - Choose a representation
  - Learn or fit parameters of model / classifier
- Generate candidates in new image
- Score the candidates

# Generic category recognition: representation choice



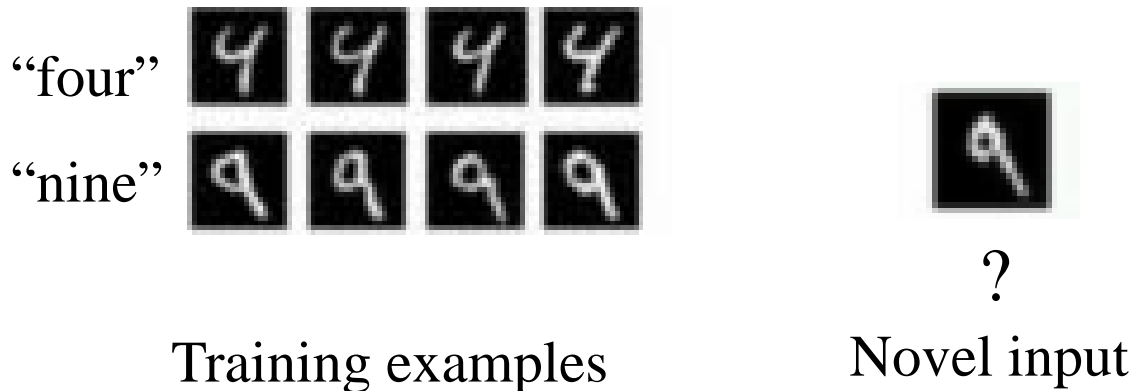
Window-based



Part-based

# Supervised classification

- Given a collection of *labeled* examples, come up with a function that will predict the labels of new examples.



- How good is some function we come up with to do the classification?
- Depends on
  - Mistakes made
  - Cost associated with the mistakes



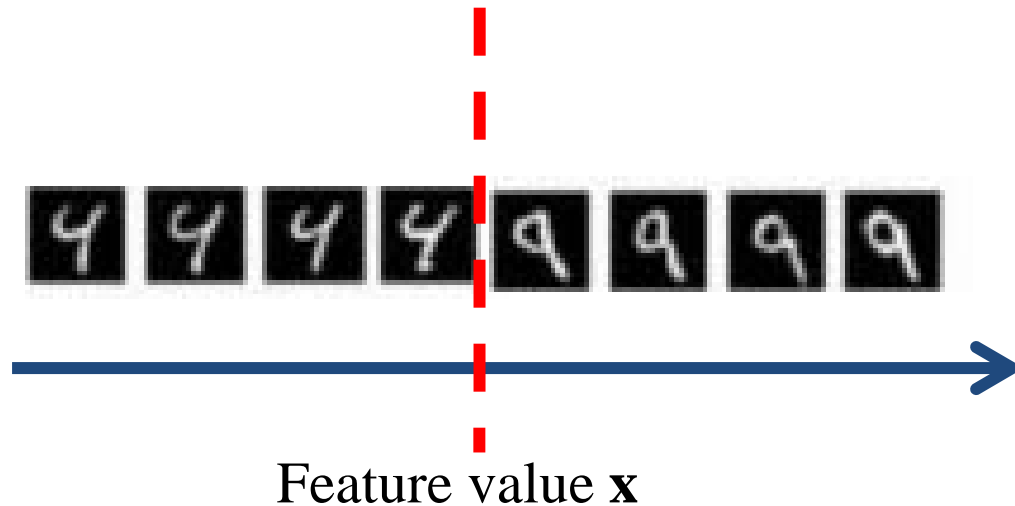
# Supervised classification

- Given a collection of *labeled* examples, come up with a function that will predict the labels of new examples.
- Consider the two-class (binary) decision problem
  - $L(4 \rightarrow 9)$ : Loss of classifying a 4 as a 9
  - $L(9 \rightarrow 4)$ : Loss of classifying a 9 as a 4
- Risk of a classifier  $s$  is expected loss:

$$R(s) = \Pr(4 \rightarrow 9 \mid \text{using } s)L(4 \rightarrow 9) + \Pr(9 \rightarrow 4 \mid \text{using } s)L(9 \rightarrow 4)$$

- We want to choose a classifier so as to minimize this total risk

# Supervised classification



Optimal classifier will minimize total risk.

At decision boundary, either choice of label yields same expected loss.

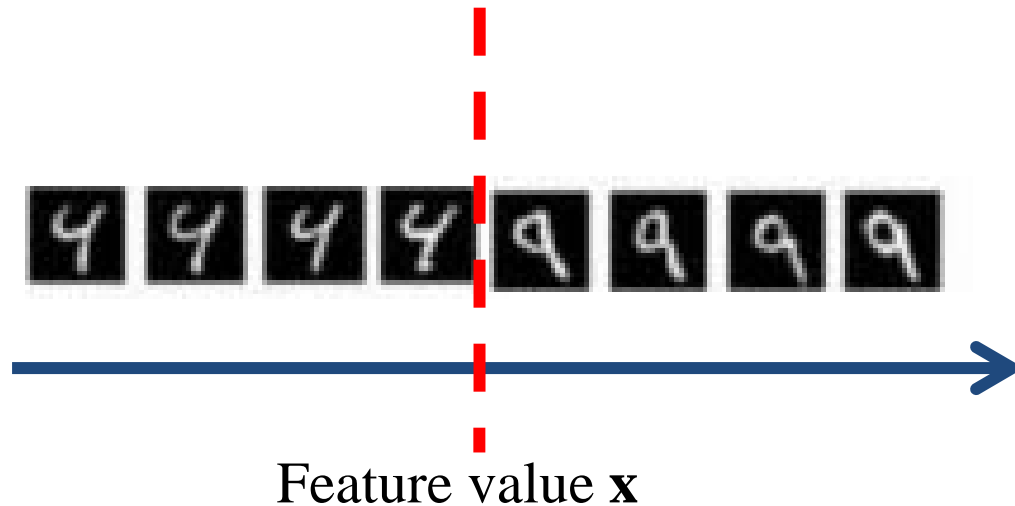
If we choose class “four” at boundary, expected loss is:

$$= P(\text{class is } 9 \mid \mathbf{x}) L(9 \rightarrow 4) + P(\text{class is } 4 \mid \mathbf{x}) L(4 \rightarrow 4)$$

If we choose class “nine” at boundary, expected loss is:

$$= P(\text{class is } 4 \mid \mathbf{x}) L(4 \rightarrow 9)$$

# Supervised classification



Optimal classifier will minimize total risk.

At decision boundary, either choice of label yields same expected loss.

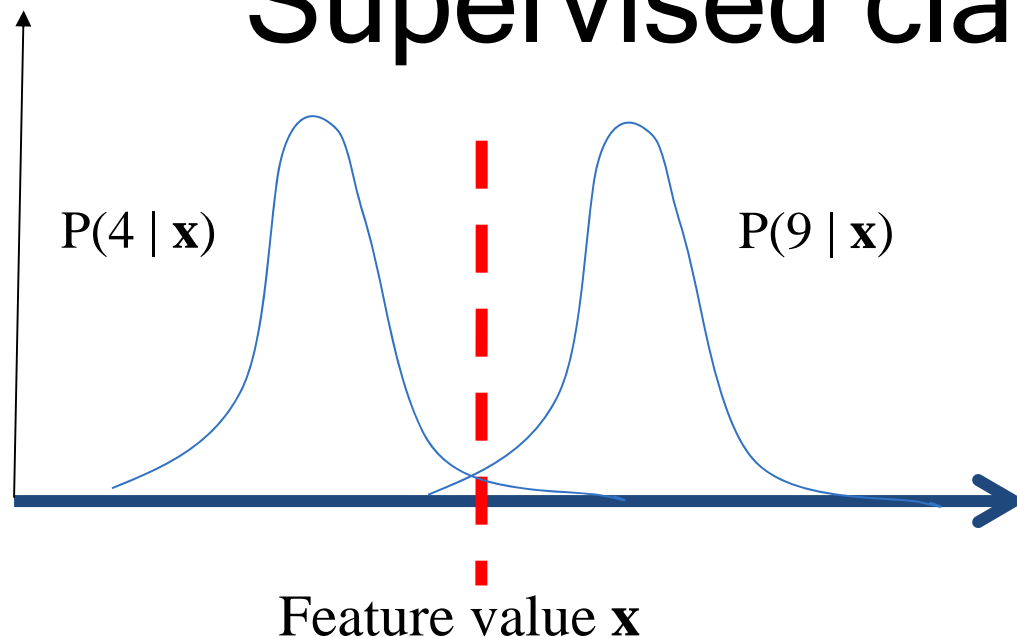
So, best decision boundary is at point  $\mathbf{x}$  where

$$P(\text{class is } 9 \mid \mathbf{x}) L(9 \rightarrow 4) = P(\text{class is } 4 \mid \mathbf{x}) L(4 \rightarrow 9)$$

To classify a new point, choose class with lowest expected loss; i.e., choose “four” if

$$P(4 \mid \mathbf{x}) L(4 \rightarrow 9) > P(9 \mid \mathbf{x}) L(9 \rightarrow 4)$$

# Supervised classification



Optimal classifier will minimize total risk.

At decision boundary, either choice of label yields same expected loss.

So, best decision boundary is at point  $\mathbf{x}$  where

$$P(\text{class is } 9 | \mathbf{x}) L(9 \rightarrow 4) = P(\text{class is } 4 | \mathbf{x}) L(4 \rightarrow 9)$$

To classify a new point, choose class with lowest expected loss; i.e., choose “four” if

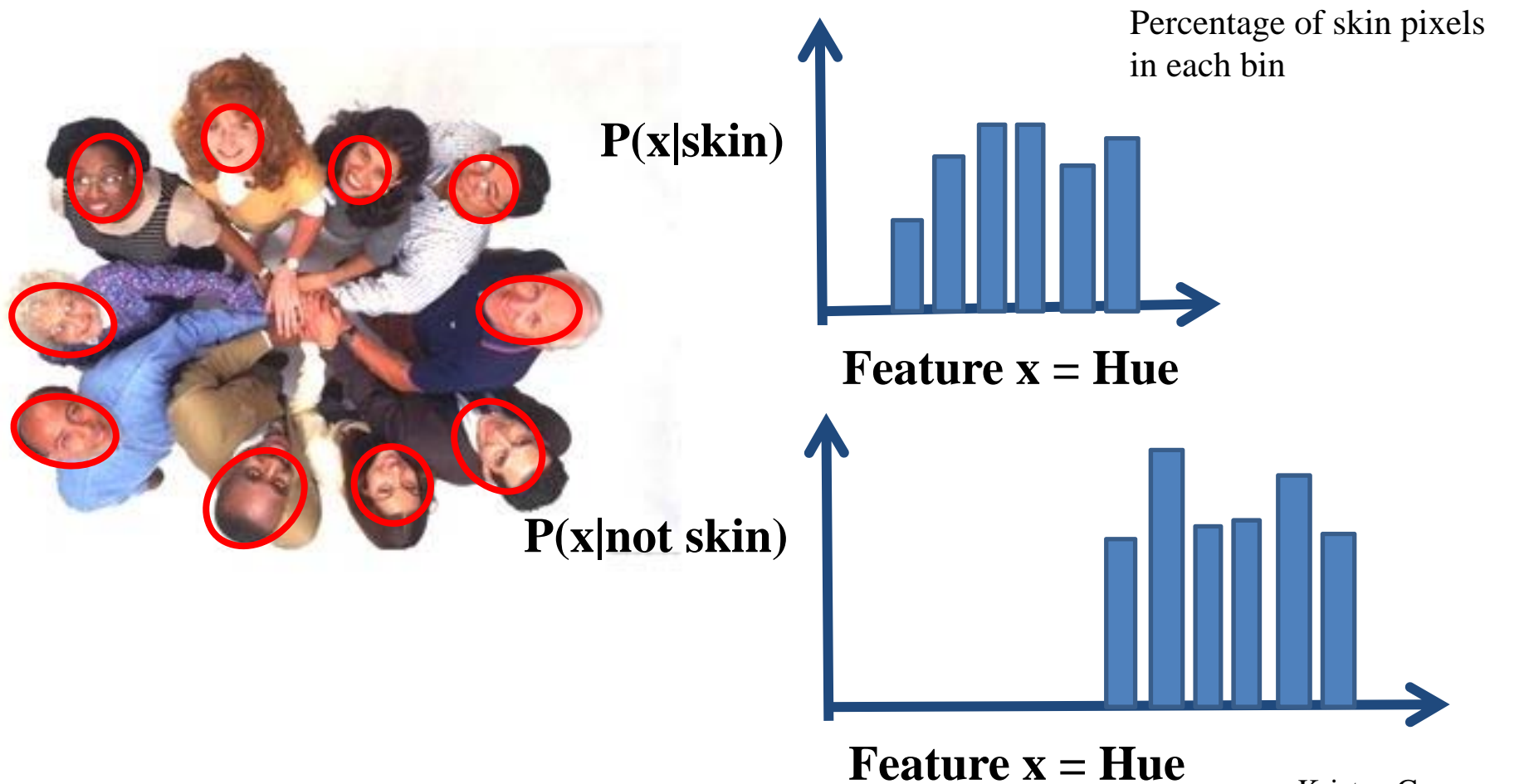
$$P(4 | \mathbf{x}) L(4 \rightarrow 9) > P(9 | \mathbf{x}) L(9 \rightarrow 4)$$

*How to evaluate these probabilities?*



# Example: learning skin colors

- We can represent a class-conditional density using a histogram (a “non-parametric” distribution)



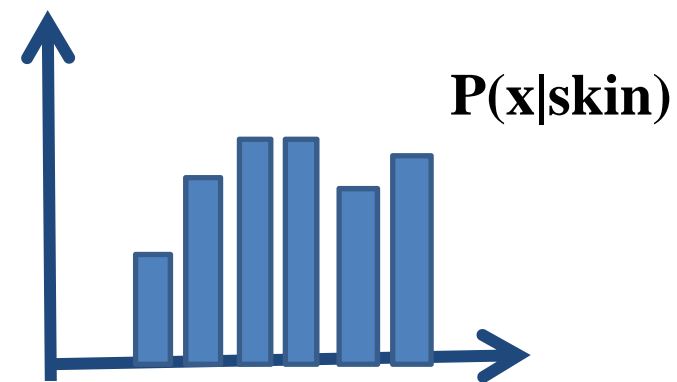
# Example: learning skin colors

- We can represent a class-conditional density using a histogram (a “non-parametric” distribution)

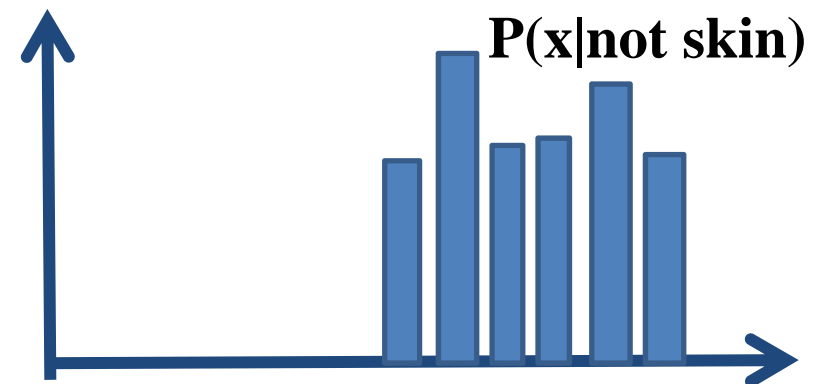


Now we get a new image, and want to label each pixel as skin or non-skin.

*What's the probability we care about to do skin detection?*



Feature x = Hue



Feature x = Hue

# Bayes rule

$$\overbrace{P(\textit{skin} \mid x)}^{\text{posterior}} = \frac{\overbrace{P(x \mid \textit{skin})}^{\text{likelihood}} \overbrace{P(\textit{skin})}^{\text{prior}}}{P(x)}$$

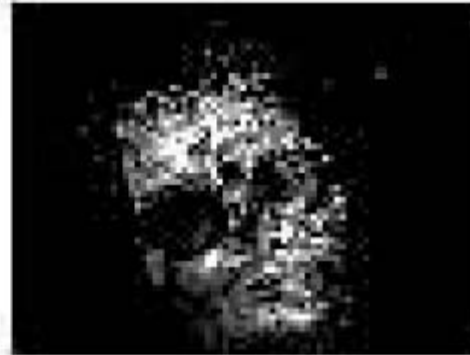
$$P(\textit{skin} \mid x) \propto P(x \mid \textit{skin})P(\textit{skin})$$

*Where does the prior come from?*

*Why use a prior?*

# Example: classifying skin pixels

Now for every pixel in a new image, we can estimate probability that it is generated by skin.

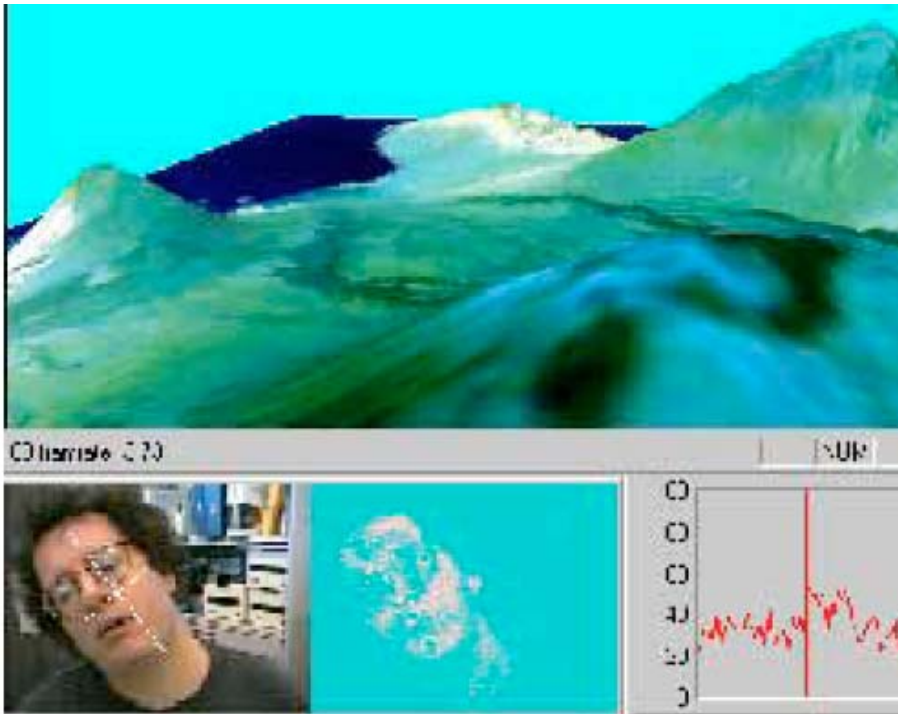


Brighter pixels →  
higher probability  
of being skin

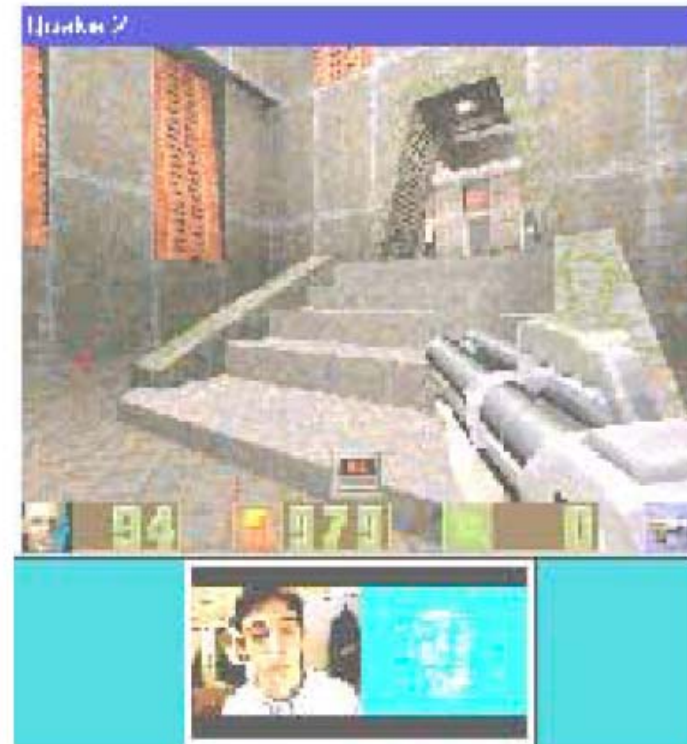
Classify pixels based on these probabilities

- if  $p(\text{skin}|\mathbf{x}) > \theta$ , classify as skin
- if  $p(\text{skin}|\mathbf{x}) < \theta$ , classify as not skin

# Example: classifying skin pixels



**Figure 13:** CAMSHIFT-based face tracker used to interact with a 3D graphic's model of Hawaii



**Figure 12:** CAMSHIFT-based face tracker used to play Quake 2 hands free by inserting control variables into the mouse queue

Using skin color-based face detection and pose estimation as a video-based interface

# Supervised classification

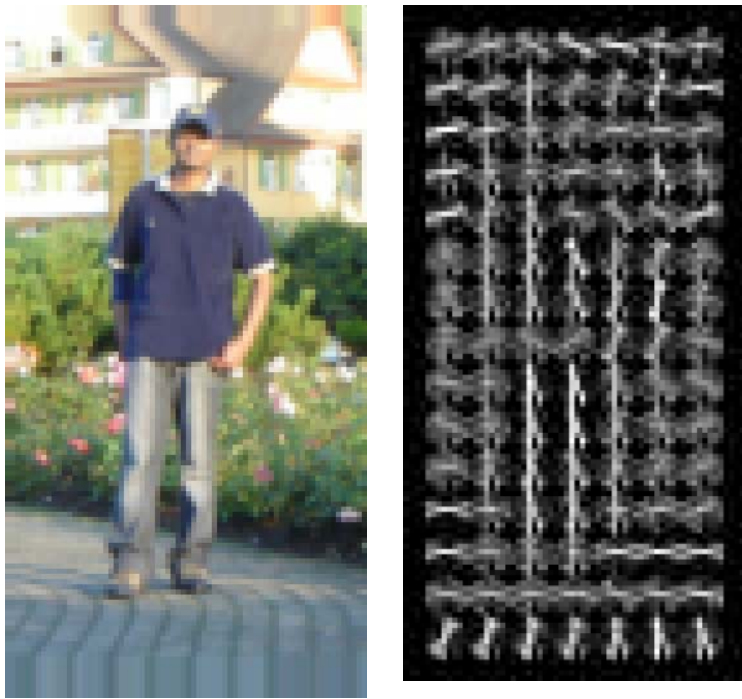
- Want to minimize the expected misclassification
- Two general strategies
  - Use the training data to build representative probability model; separately model class-conditional densities and priors (*generative*)
  - Directly construct a good decision boundary, model the posterior (*discriminative*)



# Generic category recognition: basic framework

- Build/train object model
  - Choose a representation
  - Learn or fit parameters of model / classifier
- Generate candidates in new image
- Score the candidates

# Generic category recognition: representation choice



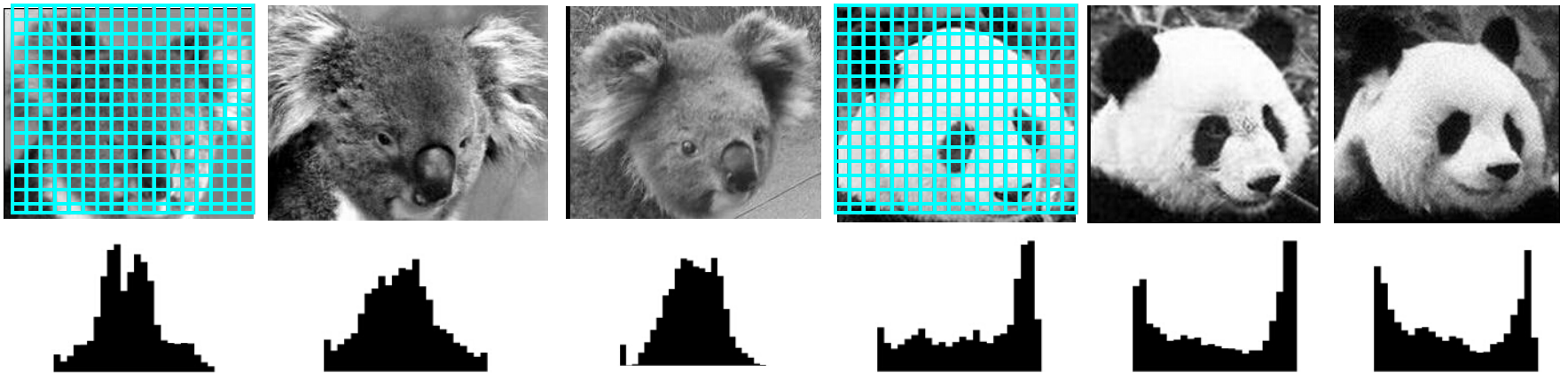
Window-based



Part-based

# Window-based models

## Building an object model



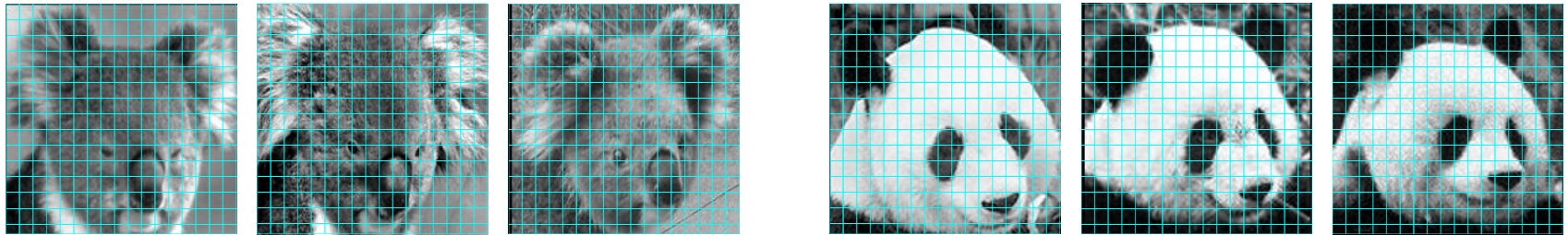
### Simple holistic descriptions of image content

- grayscale / color histogram
- vector of pixel intensities

# Window-based models

## Building an object model

- Pixel-based representations sensitive to small shifts

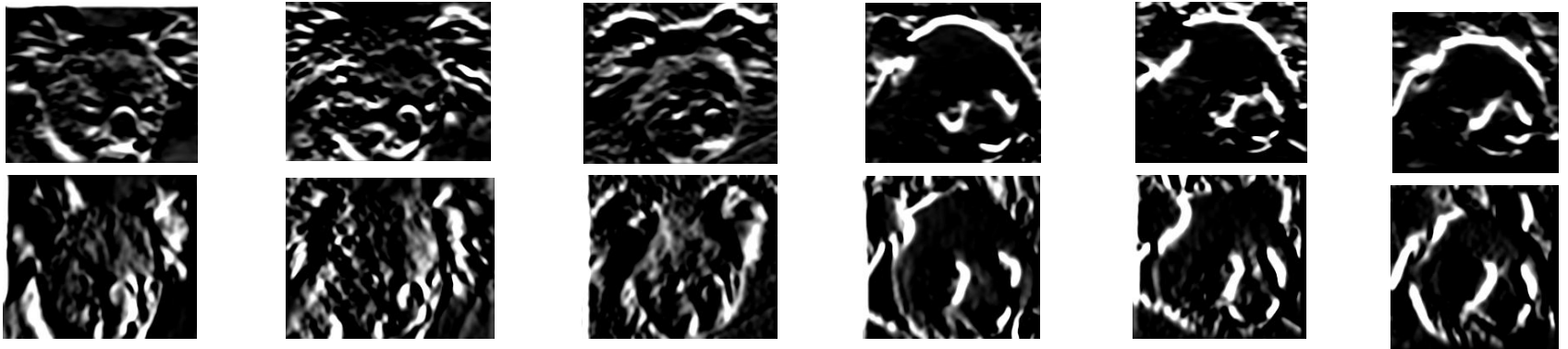


- Color or grayscale-based appearance description can be sensitive to illumination and intra-class appearance variation

# Window-based models

## Building an object model

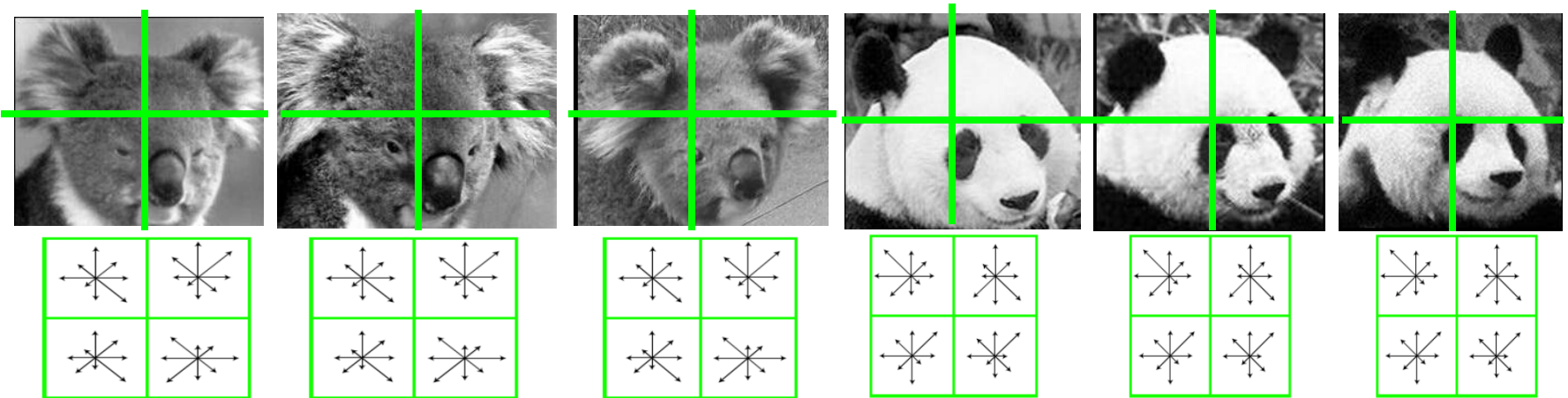
- Consider edges, contours, and (oriented) intensity gradients



# Window-based models

## Building an object model

- Consider edges, contours, and (oriented) intensity gradients



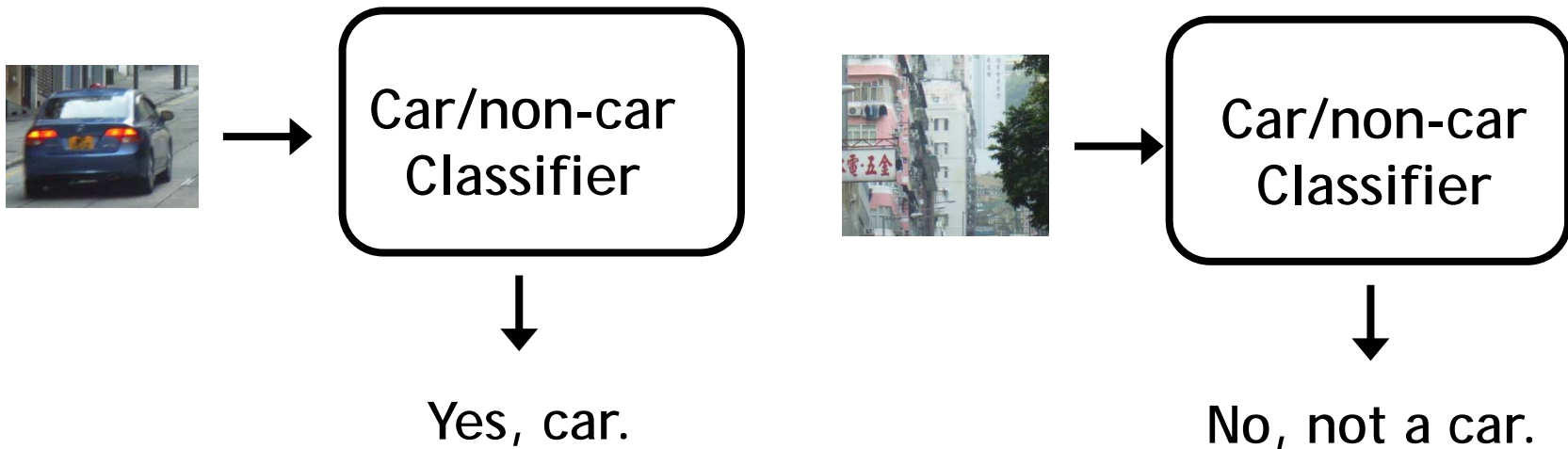
- Summarize local distribution of gradients with histogram
  - Locally orderless: offers invariance to small shifts and rotations
  - Contrast-normalization: try to correct for variable illumination



# Window-based models

## Building an object model

Given the representation, train a binary classifier

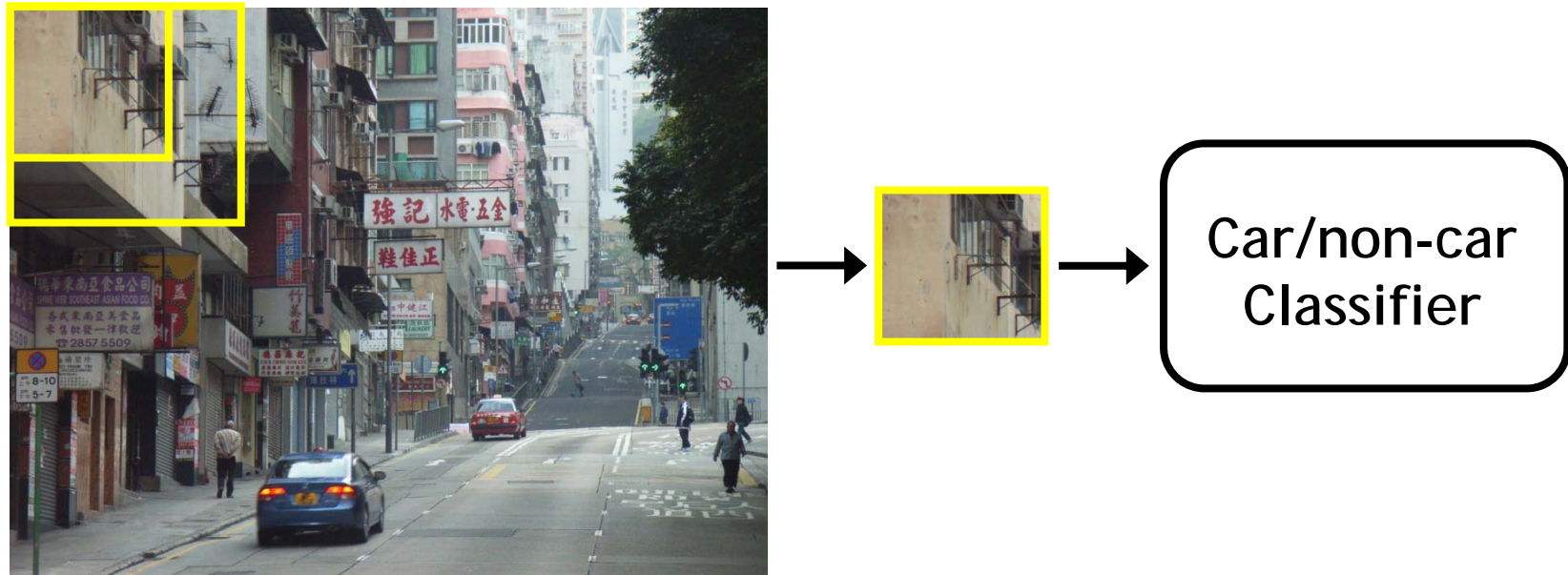


# Generic category recognition: basic framework

- Build/train object model
  - Choose a representation
  - Learn or fit parameters of model / classifier
- **Generate candidates in new image**
- **Score the candidates**

# Window-based models

## Generating and scoring candidates



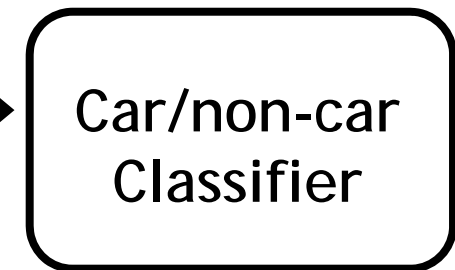
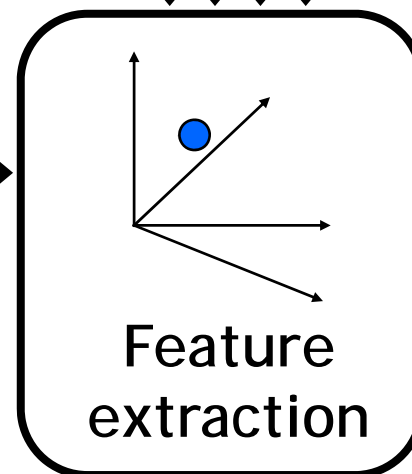
# Window-based object detection: recap

## Training:

1. Obtain training data
2. Define features
3. Define classifier

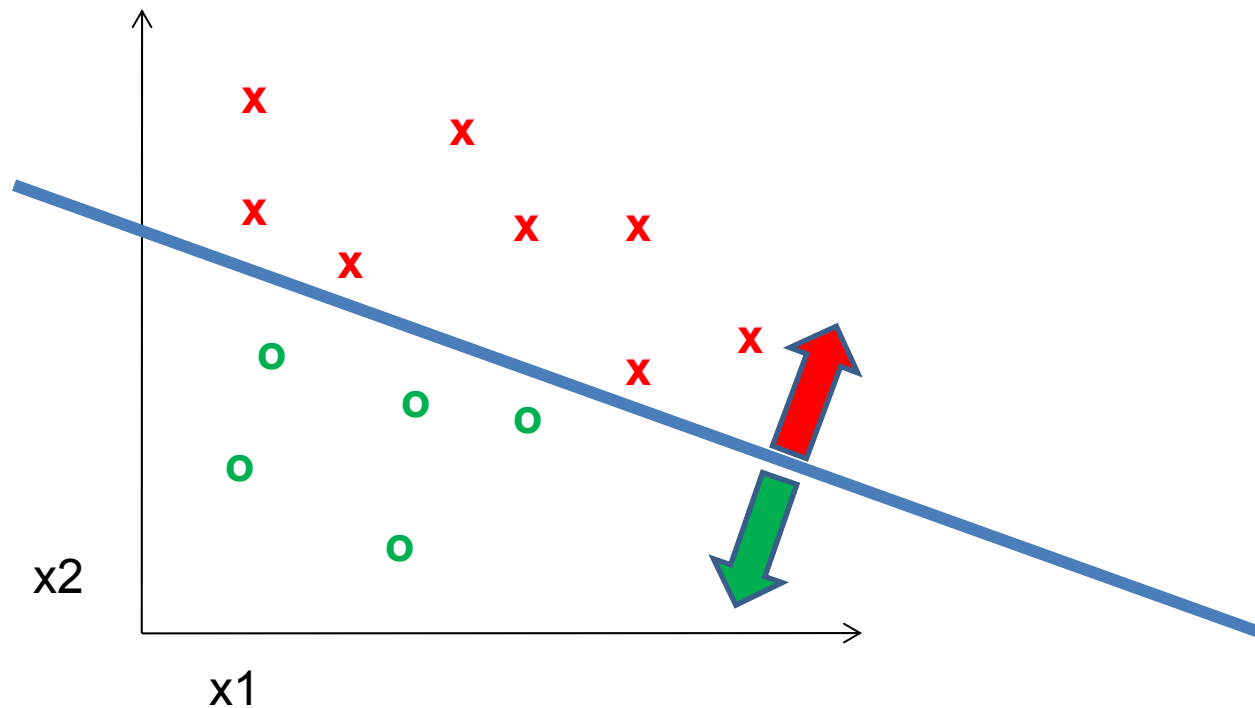
## Given new image:

1. Slide window
2. Score by classifier



# Classifier

A classifier maps from the feature space to a label



# Different types of classification

- Exemplar-based: transfer category labels from examples with most similar features
  - What similarity function? What parameters?
- Linear classifier: confidence in positive label is a weighted sum of features
  - What are the weights?
- Non-linear classifier: predictions based on more complex function of features
  - What form does the classifier take? Parameters?
- Generative classifier: assign to the label that best explains the features (makes features most likely)
  - What is the probability function and its parameters?

Note: You can always fully design the classifier by hand, but usually this is too difficult. Typical solution: learn from training examples.



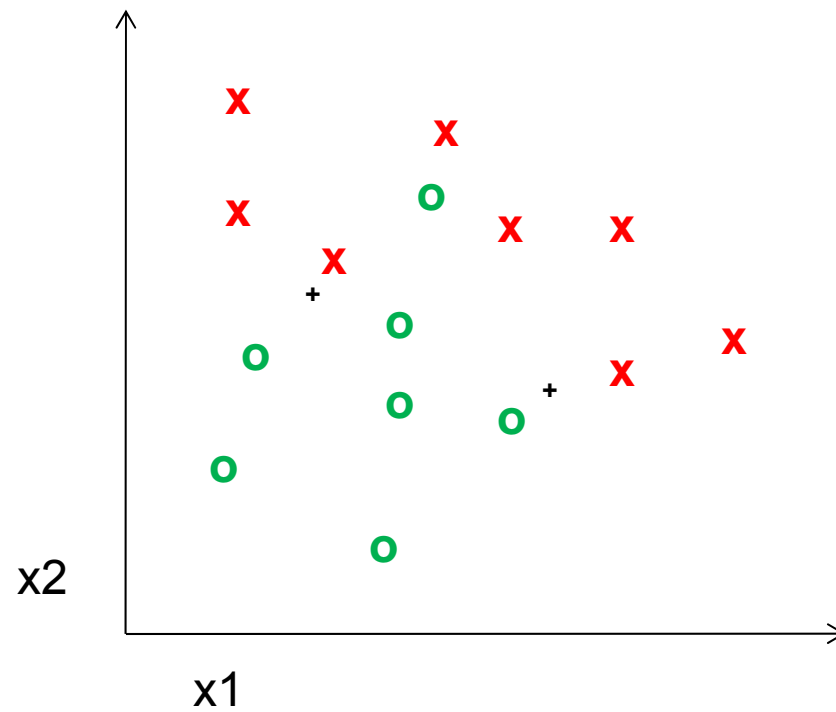
# One way to think about it...

- Training labels dictate that two examples are the same or different, in some sense
- Features and distance measures define visual similarity
- Goal of training is to learn feature weights or distance measures so that visual similarity predicts label similarity
- *We want the simplest function that is confidently correct*

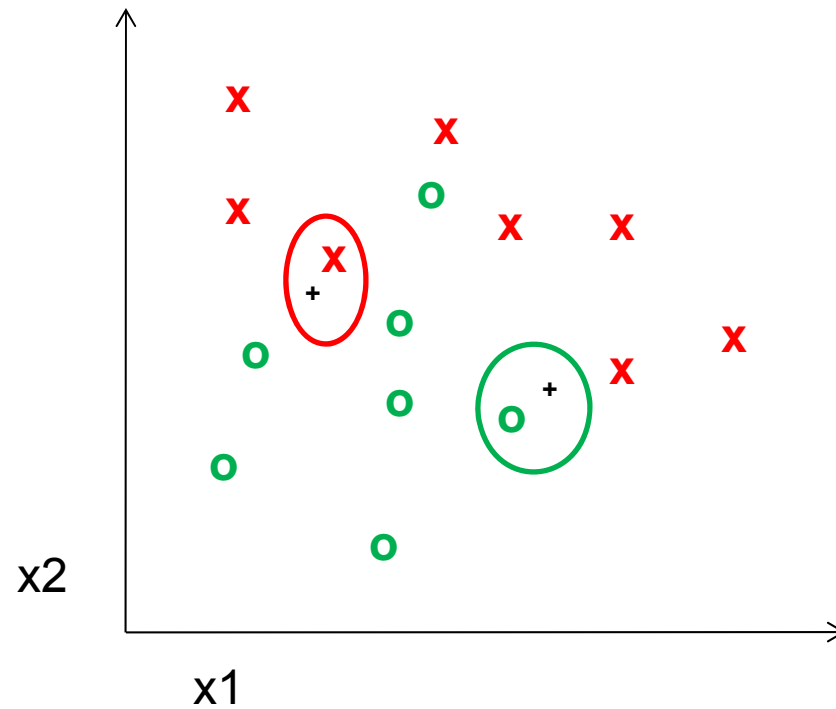
# Exemplar-based Models

- Transfer the label(s) of the most similar training examples

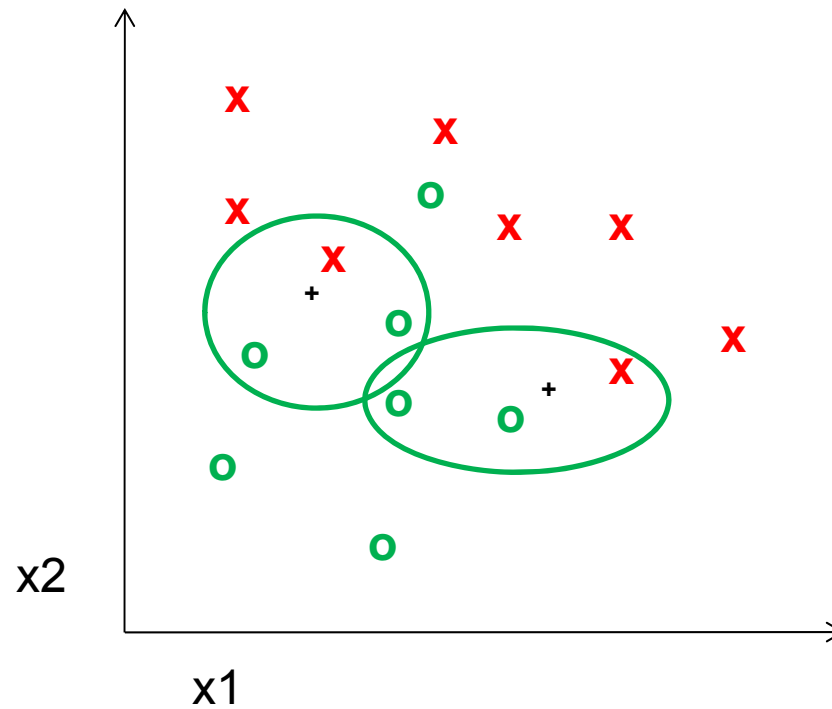
# K-nearest neighbor classifier



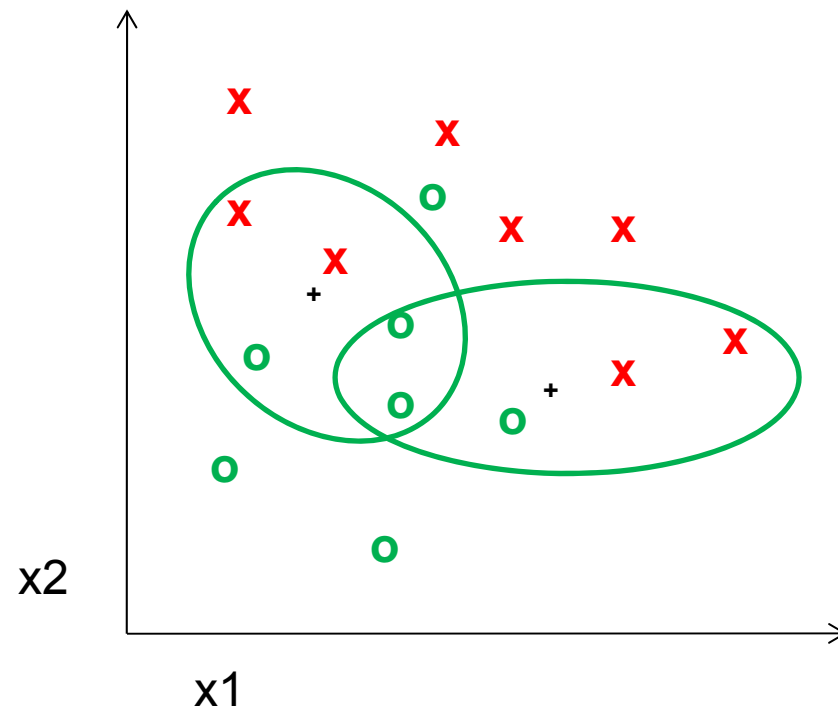
# 1-nearest neighbor



# 3-nearest neighbor



# 5-nearest neighbor



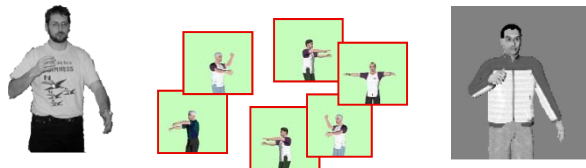


# Using K-NN

- Simple, a good classifier to try first
- No training time (unless you want to learn a distance function)
- With infinite examples, 1-NN provably has error that is at most twice Bayes optimal error

# Discriminative classifier construction

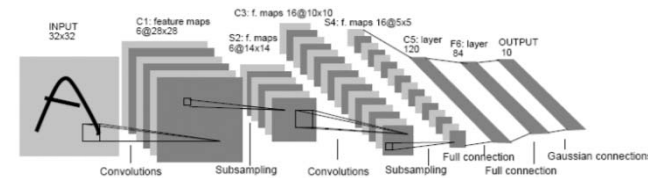
## Nearest neighbor



$10^6$  examples

Shakhnarovich, Viola, Darrell 2003  
Berg, Berg, Malik 2005...

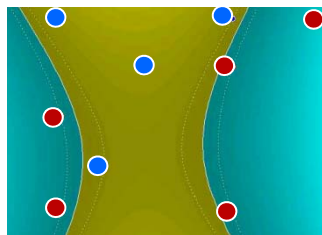
## Neural networks



LeCun, Bottou, Bengio, Haffner 1998  
Rowley, Baluja, Kanade 1998

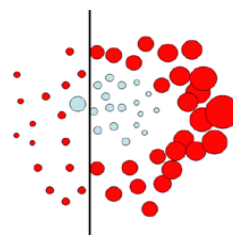
...

## Support Vector Machines



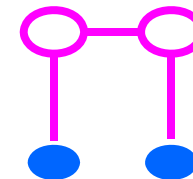
Guyon, Vapnik  
Heisele, Serre, Poggio, 2001,...

## Boosting



Viola, Jones 2001, Torralba et al.  
2004, Opelt et al. 2006,...

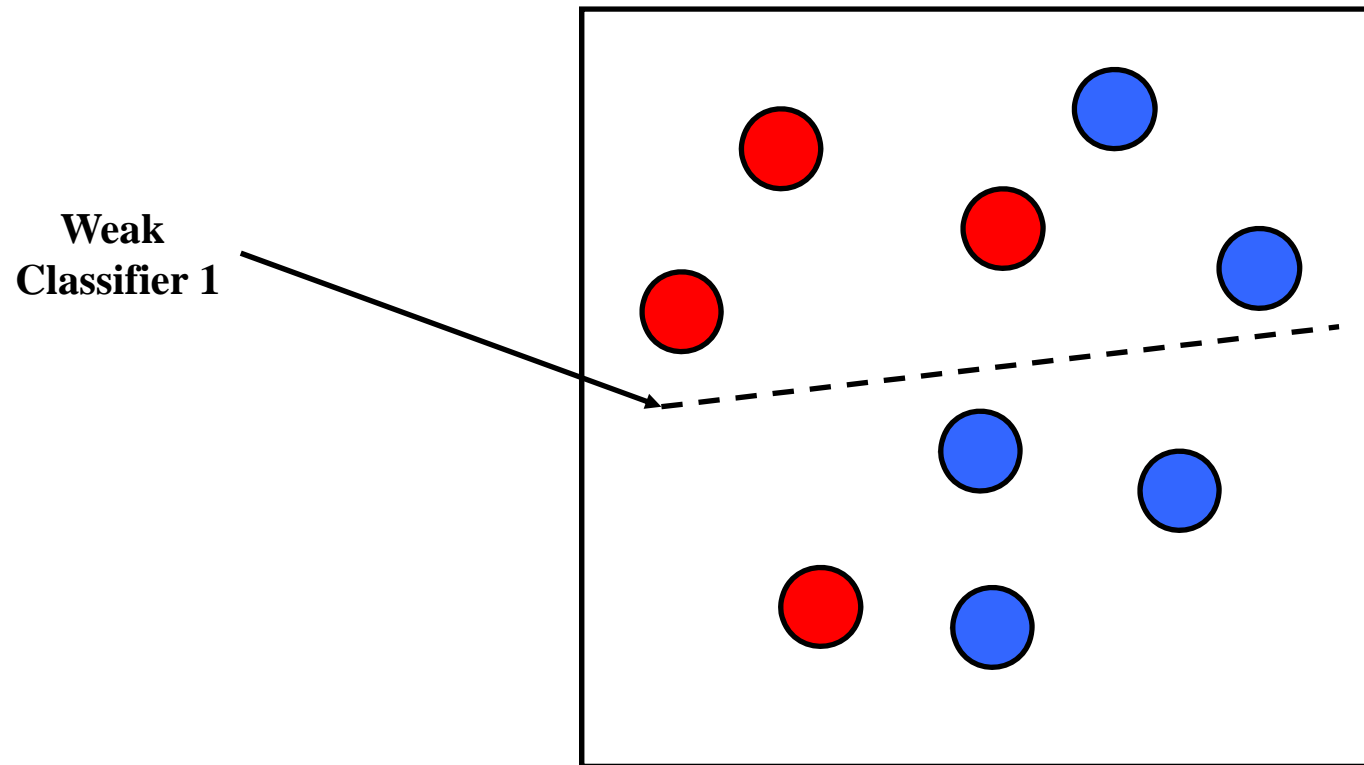
## Conditional Random Fields



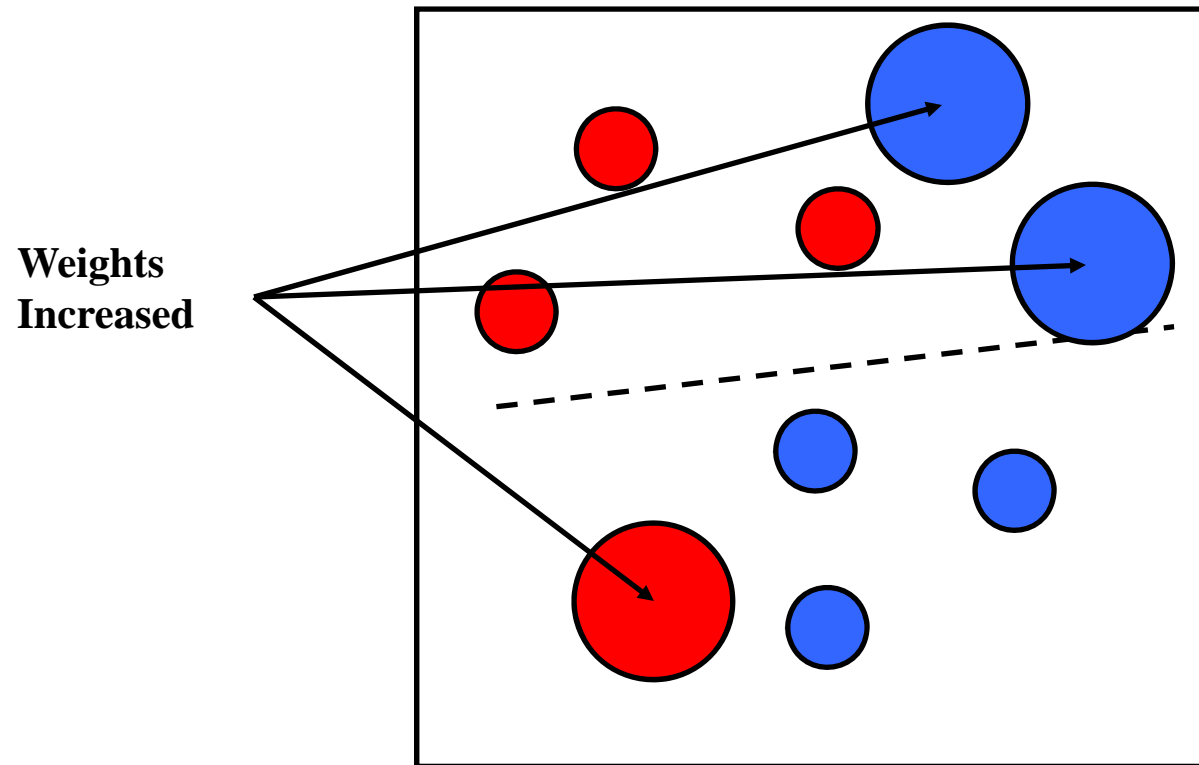
McCallum, Freitag, Pereira 2000; Kumar, Hebert  
2003

...

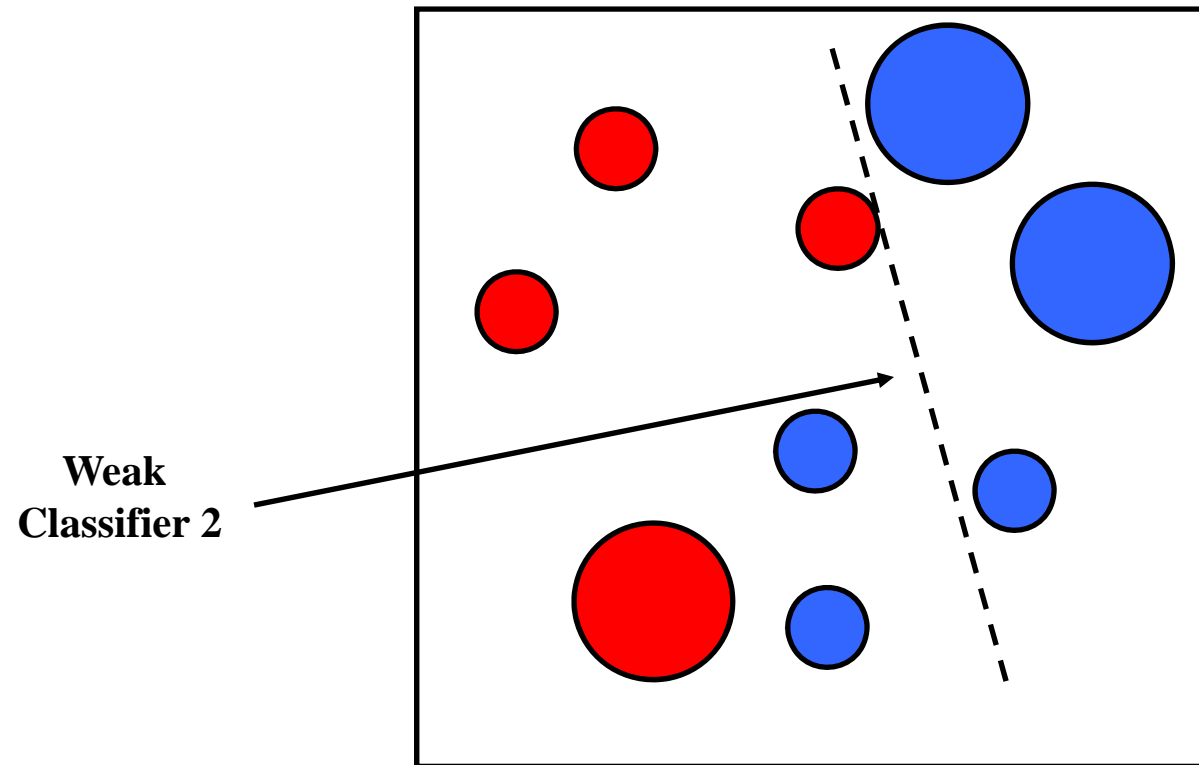
# Boosting intuition



# Boosting illustration

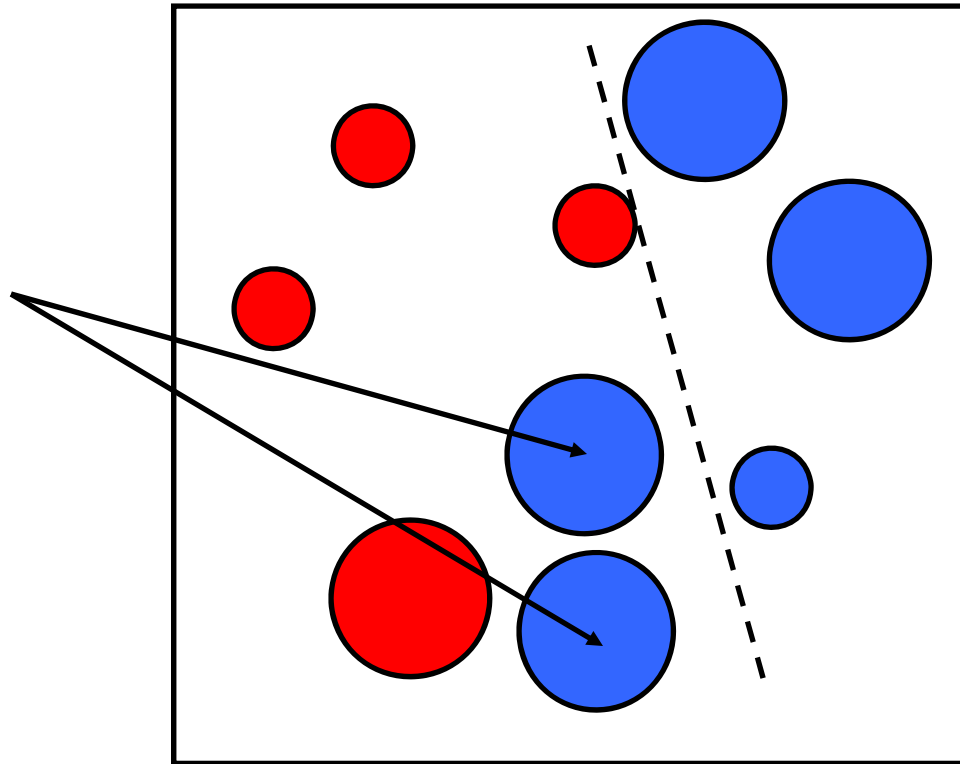


# Boosting illustration

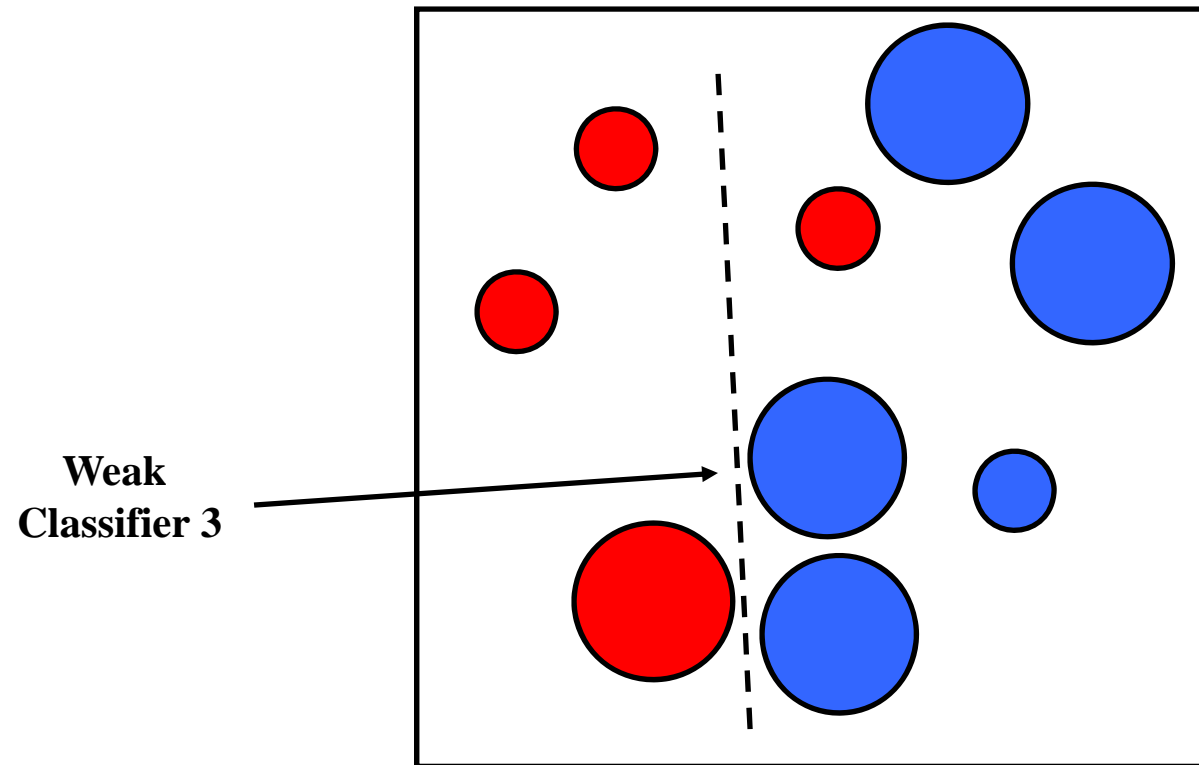


# Boosting illustration

Weights  
Increased

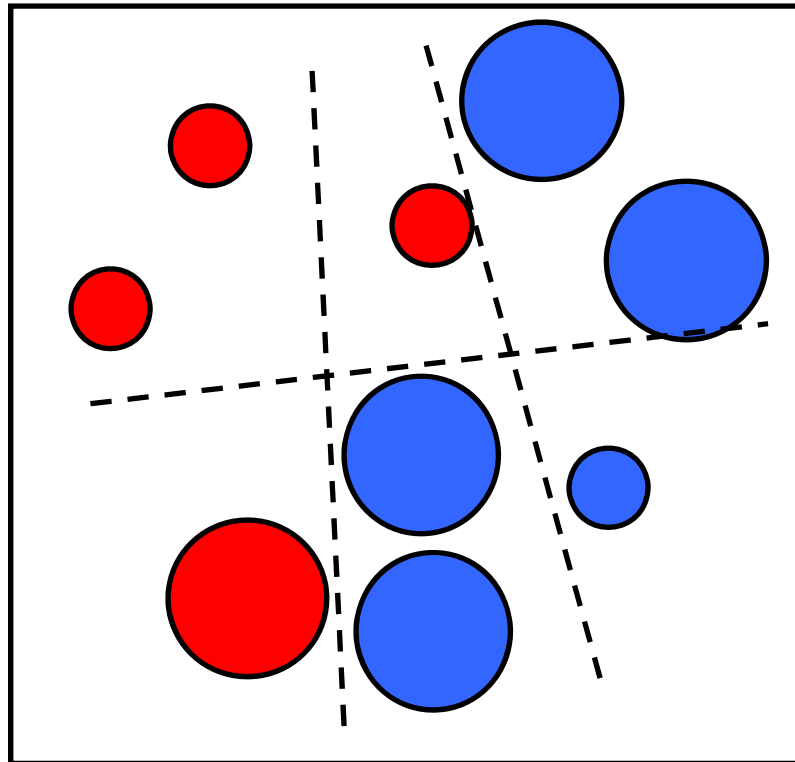


# Boosting illustration



# Boosting illustration

**Final classifier is  
a combination of weak  
classifiers**





# Boosting: training

- Initially, weight each training example equally
- In each boosting round:
  - Find the weak learner that achieves the lowest *weighted* training error
  - Raise weights of training examples misclassified by current weak learner
- Compute final classifier as linear combination of all weak learners (weight of each learner is directly proportional to its accuracy)
- Exact formulas for re-weighting and combining weak learners depend on the particular boosting scheme (e.g., AdaBoost)

# Challenges of face detection

- Sliding window detector must evaluate tens of thousands of location/scale combinations
- Faces are rare: 0-10 per image
  - A megapixel image has  $\sim 10^6$  pixels and a comparable number of candidate face locations
  - For computational efficiency, we should try to spend as little time as possible on the non-face windows
  - To avoid having a false positive in every image, our false positive rate has to be less than  $10^{-6}$

# The Viola/Jones Face Detector

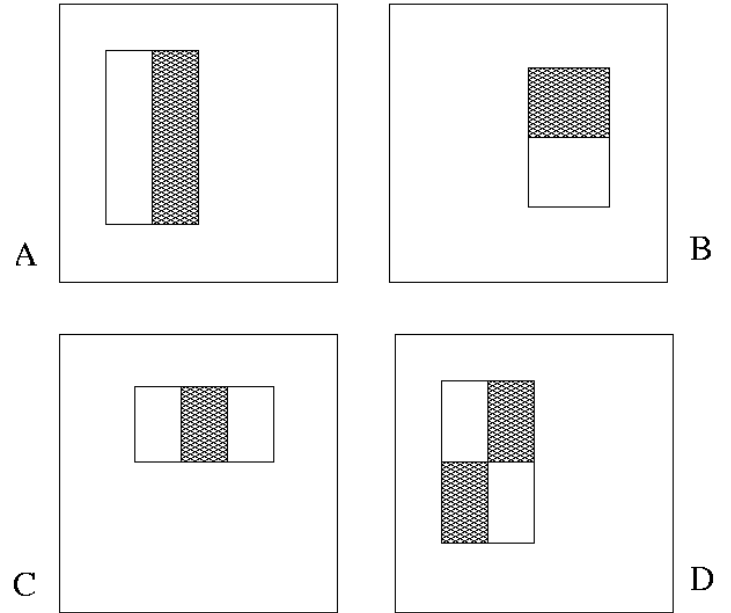
- A seminal approach to real-time object detection
- Training is slow, but detection is very fast
- Key ideas
  - *Integral images* for fast feature evaluation
  - *Boosting* for feature selection
  - *Attentional cascade* for fast rejection of non-face windows

P. Viola and M. Jones. [\*Rapid object detection using a boosted cascade of simple features\*](#). CVPR 2001.

P. Viola and M. Jones. [\*Robust real-time face detection\*](#). IJCV 57(2), 2004.

# Image Features

“Rectangle filters”

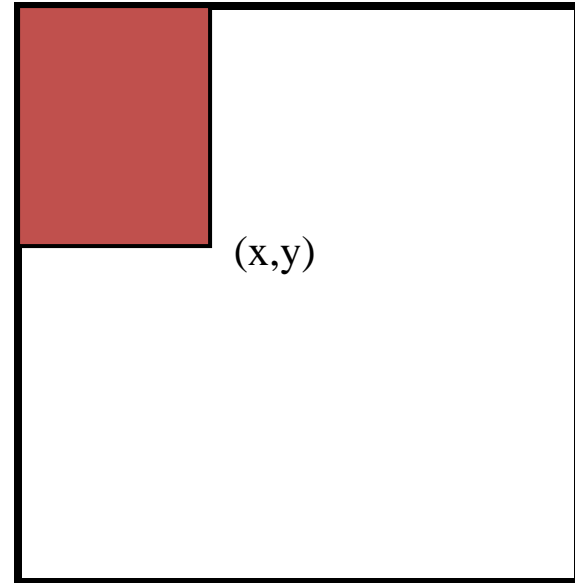


*Value* =

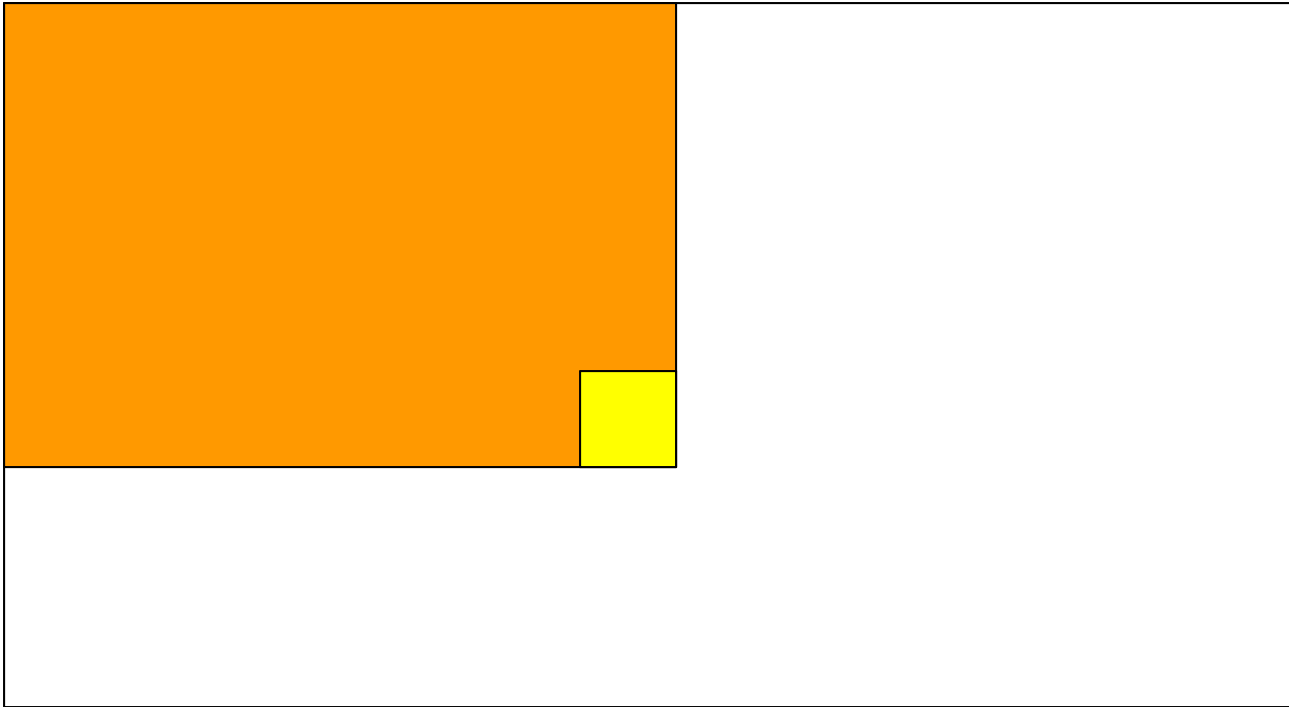
$$\sum (\text{pixels in white area}) - \sum (\text{pixels in black area})$$

# Fast computation with integral images

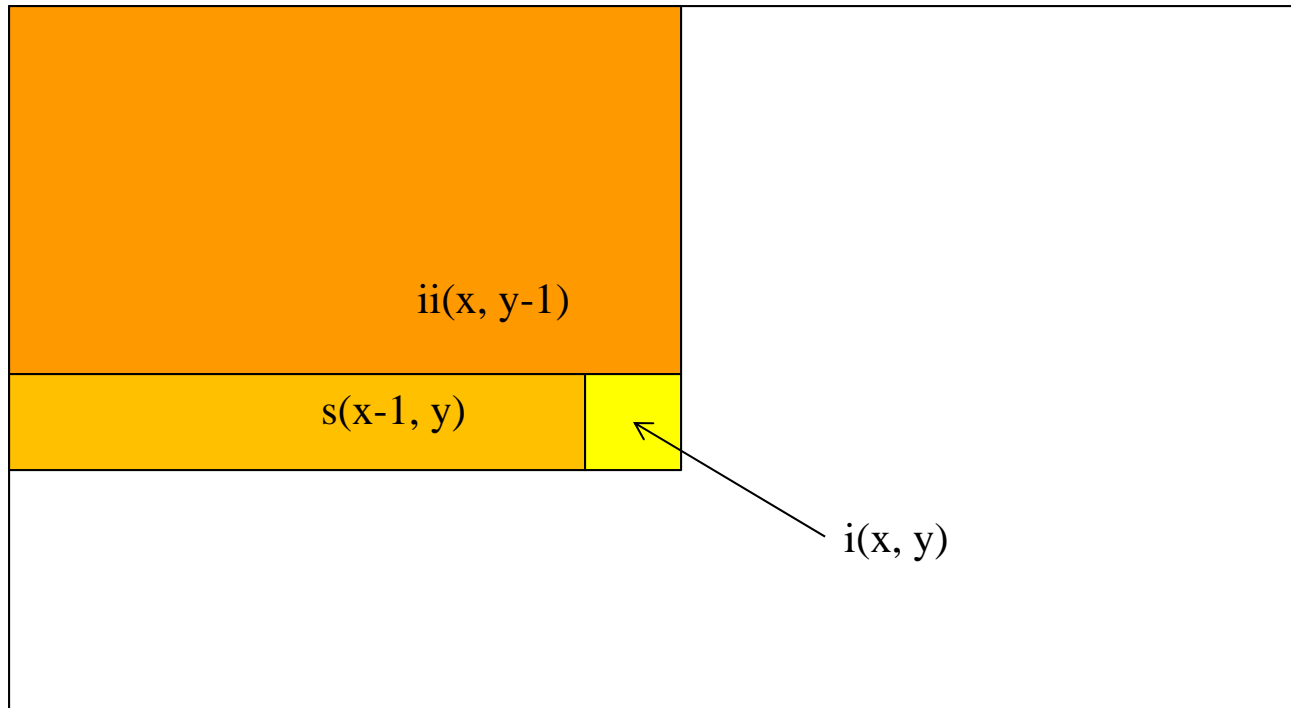
- The *integral image* computes a value at each pixel  $(x,y)$  that is the sum of the pixel values above and to the left of  $(x,y)$ , inclusive
- This can quickly be computed in one pass through the image



# Computing the integral image



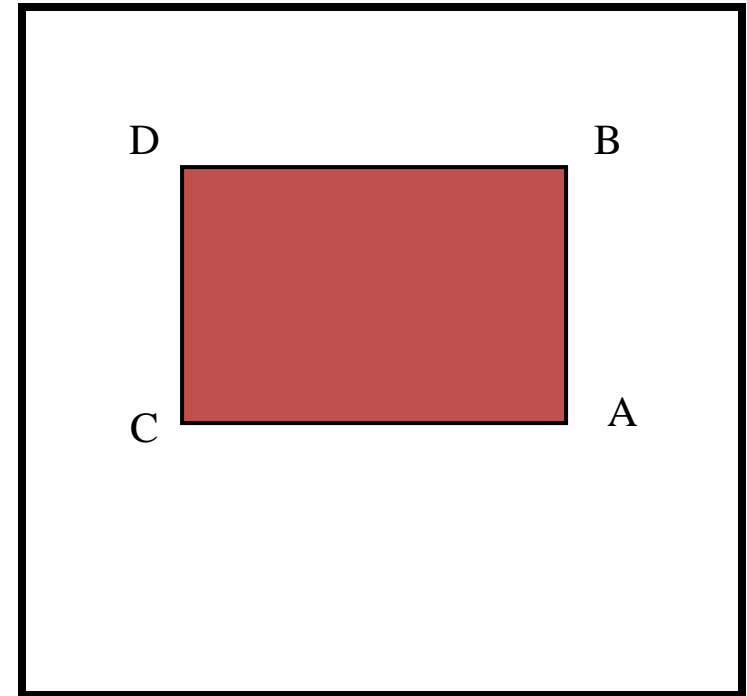
# Computing the integral image



- Cumulative row sum:  $s(x, y) = s(x-1, y) + i(x, y)$
- Integral image:  $ii(x, y) = ii(x, y-1) + s(x, y)$

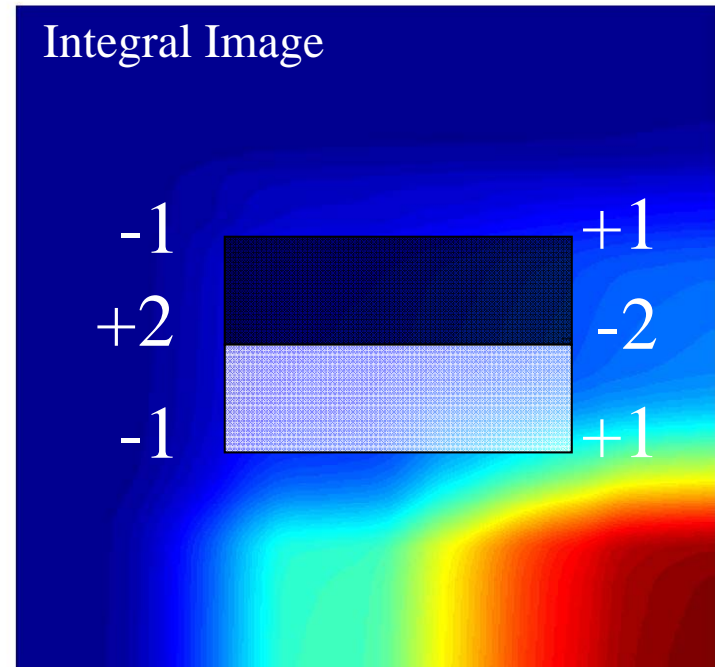
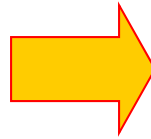
# Computing sum within a rectangle

- Let A,B,C,D be the values of the integral image at the corners of a rectangle
- Then the sum of original image values within the rectangle can be computed as:  
$$\text{sum} = A - B - C + D$$
- Only 3 additions are required for any size of rectangle!



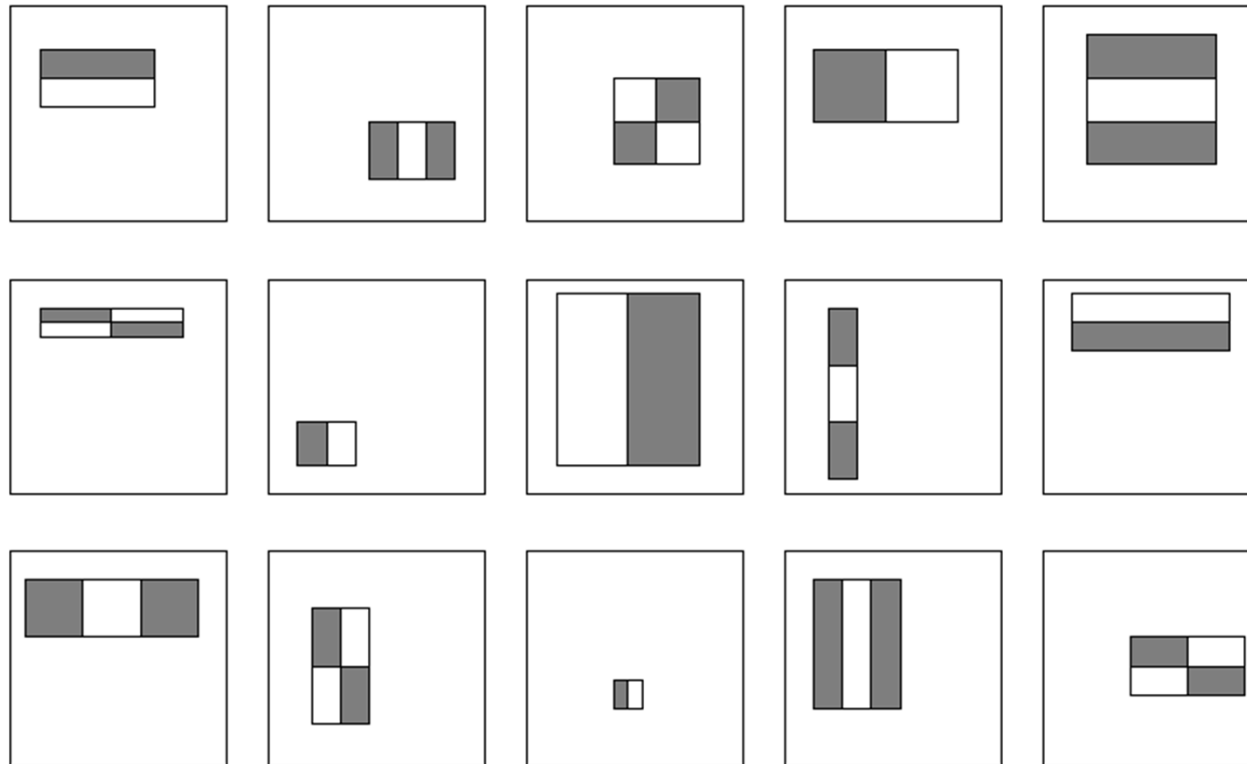


# Computing a rectangle feature



# Feature selection

- For a 24x24 detection region, the number of possible rectangle features is  $\sim 160,000$ !



# Feature selection

- For a 24x24 detection region, the number of possible rectangle features is  $\sim 160,000$ !
- At test time, it is impractical to evaluate the entire feature set
- Can we create a good classifier using just a small subset of all possible features?
- How to select such a subset?

# Boosting

- *Boosting* combines *weak learners* into a more accurate *ensemble classifier*
- Weak learners based on rectangle filters:

$$h_t(x) = \begin{cases} 1 & \text{if } f_t(x) > \theta_t \\ 0 & \text{otherwise} \end{cases}$$

Diagram annotations for the weak classifier equation:

- $h_t(x)$ : window
- $f_t(x)$ : value of rectangle feature
- $\theta_t$ : threshold

- Ensemble classification function:

$$C(x) = \begin{cases} 1 & \text{if } \sum_{t=1}^T \alpha_t h_t(x) > \frac{1}{2} \sum_{t=1}^T \alpha_t \\ 0 & \text{otherwise} \end{cases}$$

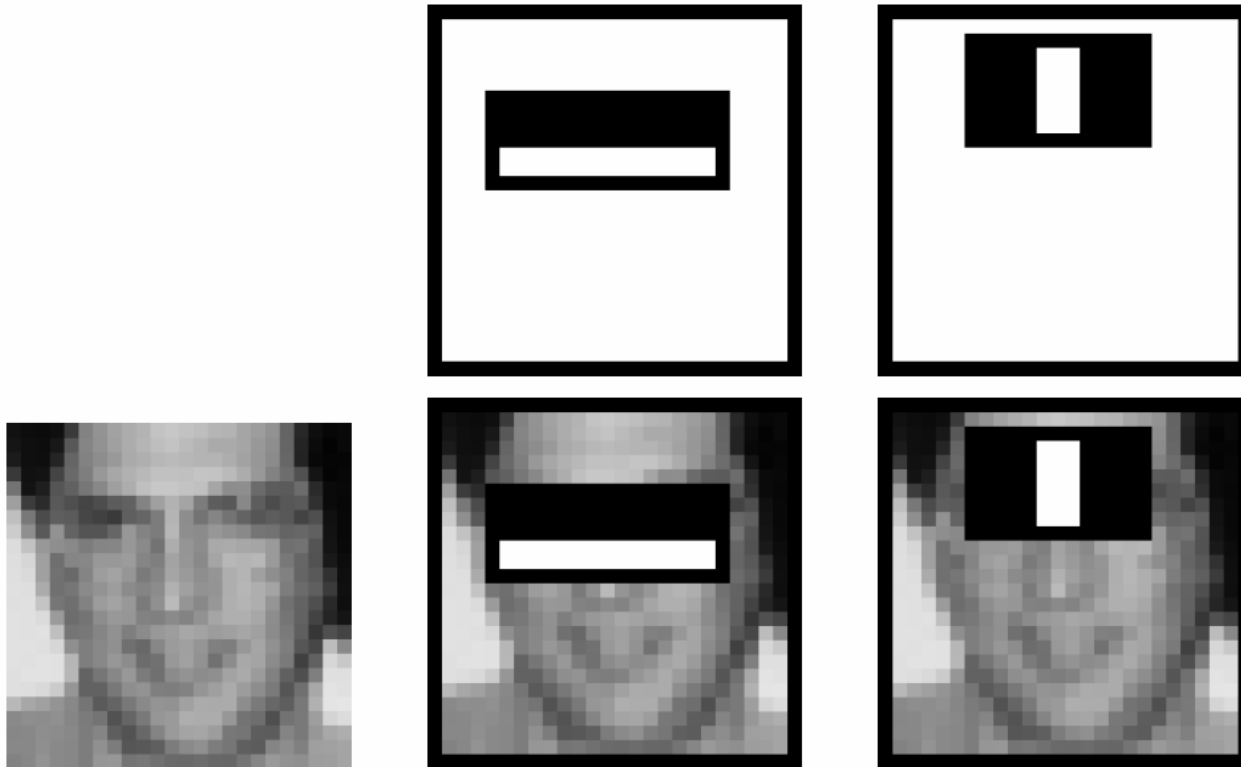
Diagram annotation for the ensemble function:

- $\alpha_t$ : learned weights

# Boosting for face detection

- First two features selected by boosting:

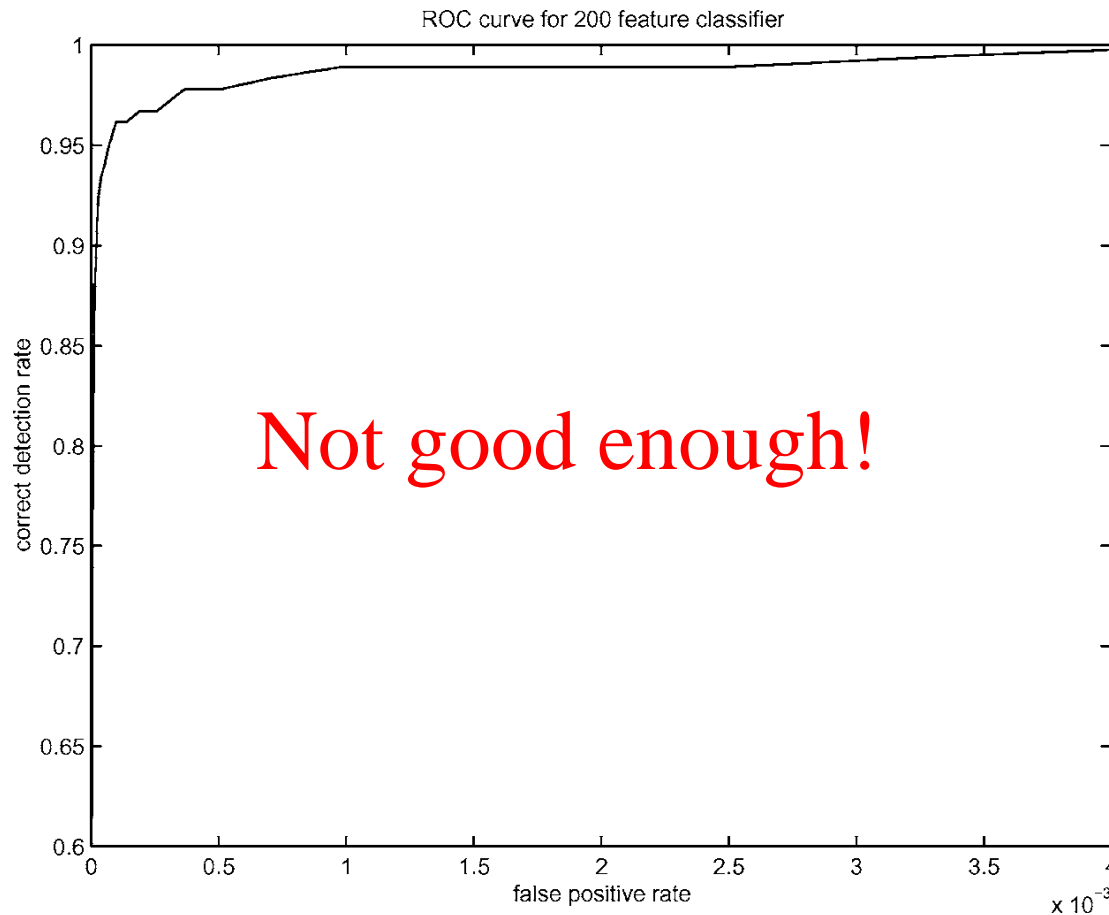
- 



This feature combination can yield 100% detection rate and 50% false positive rate

# Boosting for face detection

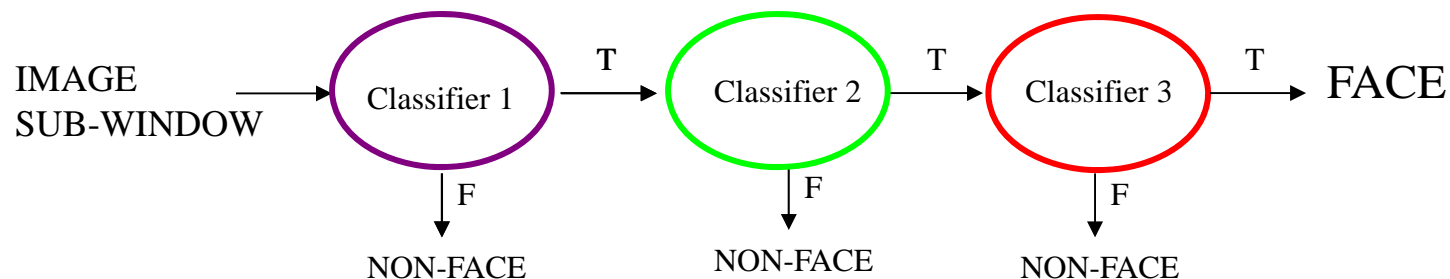
- A 200-feature classifier can yield 95% detection rate and a false positive rate of 1 in 14084



Receiver operating characteristic (ROC) curve

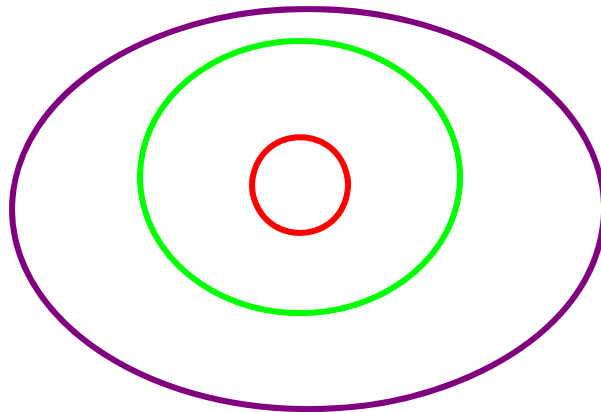
# Attentional cascade

- We start with simple classifiers which reject many of the negative sub-windows while detecting almost all positive sub-windows
- Positive response from the first classifier triggers the evaluation of a second (more complex) classifier, and so on
- A negative outcome at any point leads to the immediate rejection of the sub-window

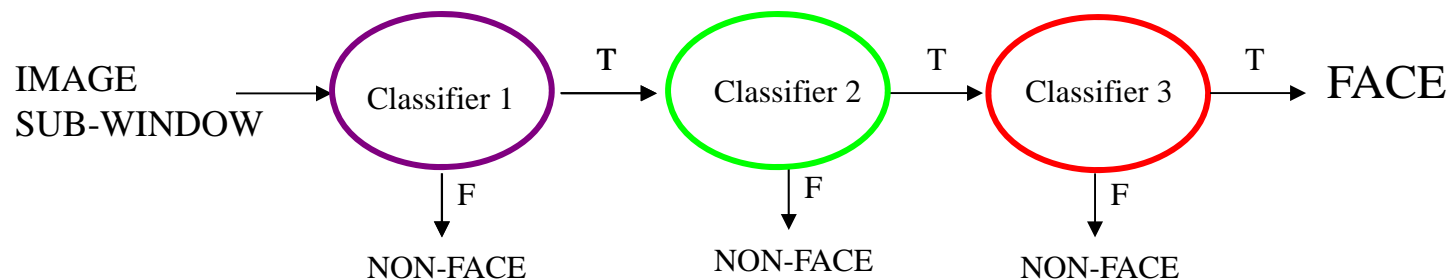
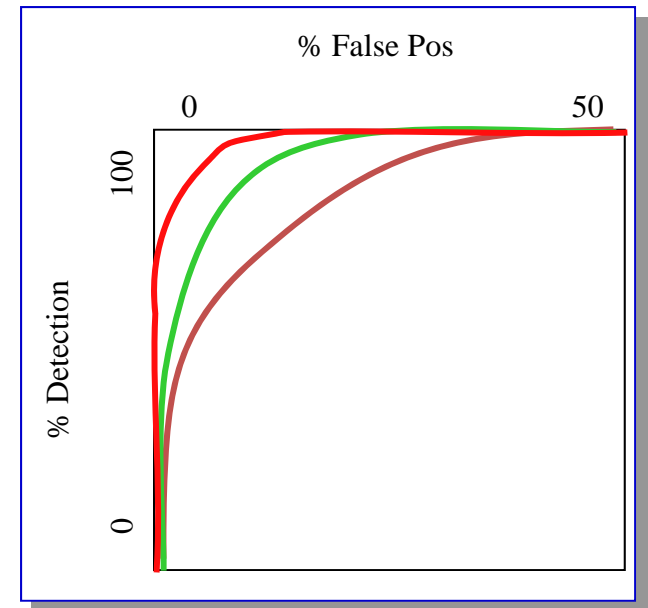


# Attentional cascade

- Chain classifiers that are progressively more complex and have lower false positive rates:



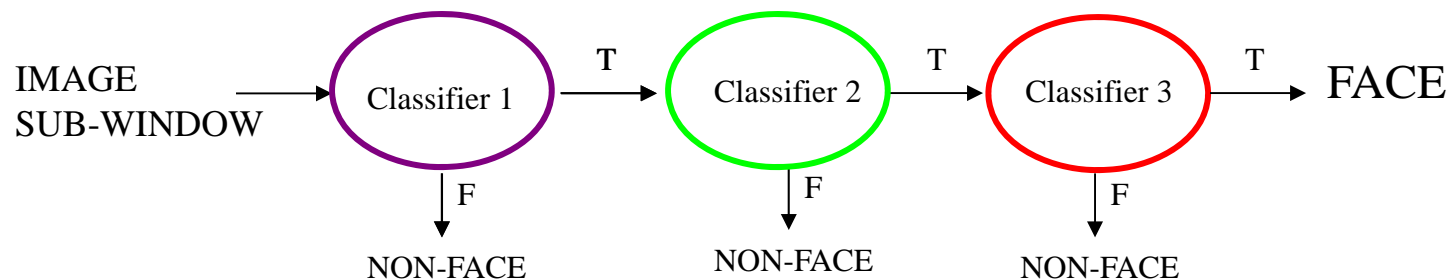
Receiver operating characteristic





# Attentional cascade

- The detection rate and the false positive rate of the cascade are found by multiplying the respective rates of the individual stages
- A detection rate of 0.9 and a false positive rate on the order of  $10^{-6}$  can be achieved by a 10-stage cascade if each stage has a detection rate of 0.99 ( $0.99^{10} \approx 0.9$ ) and a false positive rate of about 0.30 ( $0.3^{10} \approx 6 \times 10^{-6}$ )



# Training the cascade

- Set target detection and false positive rates for each stage
- Keep adding features to the current stage until its target rates have been met
  - Need to lower AdaBoost threshold to maximize detection  
(as opposed to minimizing total classification error)
  - Test on a *validation set*
- If the overall false positive rate is not low enough, then add another stage
- Use false positives from current stage as the negative training examples for the next stage

# The implemented system

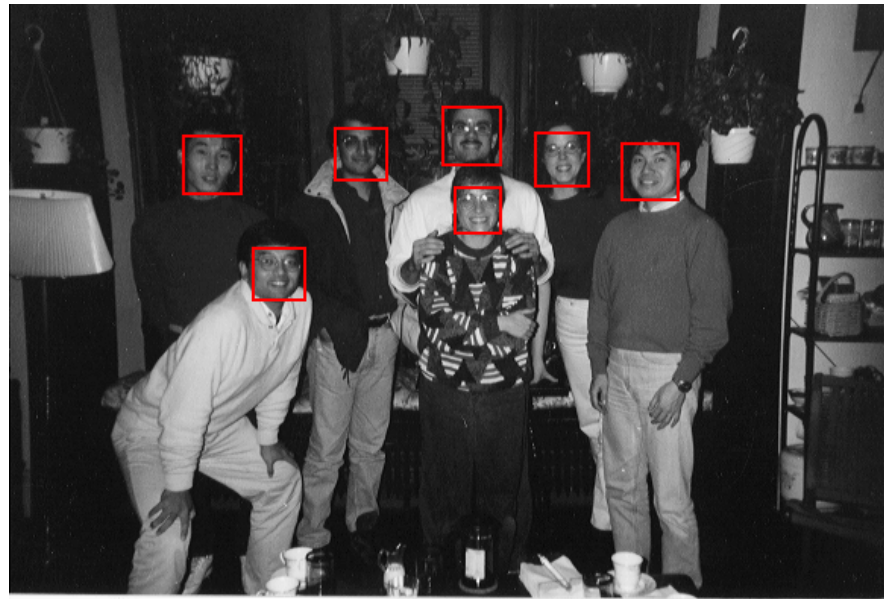
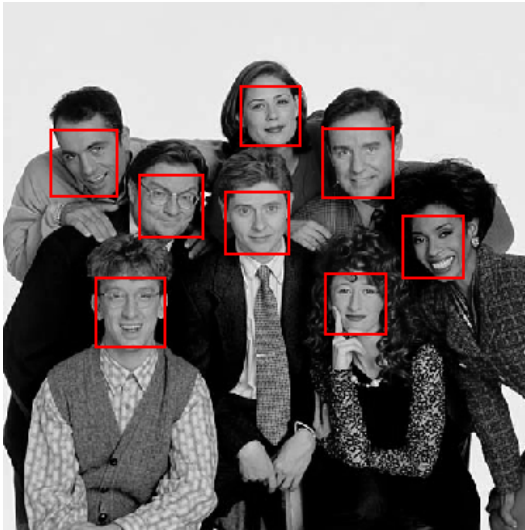
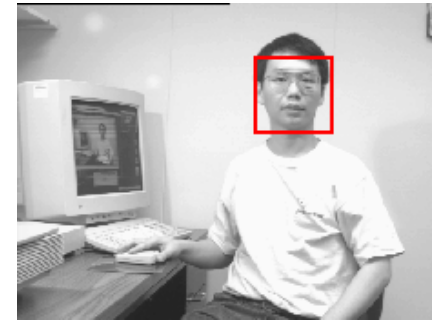
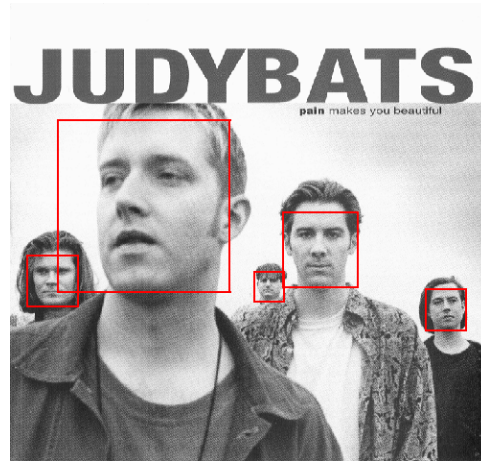
- Training Data
  - 5000 faces
    - All frontal, rescaled to 24x24 pixels
  - 300 million non-faces
    - 9500 non-face images
  - Faces are normalized
    - Scale, translation
- Many variations
  - Across individuals
  - Illumination
  - Pose



# System performance

- Training time: “weeks” on 466 MHz Sun workstation
- 38 layers, total of 6061 features
- Average of 10 features evaluated per window on test set
- “On a 700 Mhz Pentium III processor, the face detector can process a 384 by 288 pixel image in about .067 seconds”
  - 15 Hz
  - 15 times faster than previous detector of comparable accuracy

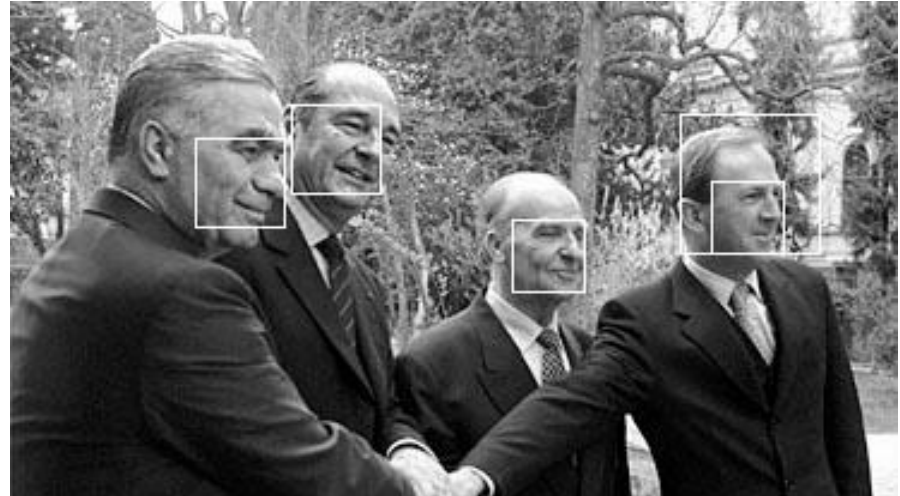
# Output of Face Detector on Test Images



# Related detection tasks

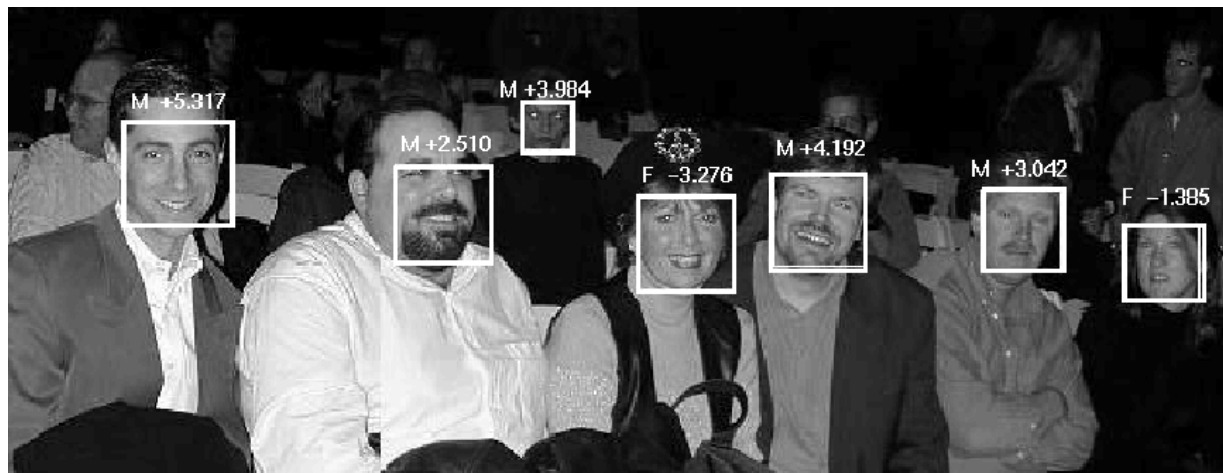


Facial Feature Localization

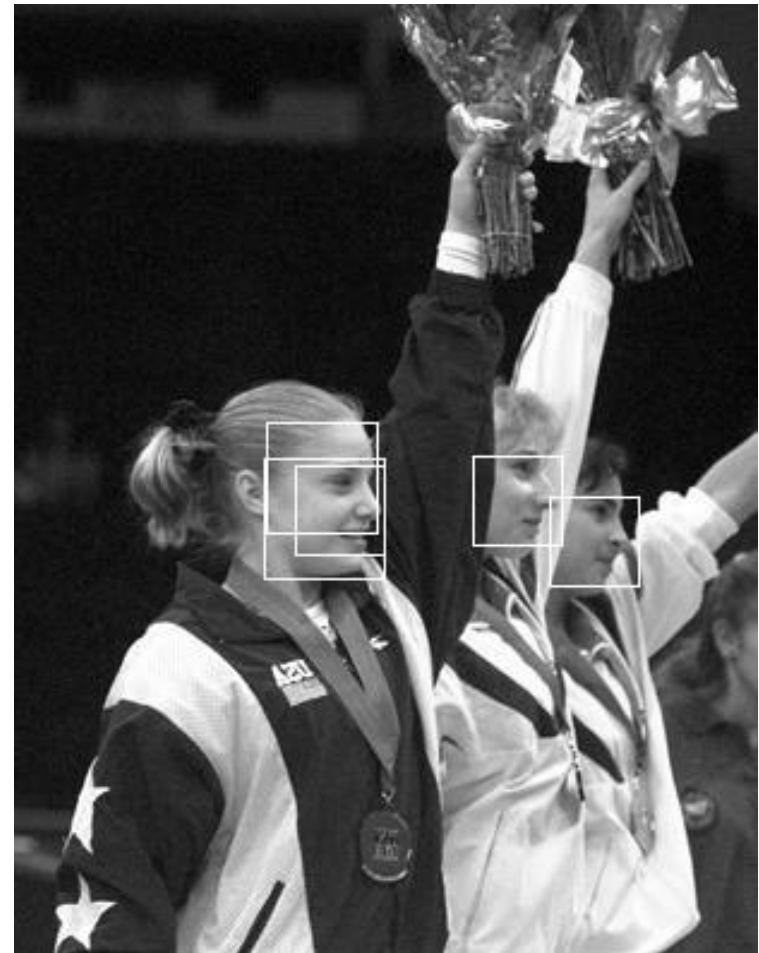


Profile Detection

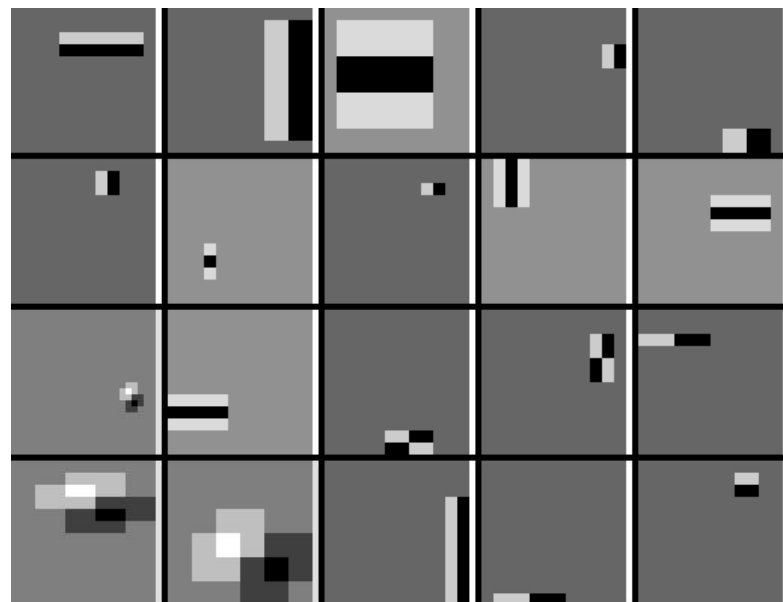
Male vs.  
female



# Profile Detection



# Profile Features





# Summary: Viola/Jones detector

- Rectangle features
- Integral images for fast computation
- Boosting for feature selection
- Attentional cascade for fast rejection of negative windows

# Face detection and recognition



Detection



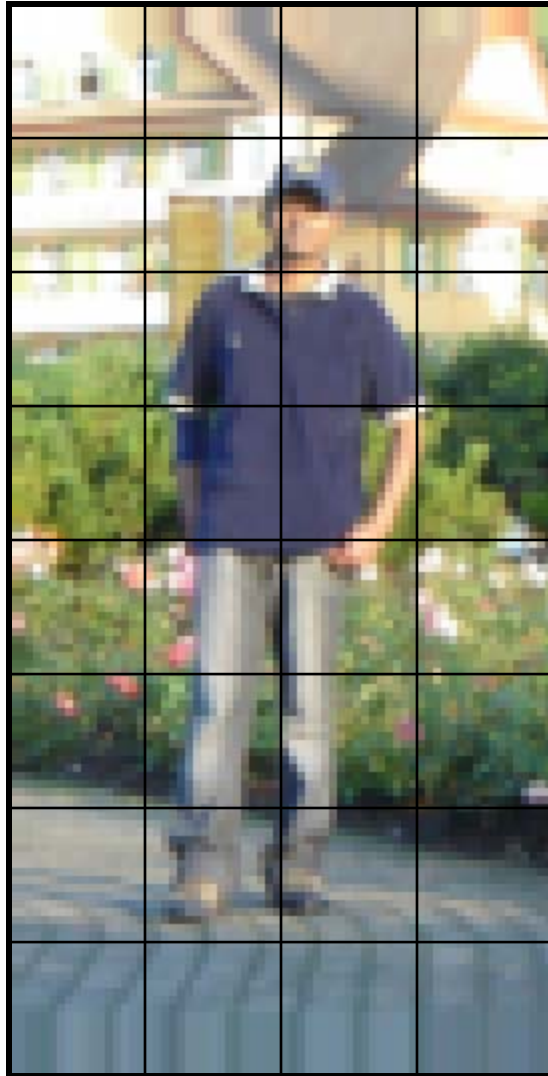
Recognition

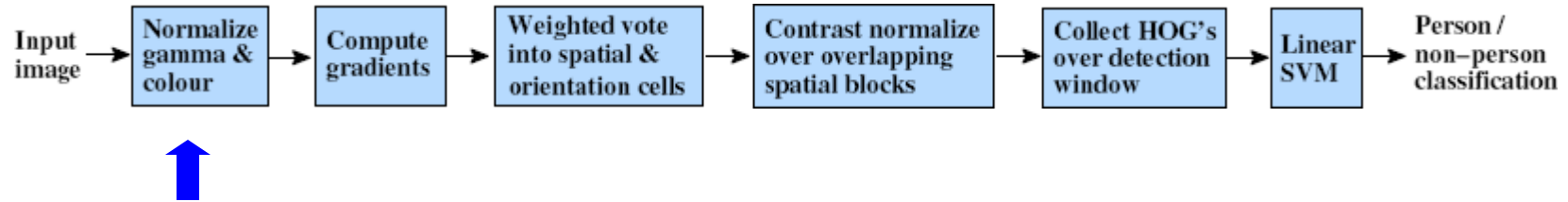
“Sally”

# Dalal-Triggs pedestrian detector



1. Extract fixed-sized (64x128 pixel) window at each position and scale
2. Compute HOG (histogram of gradient) features within each window
3. Score the window with a linear SVM classifier
4. Perform non-maxima suppression to remove overlapping detections with lower scores





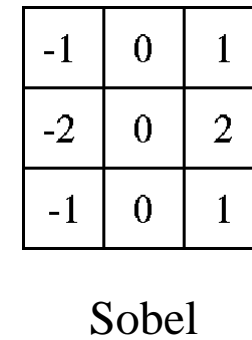
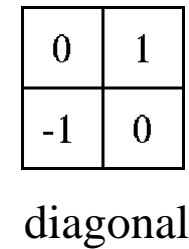
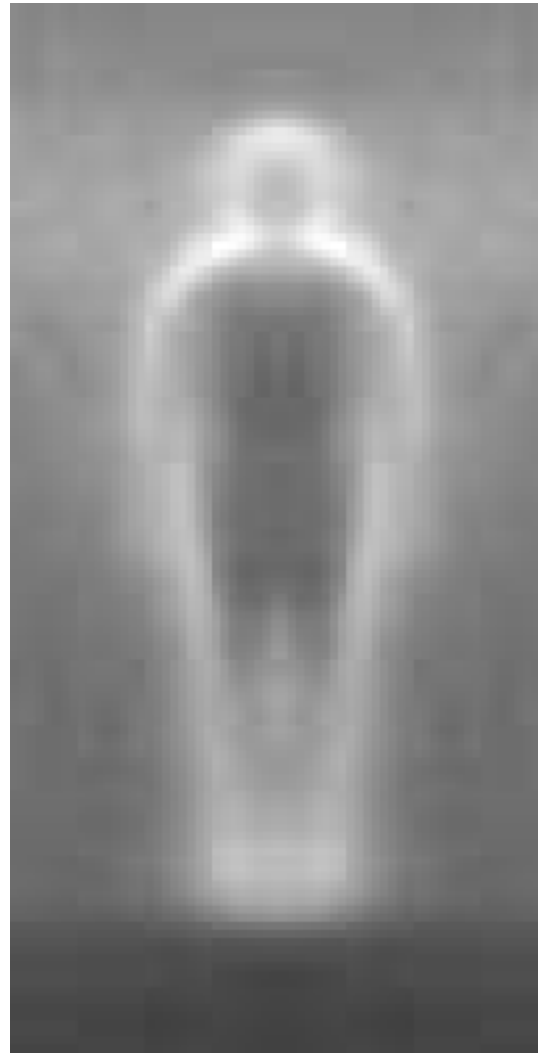
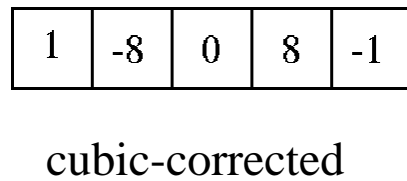
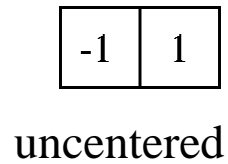
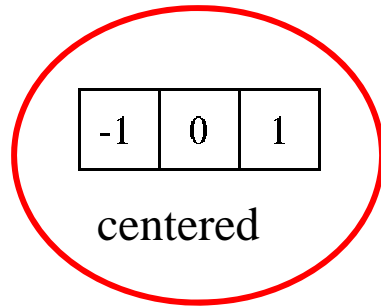
- Tested with
  - RGB
  - LAB
  - Grayscale

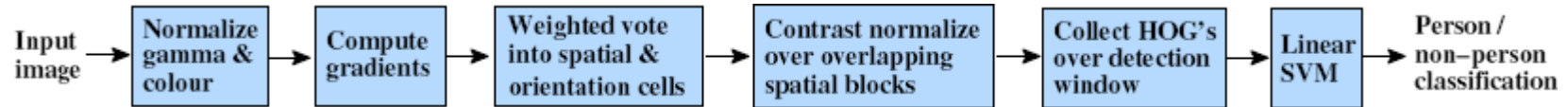
} Slightly better performance vs. grayscale
- Gamma Normalization and Compression
  - Square root
  - Log

} Very slightly better performance vs. no adjustment



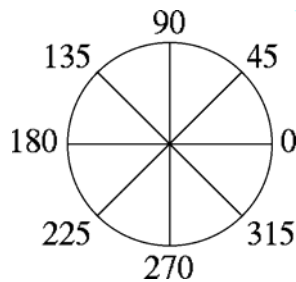
Works best



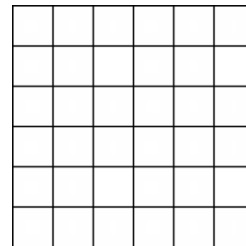


- Histogram of gradient orientations

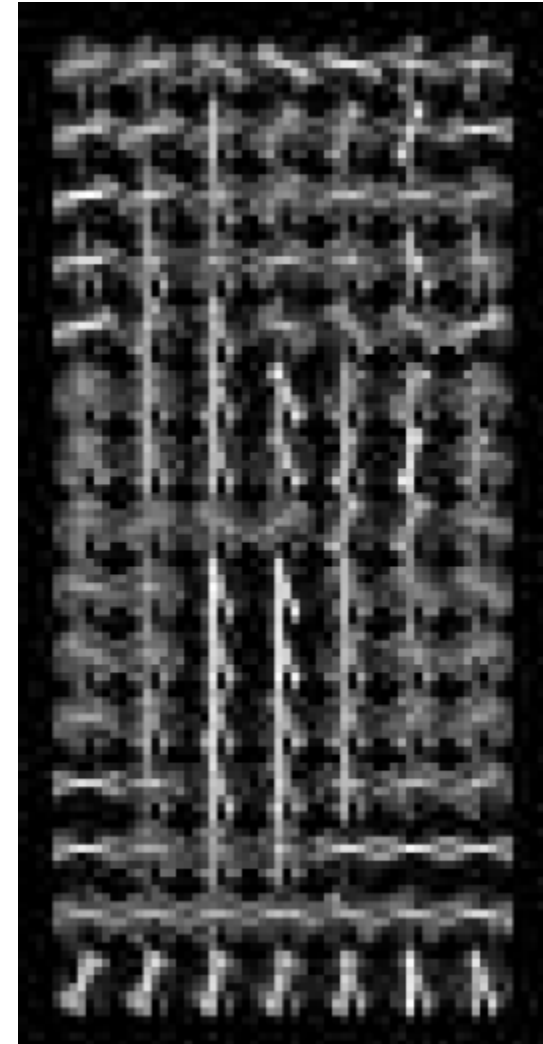
Orientation: 9 bins (for unsigned angles 0-180)



Histograms in 8x8 pixel cells



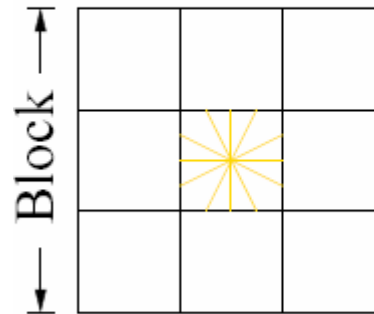
- Votes weighted by magnitude
- Bilinear interpolation between cells





R-HOG

Cell



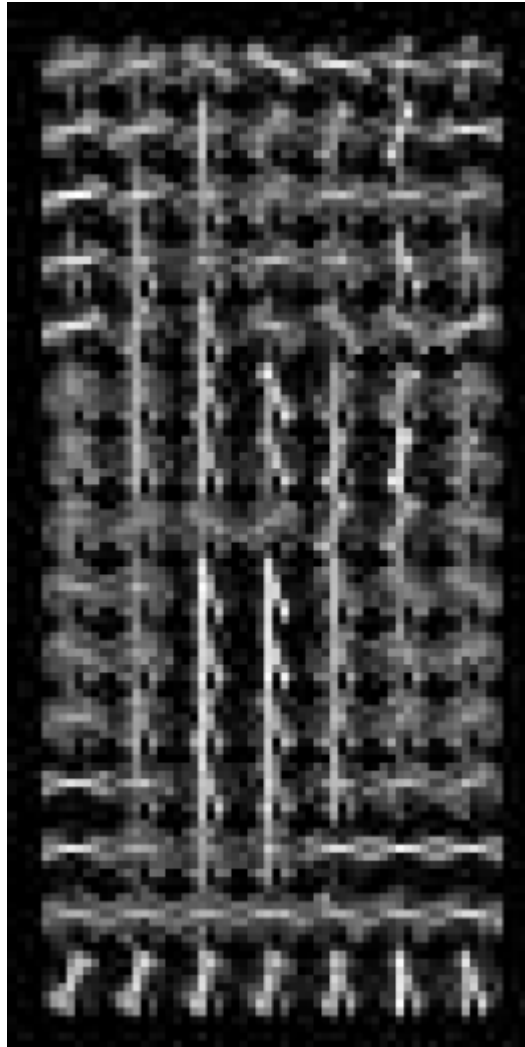
Normalize with respect to surrounding cells in overlapping blocks with different cell and block sizes

$$L2 - norm : v \longrightarrow v / \sqrt{\|v\|_2^2 + \epsilon^2}$$



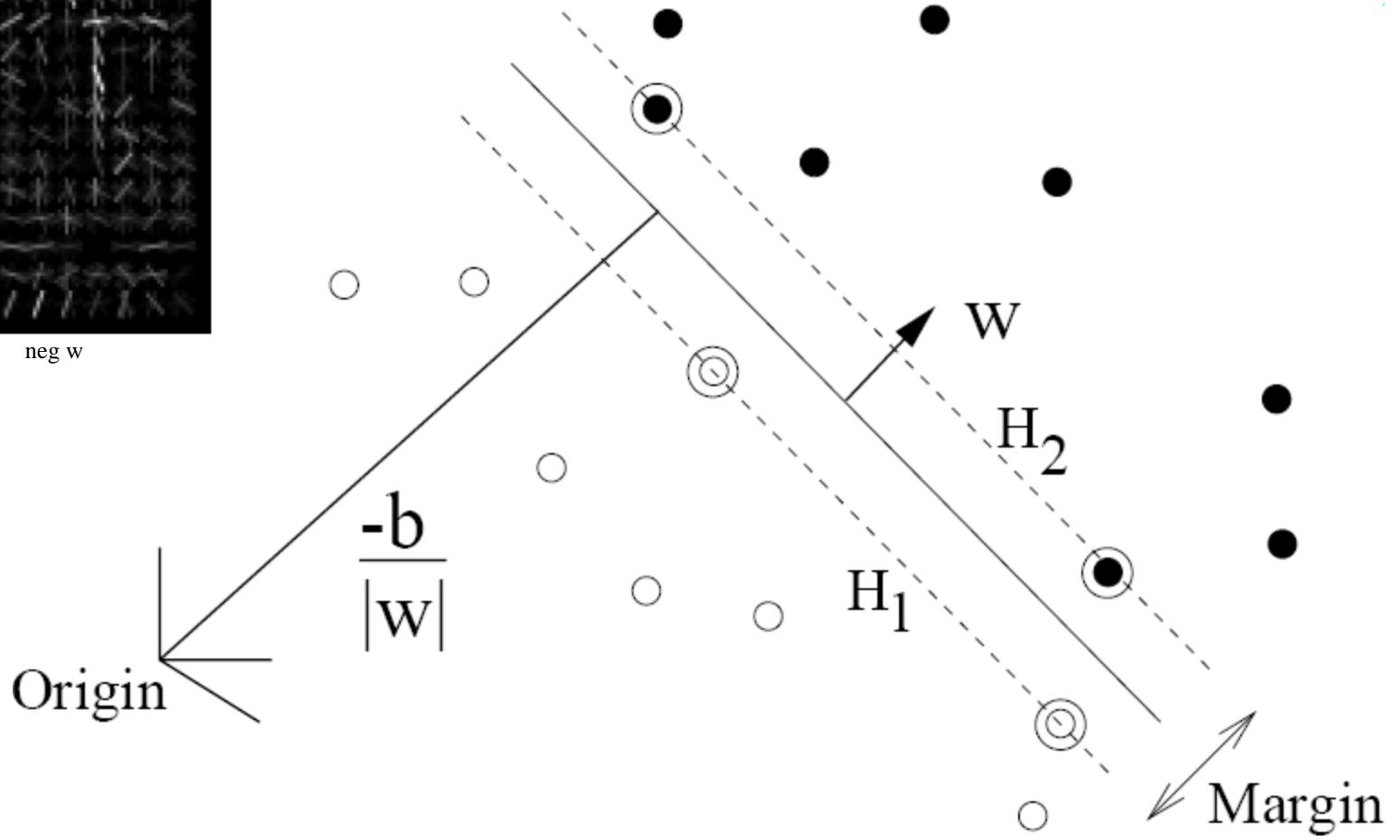
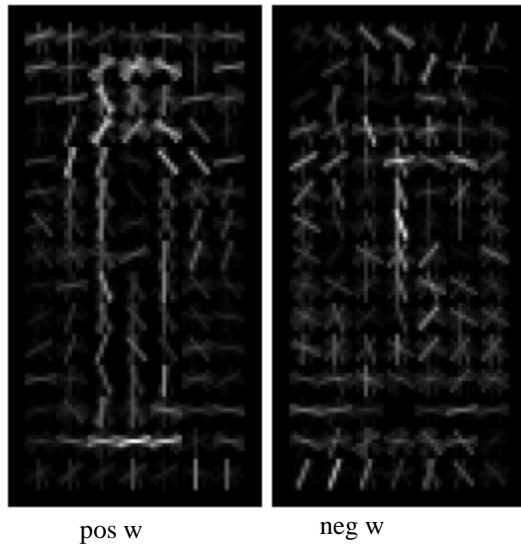


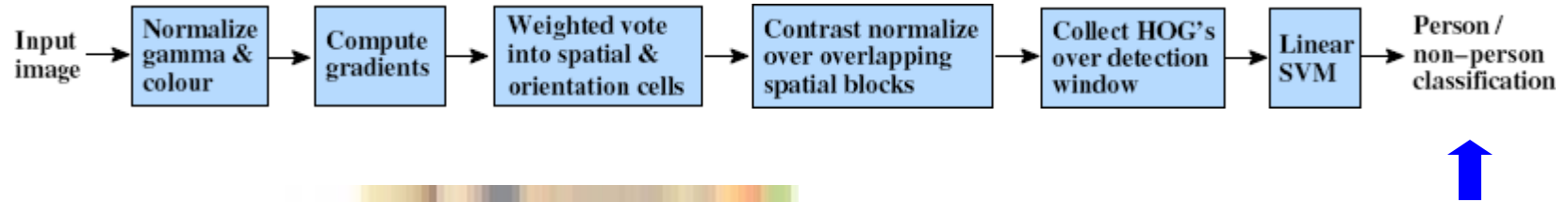
X=



$$\# \text{ features} = 15 \times 7 \times 9 \times 4 = 3780$$

# orientations  
 # cells  
 # normalizations by neighboring cells





$$0.16 = w^T x - b$$

$$\text{sign}(0.16) = 1$$

$\Rightarrow$  pedestrian

# Pedestrian detection with HOG

- Train a pedestrian template using a linear support vector machine

positive training examples



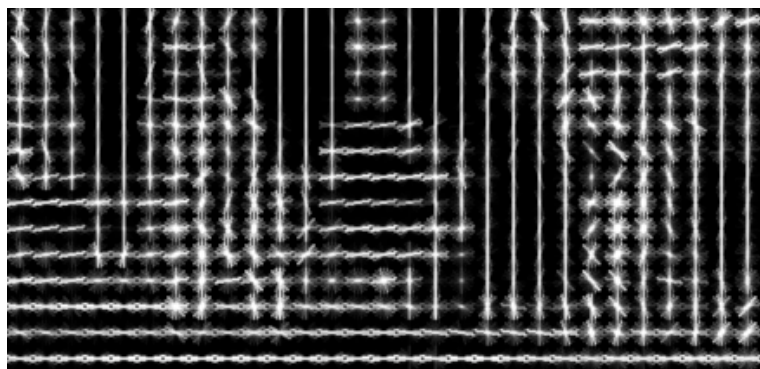
negative training examples



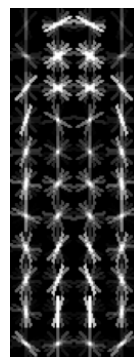
# Pedestrian detection with HOG

- Train a pedestrian template using a linear support vector machine
- At test time, convolve feature map with template
- Find local maxima of response - apply non-max suppression
- For multi-scale detection, repeat over multiple levels of a HOG *pyramid*

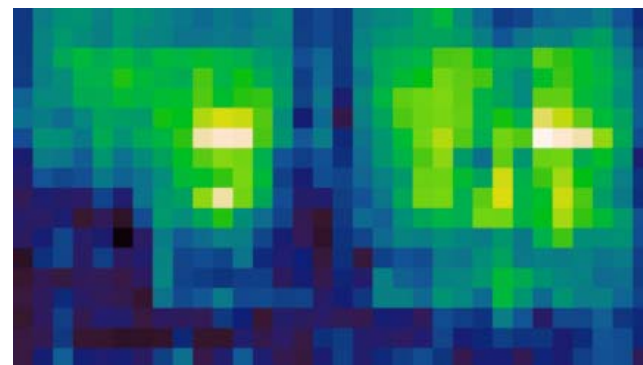
HOG feature map



Template



Detector response map





# Detection examples

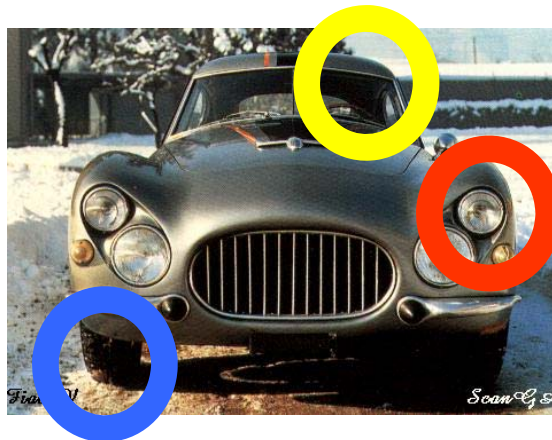


# Part-based Models

# Part-based Models

Define object by collection of parts modeled by

1. Appearance
2. Spatial configuration

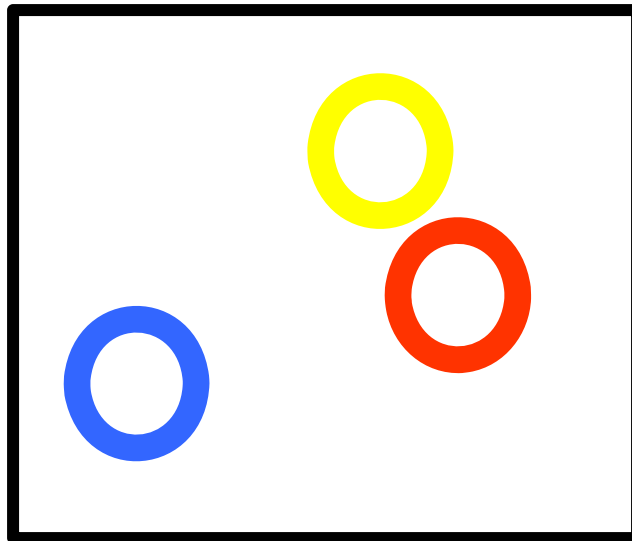


Slide credit: Rob Fergus



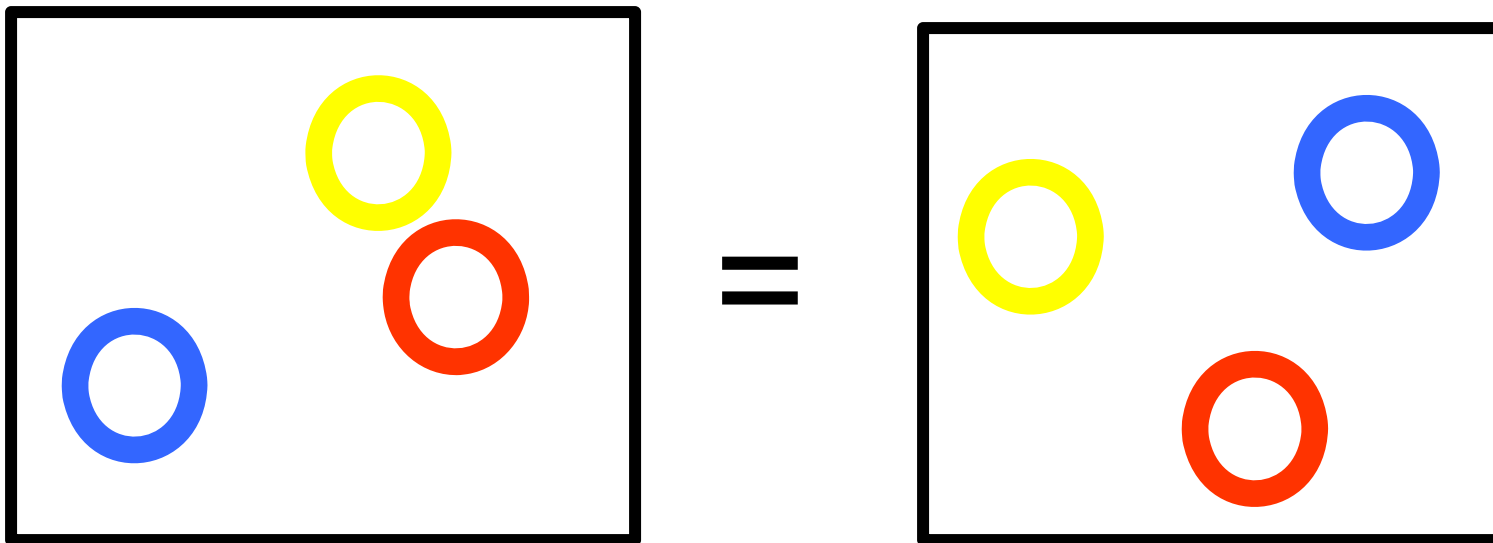
# How to model spatial relations?

- One extreme: fixed template



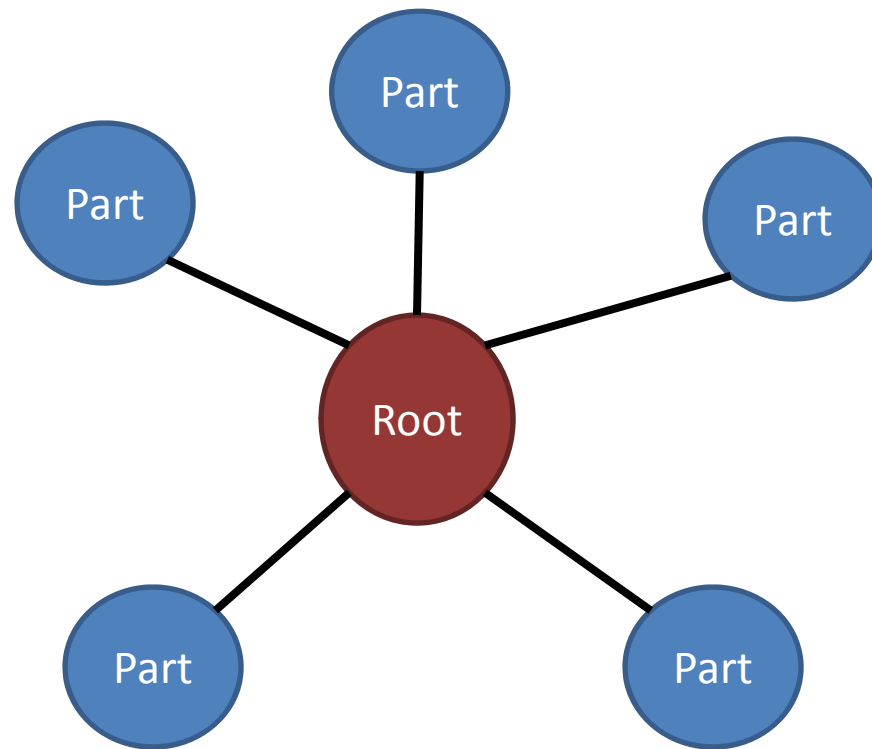
# How to model spatial relations?

- Another extreme: bag of words



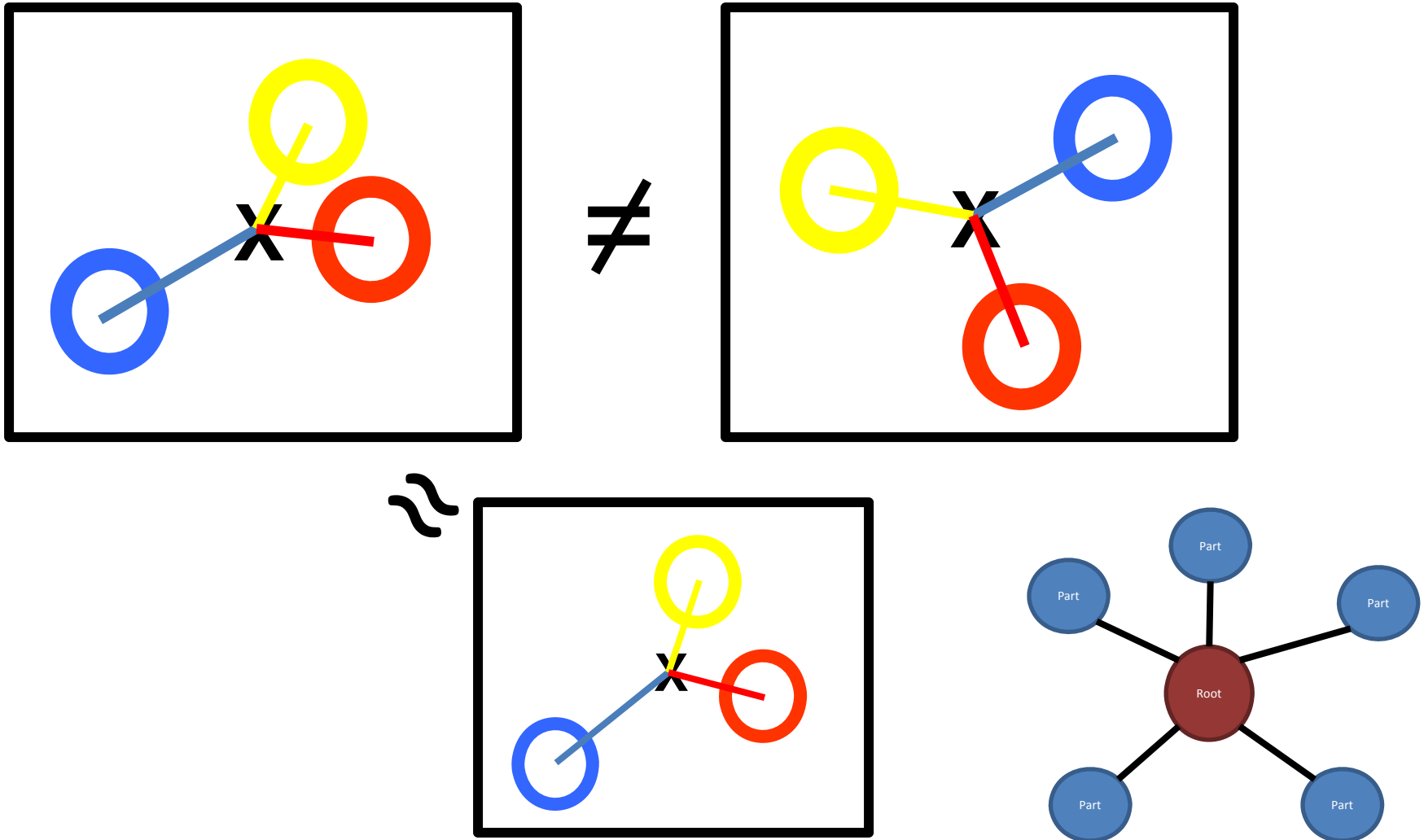
# How to model spatial relations?

- Star-shaped model



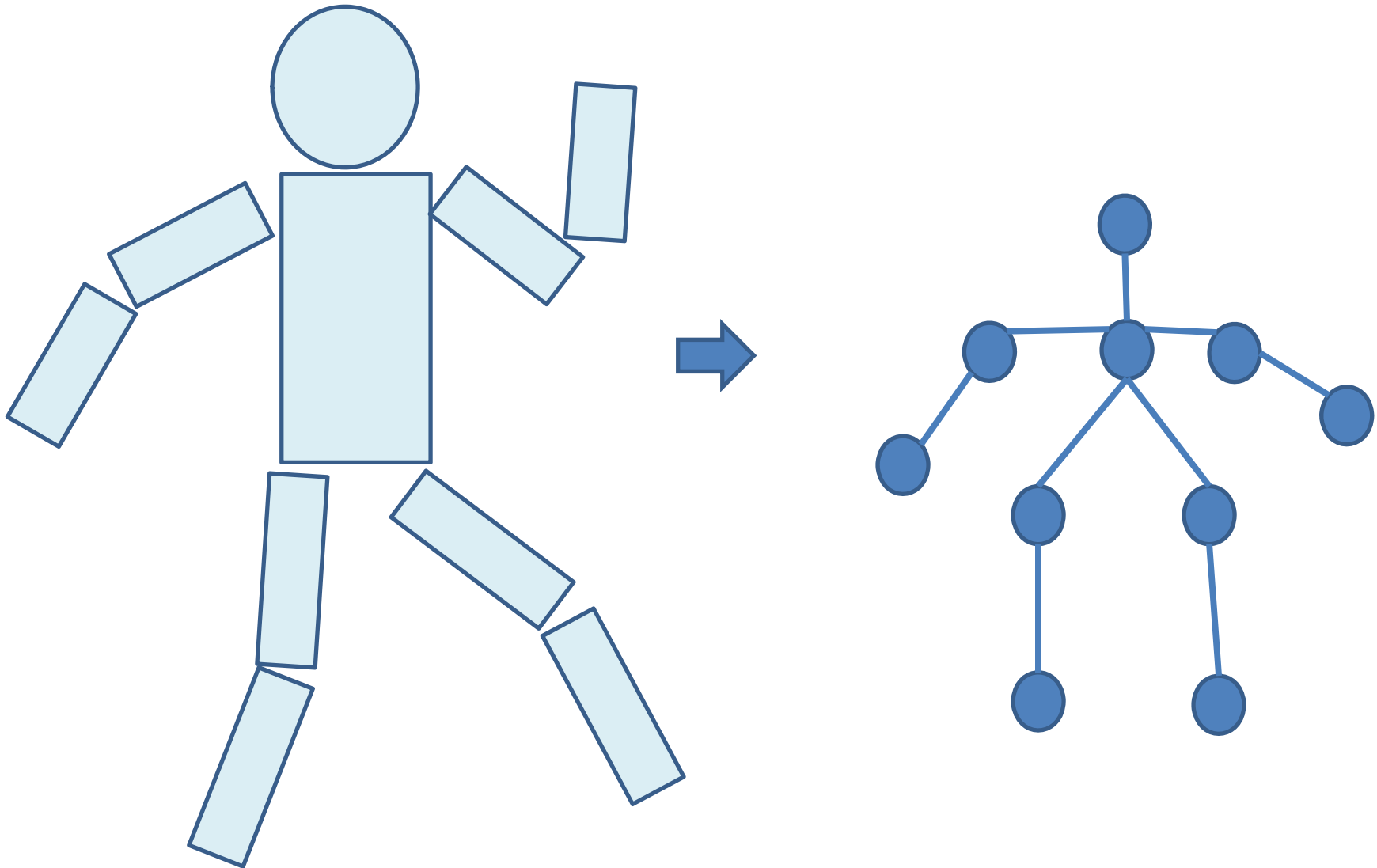
# How to model spatial relations?

- Star-shaped model



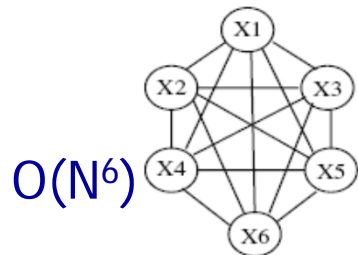
# How to model spatial relations?

- Tree-shaped model



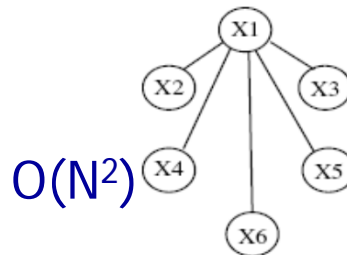
# How to model spatial relations?

- Many others...



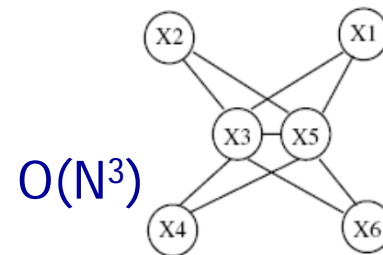
a) Constellation

Fergus et al. '03  
Fei-Fei et al. '03



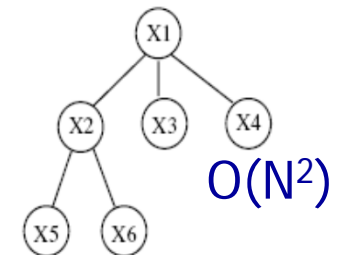
b) Star shape

Leibe et al. '04, '08  
Crandall et al. '05  
Fergus et al. '05



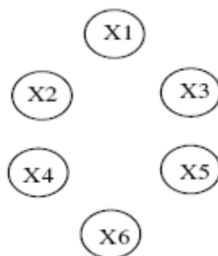
c)  $k$ -fan ( $k = 2$ )

Crandall et al. '05



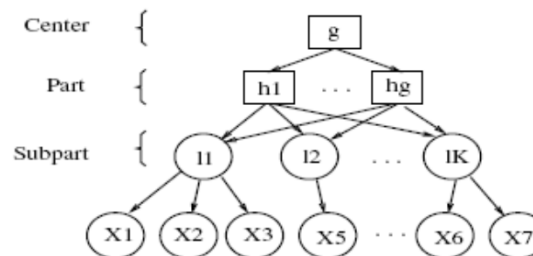
d) Tree

Felzenszwalb &  
Huttenlocher '05



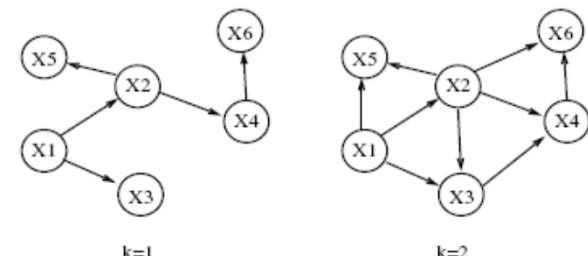
e) Bag of features

Csurka '04  
Vasconcelos '00



f) Hierarchy

Bouchard & Triggs '05



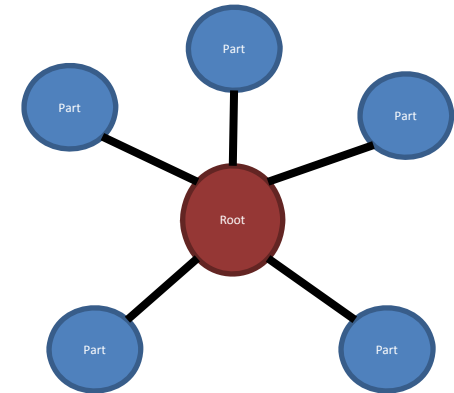
g) Sparse flexible model

Carneiro & Lowe '06

# Star and Tree-shaped Models

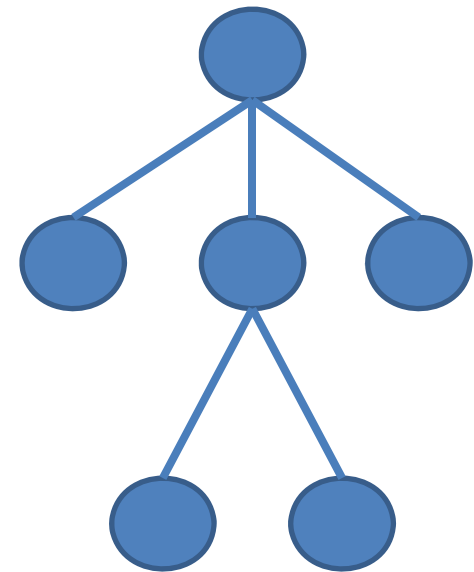
## 1. Star-shaped model

- Example: Deformable Parts Model
  - [Felzenszwalb et al. 2010](#)



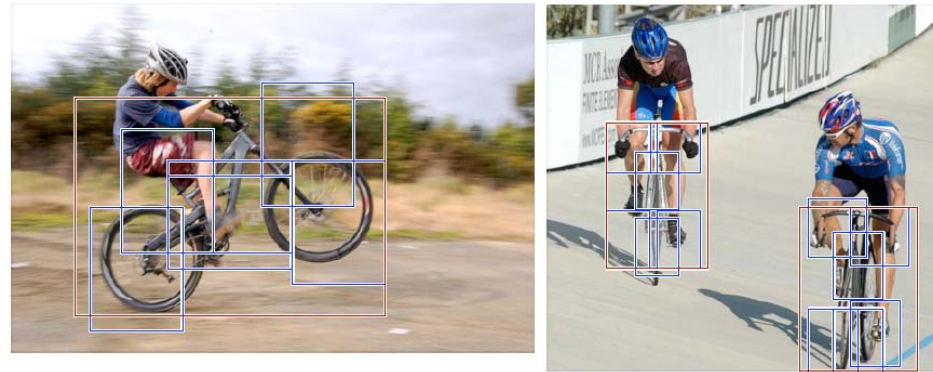
## 2. Tree-shaped model

- Example: Pictorial structures
  - [Felzenszwalb Huttenlocher 2005](#)

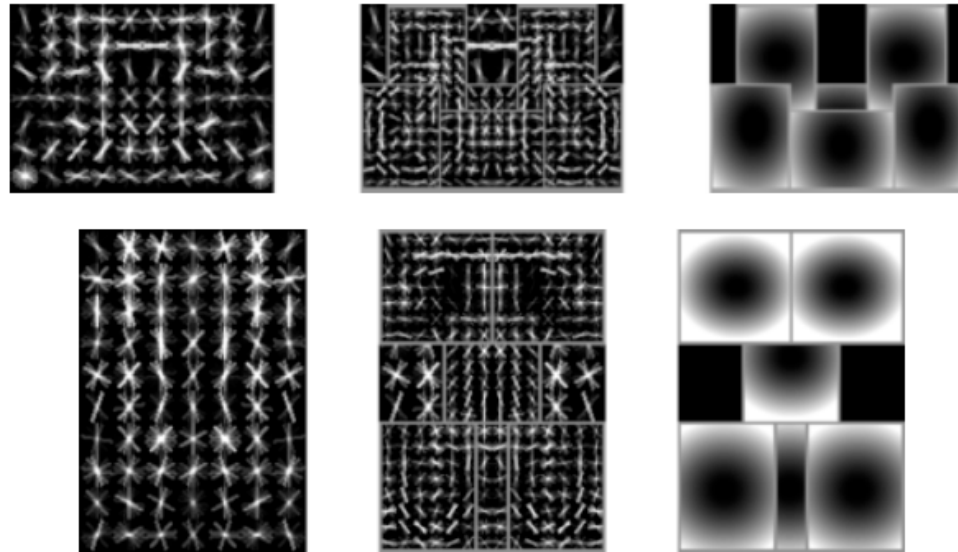


# Deformable Part Model (DPM)

Detections



Template Visualization



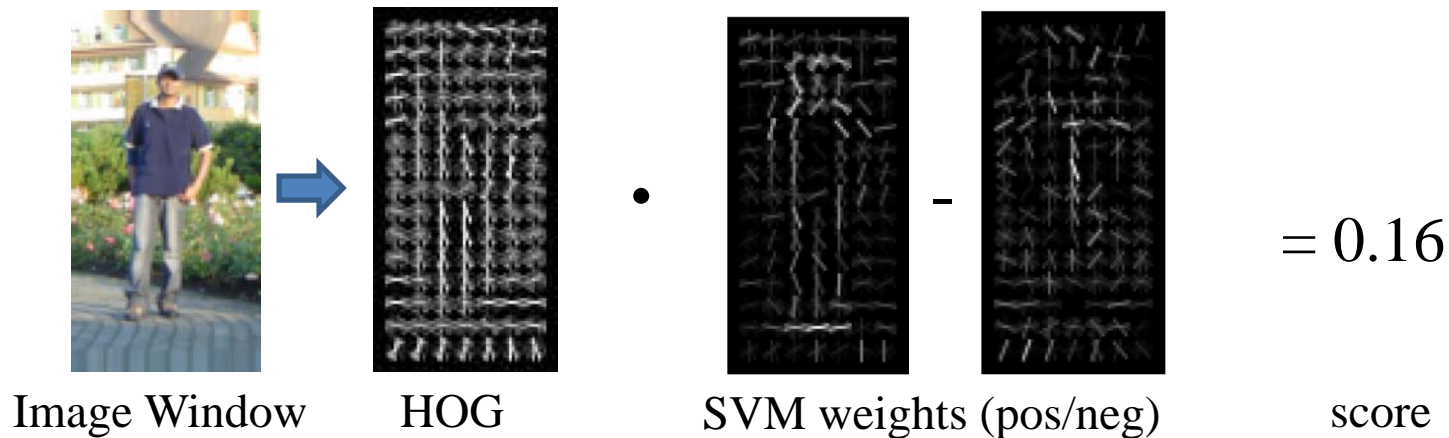
root filters  
coarse resolution

part filters  
finer resolution

deformation  
models



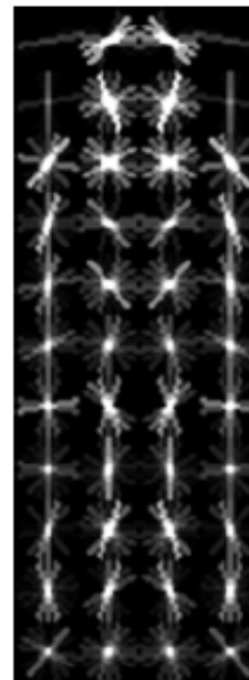
# Review: Dalal-Triggs detector



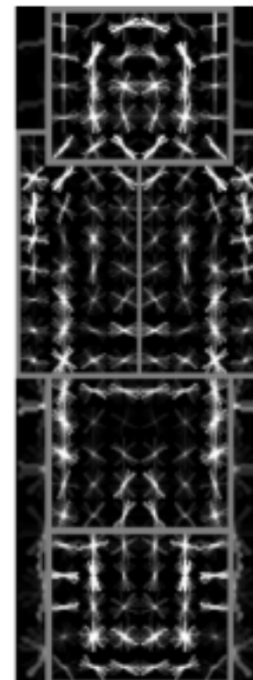
1. Extract fixed-sized (64x128 pixel) window at each position and scale
2. Compute HOG (histogram of gradient) features within each window
3. Score the window with a linear SVM classifier
4. Perform non-maxima suppression to remove overlapping detections with lower scores

# Deformable parts model

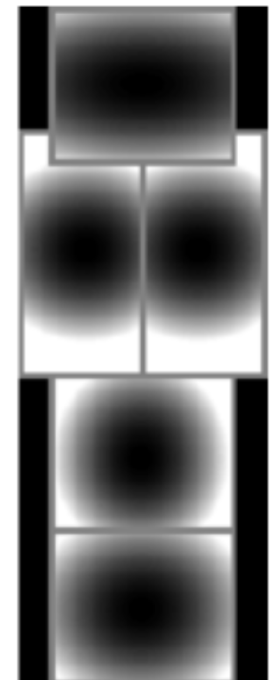
- Root filter models coarse whole-object appearance
- Part filters model finer-scale appearance of smaller patches
- For each root window, part positions that maximize appearance score minus spatial cost are found
- Total score is sum of scores of each filter and spatial costs



Root filter

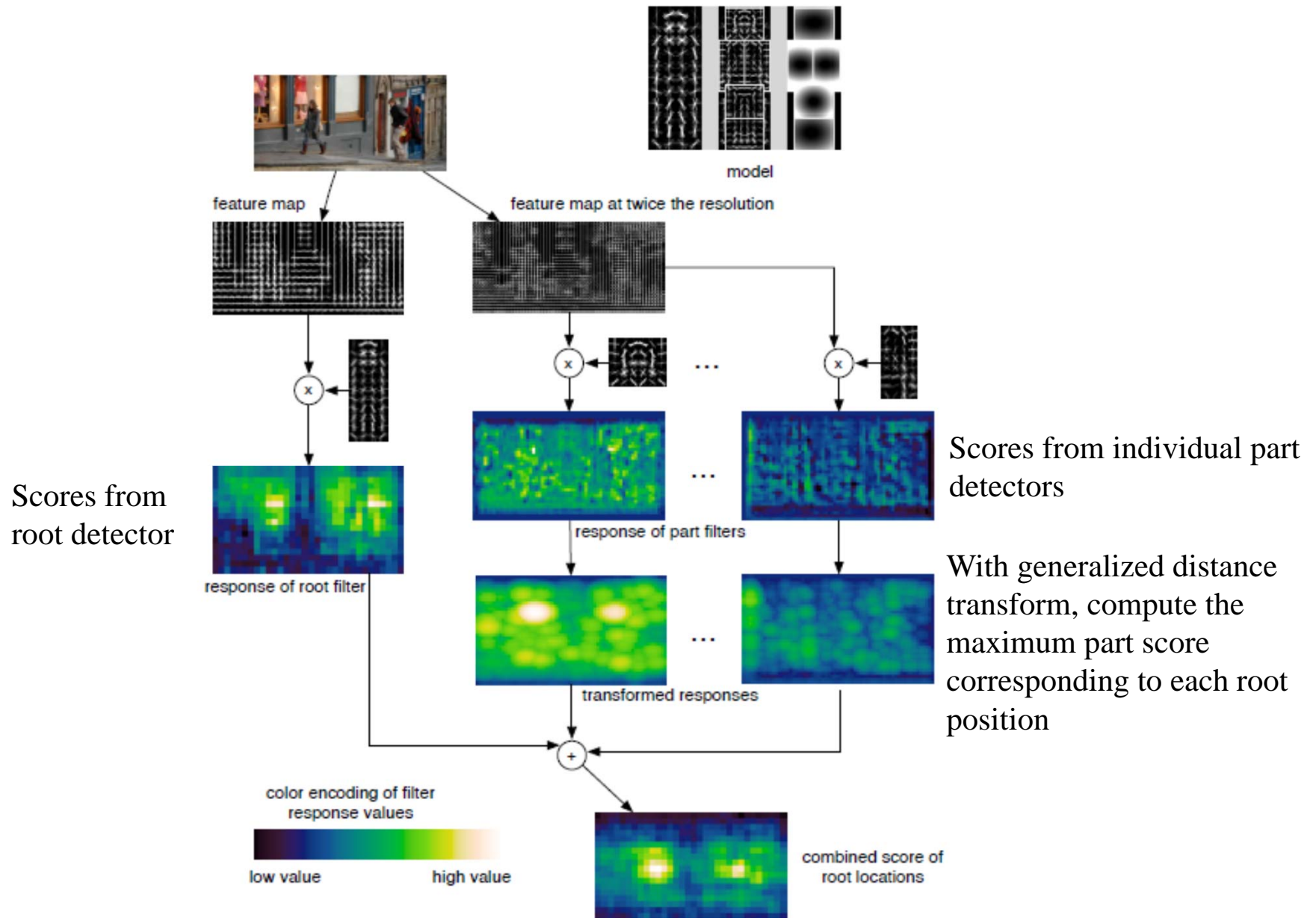


Part filters



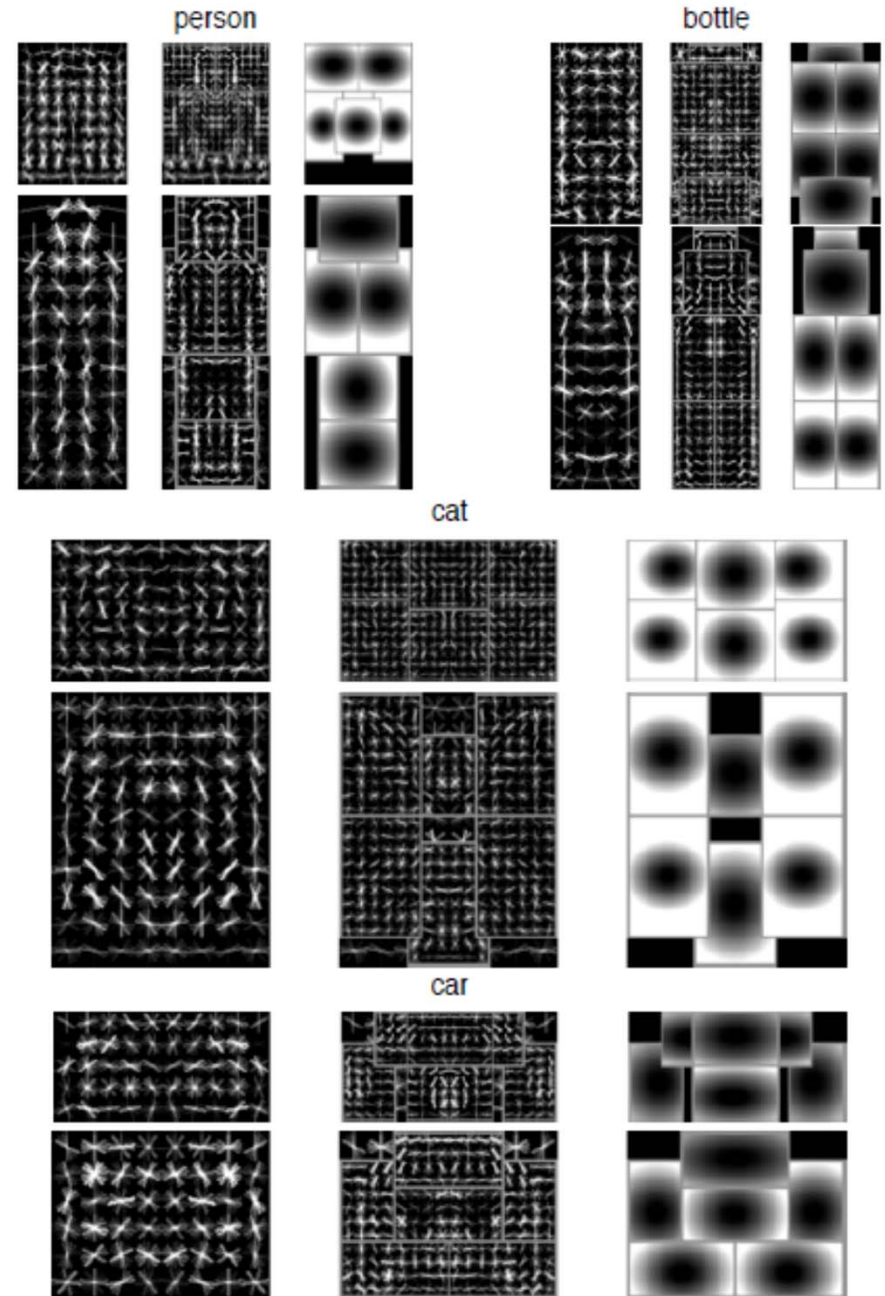
Spatial costs

# DPM: computing object score



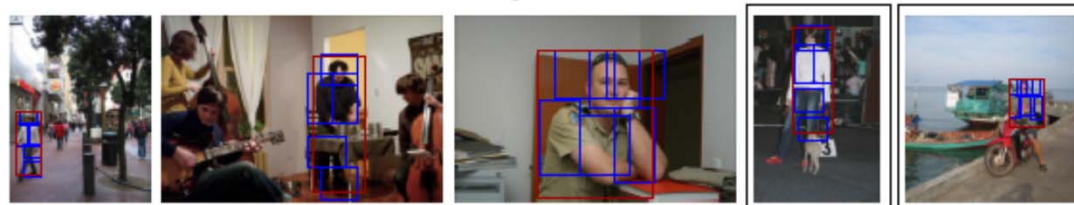
# DPM: mixture model

- Each positive example is modeled by one of  $M$  detectors
- In testing, all detectors are applied with non-max suppression

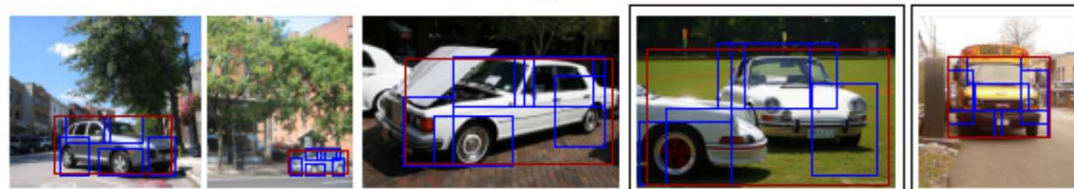




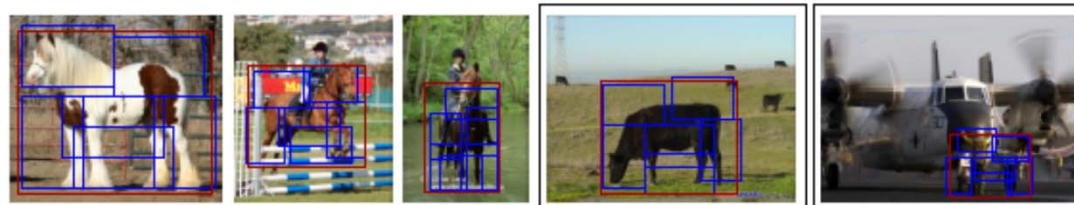
person



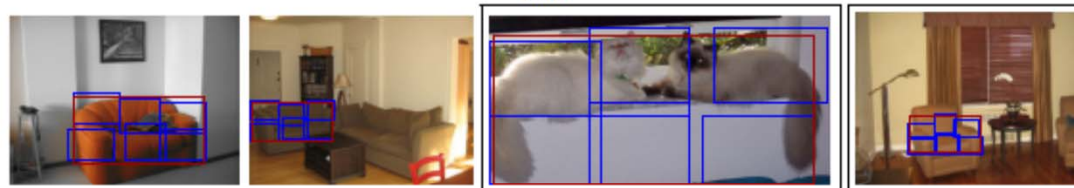
car



horse



sofa



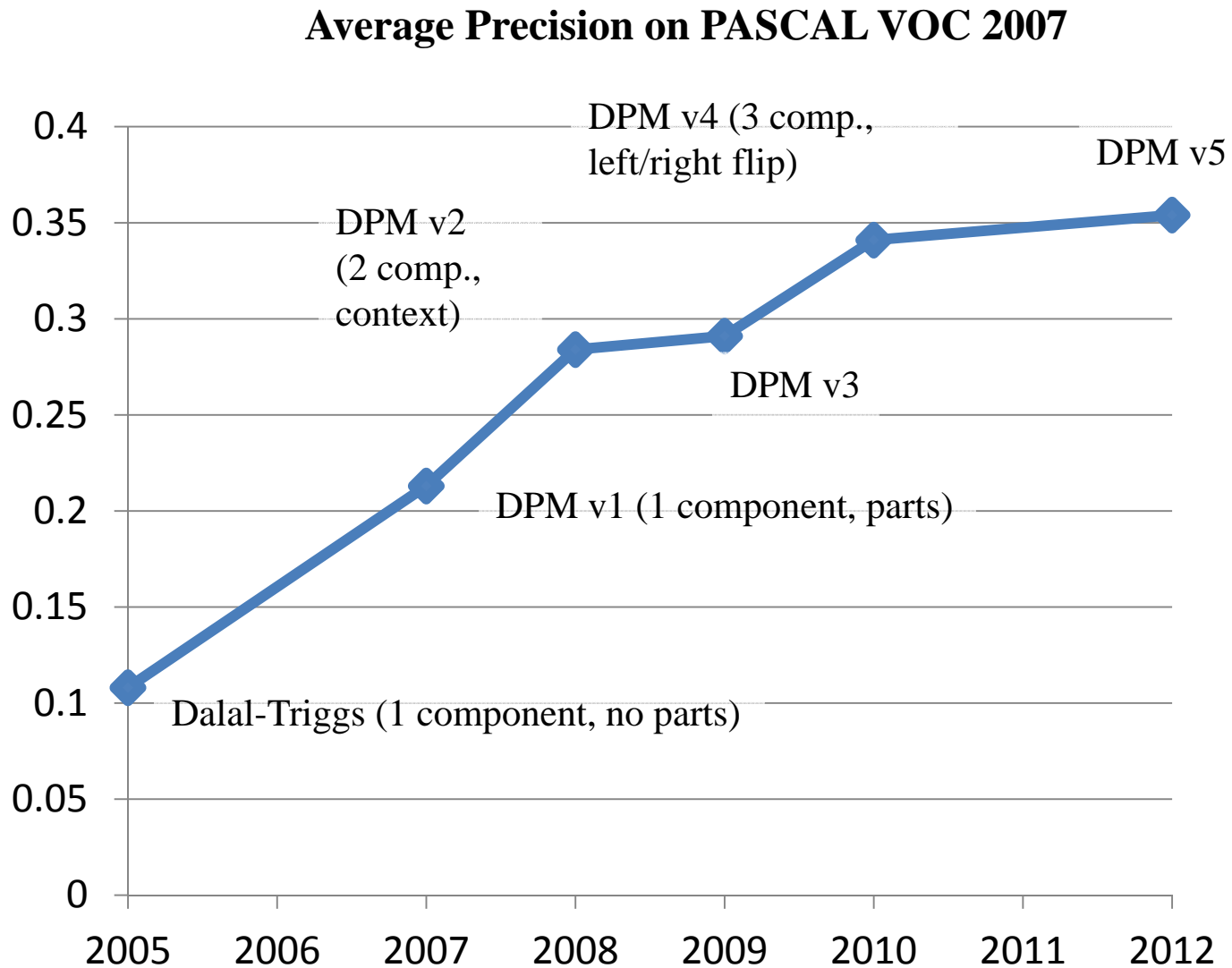
bottle



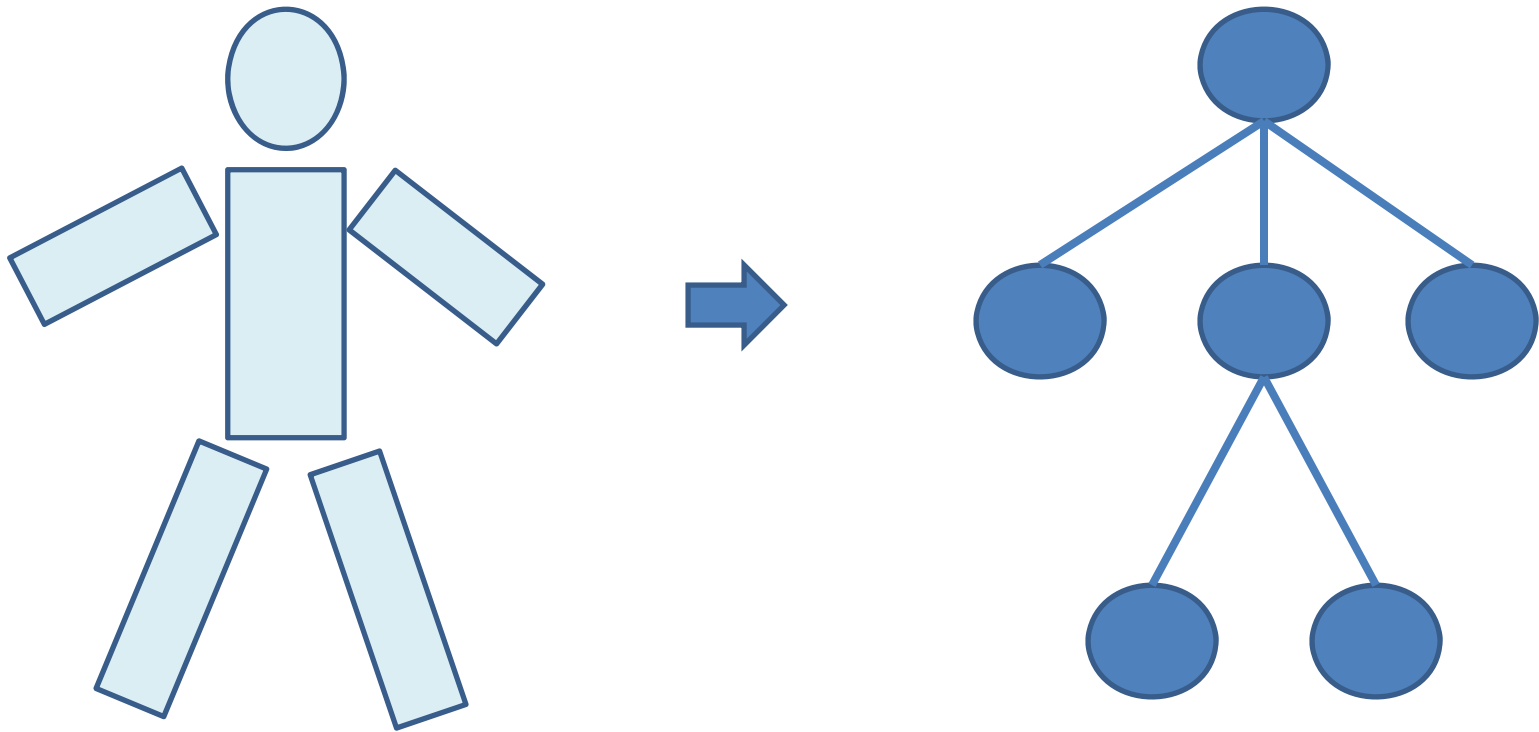
cat



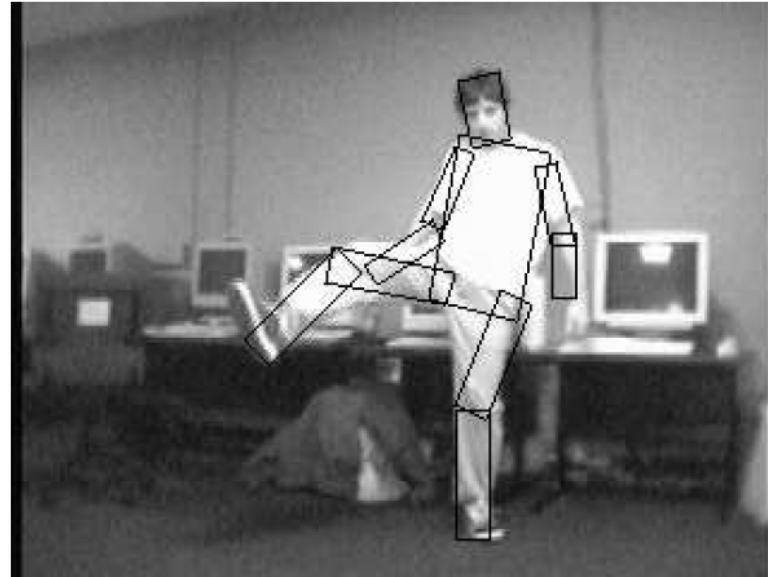
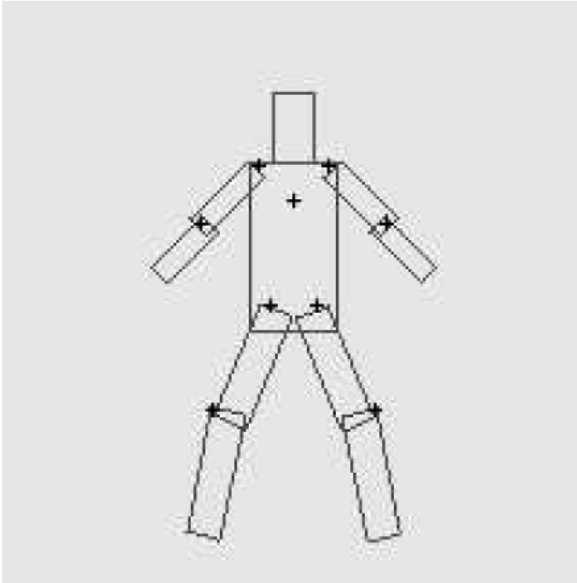
# Improvement over time for HOG-based detectors



# Tree-shaped model

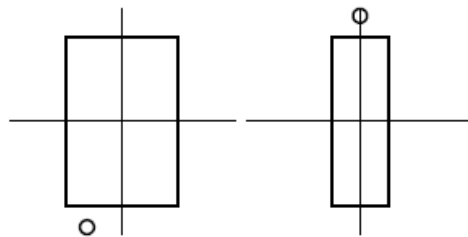


# Pictorial Structures

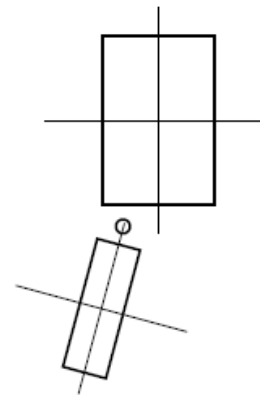


Part = oriented rectangle

Spatial model = relative size/orientation



a

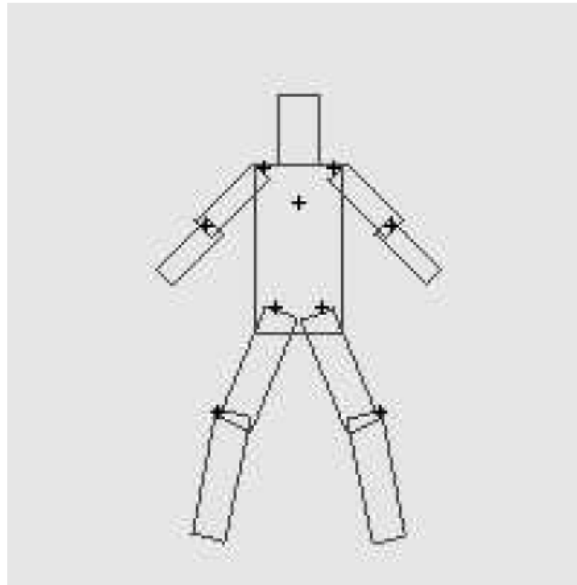


b

Felzenszwalb and Huttenlocher 2005



# Pictorial Structures Model



$$P(L|I, \theta) \propto \left( \prod_{i=1}^n p(I|l_i, u_i) \prod_{(v_i, v_j) \in E} p(l_i, l_j | c_{ij}) \right)$$

Appearance likelihood

Geometry likelihood

# Modeling the Appearance

- Any appearance model could be used
  - HOG Templates, etc.
  - Here: rectangles fit to background subtracted binary map
- Can train appearance models independently (easy, not as good) or jointly (more complicated but better)

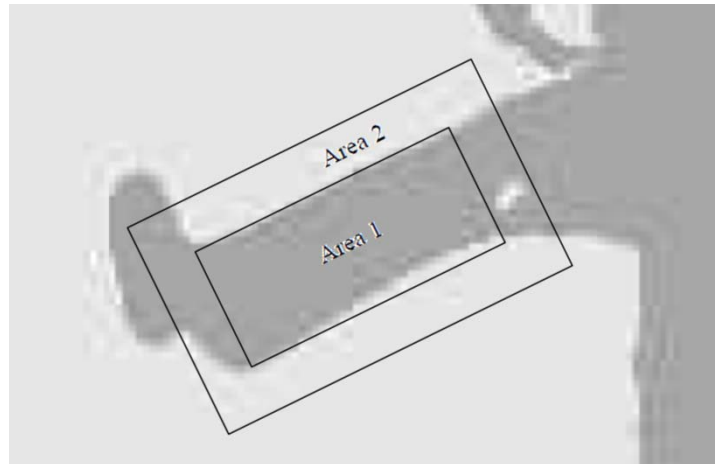
$$P(L|I, \theta) \propto \left( \prod_{i=1}^n p(I|l_i, u_i) \prod_{(v_i, v_j) \in E} p(l_i, l_j | c_{ij}) \right)$$

Appearance likelihood

Geometry likelihood

# Part representation

- Background subtraction

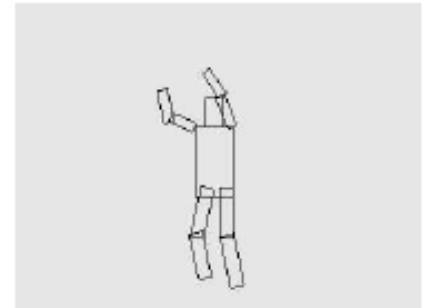
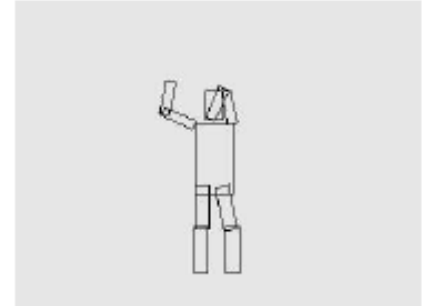
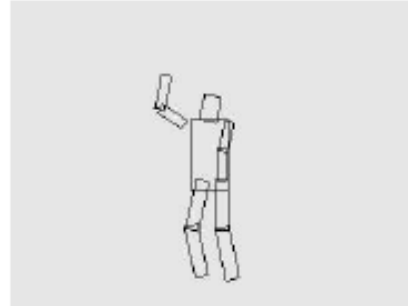


# Pictorial structures model

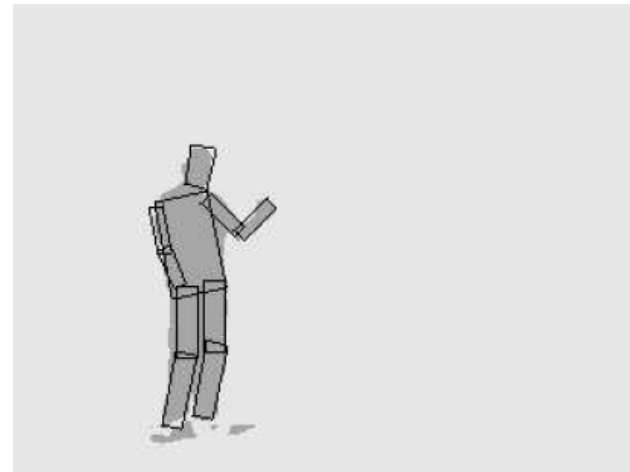
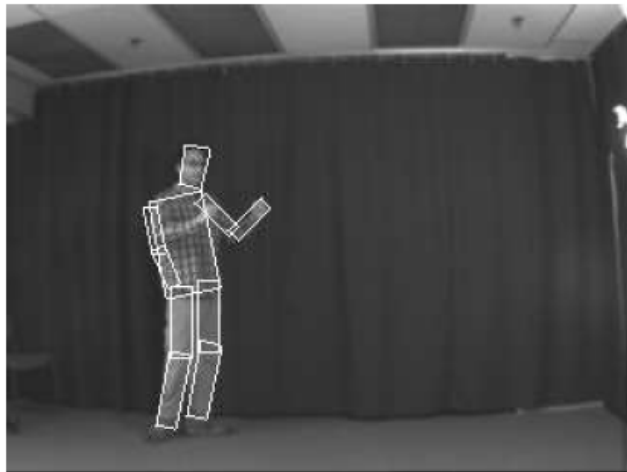
To create multiple likely candidates

- Sample root node, then each node given parent, until all parts are sampled

Sample poses from  
likelihood and  
choose best match



# Results for person matching



# Results for person matching

